Sliding Mode Control of a Bidirectional Buck/Boost DC-DC Converter with Constant Switching Frequency

A. Safari* (C.A.) and H. Ardi*

Abstract: In this paper, sliding mode control (SMC) for a bidirectional buck/boost DC-DC converter (BDC) with constant frequency in continuous conduction mode (CCM) is discussed. Since the converter is a high-order converter, the reduced-order sliding manifold is exploited. Because of right-half-plane zero (RHPZ) in the converter’s duty ratio to output voltage transfer function, sliding mode current controller is used. This controller benefits from various advantages such as fast dynamic response, robustness, stable and small variation of the settling time over a wide range of operation conditions. Because the converter operates in both step-down and step-up modes, two sliding manifold is derived for each mode. The existence and stability conditions are analyzed for both SMC in step-down and step-up modes. Finally, Simulation results are also provided to justify the feasibility of the controller using MATLAB/Simulink.

Keywords: DC-DC Converter, Sliding Mode Control, Current Controller, Constant Frequency.

1 Introduction

Environmental consequences of using fossil fuels and also depletion of these reserves in recent years have caused researches to be focused on renewable energies and interface converters. DC-DC converters are mostly used in these applications. In the last decade, lots of DC-DC converters have been proposed for various applications such as extracting maximum power from photovoltaic (PV) and fuel-cell (F.C) systems, portable devices, hybrid electric vehicles (HEV) and etc. [1-5]. Among DC-DC converters with different applications, BDCs have become necessary for HEV applications since energy storage systems are required for cold starting and battery recharging [4]. BDCs are used in HEVs [6-9], uninterrupted power supplies (UPS) [10-12], F.Cs [12-16], PVs [17,18], battery chargers [19-21] and many other industrial applications. BDCs are also used in DC micro-grid. Regulation of DC bus voltage and uninterrupte power supply to the sensitive loads are important in a DC micro-grid. Therefore, a battery-based energy storage system is required. As aforementioned, these storage systems are in need of BDCs. Controlling these converters is another important subject that has been researching. There are several control methods that are applied to DC-DC converters such as model predictive control (MPC) [22], passivity-based control [23], neural networks and state-space averaging [24], fuzzy logic [25], nonlinear H-infinity control and nonlinear carrier control [26], [27], direct control method [28] optimum LQR controller [29-31], nonlinear robust control with radial basis functions [32] and SMC [33-37]. With these controllers, the performance satisfaction such as fast response, stability, robustness, improvement of chaos behavior, and wide range of operating points are reported. SMC offers several benefits, namely, large signal stability, robustness, good dynamic response, system order reduction, and simple implementation [38]. There are several SMC methods such as voltage mode, current mode, reduced order, constant frequency and etc. Each method has various advantages and disadvantages which should be chosen according to the application.

In this paper, SMC is applied to a bidirectional DC-DC converter in CCM and existence and stability conditions are analyzed. The converter is proposed in...
[4] by the authors. The circuit prototype of the converter is shown in Fig. 1. The converter benefits from higher voltage gain in step-up mode and lower in step-down mode in comparison with conventional bidirectional buck/boost converter. As shown in this figure, the converter in step-up mode is based on the conventional boost converter. This cause the converter to be had RHPZ. Therefore, a current mode control should be applied to the converter. Besides, the converter is high order. Therefore, reduced-state sliding mode control is applied to the converter. Thus, reduced-state constant-frequency sliding mode current controller (CFSMCC) is applied to the converter and analyzed. This paper is divided to 6 sections. In section 2 and 3, the controllers for BDC are discussed in step-up and step-down modes, respectively. The sliding surfaces are obtained and the existence conditions are checked. Then, stability conditions are checked according to the achieved dynamic models of BDC. Control equations comprising signal controls and carriers are derived in section 4. Simulation results of the converter in step-up and step-down modes are studied under 3 different stages in section 5. Finally, the study is concluded in section 6. The nomenclature list of abbreviations are in Table 1.

2 CFSMCC for BDC in Step-Up Mode

In order to design SMC for BDC in step-up mode, state-space model of it should be obtained according to the converter’s operation principle in step-up mode. The equivalent circuit of BDC in step-up mode is shown in Fig. 1(b). S1 and S3 work as power switches in this mode.

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**Fig. 1** BDC and its equivalent circuits in the step-up and step-down mode: a) BDC, b) Equivalent circuit in the step-up mode, and c) Equivalent circuit in the step-down mode.

**Fig. 2** Current-flow path of BDC in the step-up mode: a) Mode I and b) Mode II.
Table 1 Nomenclature list of abbreviations.

<table>
<thead>
<tr>
<th>Phrase</th>
<th>Abbreviation</th>
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<tbody>
<tr>
<td>sliding mode control</td>
<td>SMC</td>
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<tr>
<td>buck/boost DC-DC converter</td>
<td>BDC</td>
</tr>
<tr>
<td>continuous conduction mode</td>
<td>CCM</td>
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<tr>
<td>right-half-plan zero</td>
<td>RHPZ</td>
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<tr>
<td>Photovoltaic</td>
<td>PV</td>
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<td>fuel-cell</td>
<td>FC</td>
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<td>hybrid electric vehicles</td>
<td>HEV</td>
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<tr>
<td>uninterrupted power supplies</td>
<td>UPS</td>
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<tr>
<td>model predictive control</td>
<td>MPC</td>
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<td>constant-frequency sliding mode current</td>
<td>CFSMCC</td>
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2.1 Operation Principle and State-Space Model of BDC

Fig. 2 shows the current-flow path in the different time intervals of BDC under CCM operation.

**Mode I:** During the interval \([t_0, t_1]\), \(S_1\) and \(S_3\) are turned on and \(S_2\) and \(S_4\) are turned off. As seen in Fig. 2(a), the energy of the input voltage \(V_L\) is transferred to the inductor \(L_1\). The inductors \(L_2\) is magnetized by the capacitor \(C\). The capacitor \(C_H\) is discharged to the load. The state-space equations in this mode can be obtained as follows:

\[
\begin{align*}
L_1 \frac{di_{L1}}{dt} &= v_L - v_C \\
L_2 \frac{di_{L2}}{dt} &= v_C - v_H \\
C \frac{dv_C}{dt} &= -i_{L2} \\
C_H \frac{dv_H}{dt} &= -v_H/R_L
\end{align*}
\]

**Mode II:** During this interval \([t_1, t_2]\), \(S_1\) and \(S_3\) are turned off and \(S_2\) and \(S_4\) are turned on. The current flow path of the proposed converter is depicted in Fig. 2(b). The energy of the \(V_i\) and the inductor \(L_1\) release to the capacitor \(C\). The capacitor \(C\) and the inductor \(L_2\) release their energies to the load. The state-space equations in this mode can be achieved as follows:

\[
\begin{align*}
L_1 \frac{di_{L1}}{dt} &= v_L - v_C \\
L_2 \frac{di_{L2}}{dt} &= v_C - v_H \\
C \frac{dv_C}{dt} &= i_{L1} - i_{L2} \\
C_H \frac{dv_H}{dt} &= i_{L2} - v_H/R_L
\end{align*}
\]

From equations (1) and (2), the state-space model of BDC can be written as:

\[
\begin{align*}
L_1 \frac{di_{L1}}{dt} &= v_L - \bar{u}v_C \\
L_2 \frac{di_{L2}}{dt} &= v_C - \bar{u}v_H \\
C \frac{dv_C}{dt} &= i_{L1} - i_{L2} \\
C_H \frac{dv_H}{dt} &= \bar{u}i_{L2} - \frac{v_H}{R_L}
\end{align*}
\]

where \(u = (0, 1)\) is the logic state of the power switch \(S\), and \(\bar{u} = 1 - u\) is the inverse logic of \(u\).

2.2 Design of Reduced-State CFSMCC for BDC in Step-Up Mode

In order to minimize the number of state variables that need to be sensed and also the number of signals that has to be generated in the controller, reduced-state CFSMCC is used [39]. In this controller, output voltage error \(v_{nf}\) and the inductor \(L_1\) current error \(i_{L1}\) are the controlled state variables. The reference of inductor current is considered as the amplified output voltage error:

\[
i_{nf} = K (v_{nf} - \beta v_H)
\]

where, \(v_{nf}\) and \(v_H\) are reference and instantaneous amount of output voltage, respectively. \(K\) is a gain which large number of it ensures a proper regulation of the output voltage and \(\beta\) is represents the feedback network ratio. The sliding surface of the controller can be written as follows:

\[
S = \alpha_1 x_1 + \alpha_2 x_2 + \alpha_3 x_3 + \alpha_4 x_4
\]

where \(\alpha_1 - \alpha_4\) are sliding coefficients and \(x_1 - x_4\) are state variables as follows:

\[
\begin{align*}
x_1 &= i_{nf} - i_{L1} \\
x_2 &= V_{nf} - v_H \\
x_3 &= \int [x_1 + x_2] dt \\
x_4 &= \int \left(\int [x_1 + x_2] dt\right) dt
\end{align*}
\]

By using just state variables \(x_1\) and \(x_2\), the output voltage and inductor current \(i_{L1}\) track their references exactly if the frequency is infinite (sliding controller is ideal). But, in constant finite frequency, the other state variables are also required. Having a double integral term \(x_4\) of the original state variables is to correct the steady-state errors. This idea is based on the control principle that the increased order of the controller improves the steady-state accuracy of the system [39]. According to operation principle of BDC and from equation (6), the derivative of sliding surface can be gained as follow:
By solving $dS/dt = 0$, the equivalent control input $u_{eq}$ can be obtained as follow:

$$
\frac{dS}{dt} = 0 \Rightarrow u_{eq} = 1 - \frac{K_{iCH} + yL - K_1(x_1 + x_2) - K_2\int(x_1 + x_2)dt}{v_c}
$$

where $K_1$, $K_2$, $K_3$ are

$$
K_1 = \frac{\alpha_1 L_1}{\alpha_i}, \quad K_2 = \frac{\alpha_2 L_1}{\alpha_i}, \quad K_3 = \frac{\beta L_1}{\alpha C_H} (K_{i1} + \alpha_3)
$$

$u_{eq}$ denotes the equivalent control signal of SM controller. This value is continuous and its amount is between 0 and 1. In order to ensure that the selected sliding coefficient is proper for controlling the converter, existence and stability conditions should be checked.

### 2.2.1 Existence Condition

It is necessary for a designed sliding surface to check the existence condition which says whether a trajectory is at the vicinity of the sliding manifold directed towards the sliding manifold. Therefore, the existence condition for a sliding surface in the domain of $0 < |S| < \delta$ can be expressed as

$$
\lim_{\delta \to 0} S(X,t) < 0 < \lim_{\delta \to 0} \dot{S}(X,t)
$$

Therefore, when $S \to 0^+$, $\dot{S} < 0$, $\ddot{u} = 0$

$$
\alpha_1 \left[ \frac{K \beta}{C_{CH}} - \frac{v_L}{L_i} \right] + \alpha_2 \left[ \frac{\beta}{C_H} i_{CH} \right]
$$

when $S \to 0$, $\dot{S} > 0$, $\ddot{u} = 1$

$$
\alpha_3 \left[ \frac{K}{C_H} i_{CH} - \frac{v_L}{L_i} \right] + \alpha_2 \left[ \frac{\beta}{C_H} i_{CH} \right]
$$

$$
\alpha_3 \left[ \frac{K}{C_H} i_{CH} - \frac{v_L}{L_i} \right] + \alpha_2 \left[ \frac{\beta}{C_H} i_{CH} \right]
$$

$$
\begin{align*}
\alpha_i \left[ \frac{K \beta}{C_{CH}} - \frac{v_L}{L_i} \right] + \alpha_2 \left[ \frac{\beta}{C_H} i_{CH} \right] \\
+ \alpha_3 \left[ \frac{K}{C_H} i_{CH} - \frac{v_L}{L_i} \right] + \alpha_2 \left[ \frac{\beta}{C_H} i_{CH} \right]
\end{align*}
$$

$$
\alpha_4 \left[ \frac{(K + 1)(v_{ref} - \beta v_H)}{K_{CL} L_i} i_{L1} \right] < 0
$$

$\Rightarrow$\( S(X,t) < 0 < \dot{S}(X,t) \)

$$
\alpha_1 \left[ \frac{K \beta}{C_{CH}} - \frac{v_L}{L_i} \right] + \alpha_2 \left[ \frac{\beta}{C_H} i_{CH} \right]
$$

$$
\alpha_3 \left[ \frac{K}{C_H} i_{CH} - \frac{v_L}{L_i} \right] + \alpha_2 \left[ \frac{\beta}{C_H} i_{CH} \right]
$$

$$
\alpha_4 \left[ \frac{(K + 1)(v_{ref} - \beta v_H)}{K_{CL} L_i} i_{L1} \right] < 0
$$

$\Rightarrow$\( S(X,t) < 0 < \dot{S}(X,t) \)

Therefore, $\alpha_{eq}$ is steady state condition. It means there will be not any changes in state variables which means:

$$
\begin{align*}
\text{Equilibrium Point} & \\
\text{Ideal Sliding Dynamics} &
\end{align*}
$$
\[
\begin{align*}
\frac{di_{L1}}{dt} &= \frac{di_{L2}}{dt} = \frac{dv_C}{dt} = \frac{dv_H}{dt} = 0 \\
\end{align*}
\]

Therefore, from equation (3), the equilibrium point can be obtained as follows:

\[
\begin{align*}
V_c &= \sqrt{V_H V_L} \\
I_{L1} &= \frac{V_H}{V_L} R_{L1} \\
I_{L2} &= \frac{V_H}{R_{L2}} V_L
\end{align*}
\]

where \(V_c, V_L, V_H, I_{L1}, I_{L2}\) are capacitor \(C\), input and output voltages, the currents of inductors \(L_1\) and \(L_2\) in steady state, respectively.

**Linearization of Ideal Sliding Dynamics**

Separating the ideal sliding dynamic’s equation into its DC and AC terms and considering the fact that the DC terms are much larger than ac terms, the linearization of the ideal sliding dynamics around the equilibrium point can be obtained as (17), where

\[
\lambda = 1 - K, I_{L2} = 1 - \frac{K V_H}{R_L} \sqrt{V_H V_L}
\]

The characteristic equation of the linearized system can be achieved as:

\[
\begin{align*}
| s - a_{11} & -a_{12} & -a_{13} & -a_{14} & -a_{15} & -a_{16} | \\
- & s - a_{22} & -a_{23} & -a_{24} & -a_{25} & -a_{26} | \\
- & - & s - a_{33} & -a_{34} & -a_{35} & -a_{36} | \\
- & - & - & s - a_{44} & -a_{45} & -a_{46} | \\
- & - & - & - & s - a_{55} & -a_{56} | \\
- & - & - & - & - & s - a_{66} |
\end{align*}
\]

where the elements are as (20).
By applying the Routh-Hurwitz criterion to the characteristic equation in (20), the conditions which should be satisfied for the system’s stability can be obtained. By these conditions and the existence conditions, the sliding coefficients can be found.

3 CFSSMCC for BDC in Step-Down Mode

The equivalent circuit of BDC in step-down mode is depicted in Fig. 1(c). $S_3$ and $S_4$ work as power switches in this mode. Designing SMC for BDC in step-down mode is same as step-up mode with the same steps.

3.1 Operation Principle and State-Space Model of BDC

The current-flow path in the different time intervals of BDC in step-down mode and under CCM operation is exhibited in Fig. 3.

Mode I: During the interval $[t_0, t_1]$, $S_2$ and $S_4$ are turned on and $S_1$ and $S_3$ are turned off. As seen in Fig. 3(a), the energy of the input voltage $V_H$ is transferred to the inductor $L_2$ and the capacitor $C$. The capacitor $C$ charges the inductor $L_1$ magnetizes the inductor $L_1$. The state-space equations in this mode can be achieved as follows:

$$
\begin{align}
L_1 \frac{di_{L_1}}{dt} &= v_C - v_L \\
L_2 \frac{di_{L_2}}{dt} &= v_H - v_C \\
C \frac{dv_C}{dt} &= i_{L_2} - i_{L_1} \\
C \frac{dv_H}{dt} &= i_{L_1} - \frac{v_H}{R_L}
\end{align}
$$ (21)

Mode II: During this interval $[t_1, t_2]$, $S_2$ and $S_4$ are turned off and $S_1$ and $S_3$ are turned on. The current-flow path of the proposed converter is depicted in Fig. 4(b). The inductor $L_2$ releases its energy to the capacitor $C$. The inductor $L_1$ is demagnetized to the load. The state-space equations in this mode can be obtained as follows:

$$
\begin{align}
L_1 \frac{di_{L_1}}{dt} &= -v_R \\
L_2 \frac{di_{L_2}}{dt} &= -v_C \\
C \frac{dv_C}{dt} &= i_{L_2} \\
C \frac{dv_H}{dt} &= i_{L_1} - \frac{v_H}{R_L}
\end{align}
$$ (22)

From equations (1) and (2), the state-space model of BDC can be written as:

$$
\begin{align}
L_1 \frac{di_{L_1}}{dt} &= uv_C - v_L \\
L_2 \frac{di_{L_2}}{dt} &= uv_H - v_C \\
C \frac{dv_C}{dt} &= i_{L_2} - ui_{L_1} \\
C \frac{dv_H}{dt} &= i_{L_1} - \frac{v_H}{R_L}
\end{align}
$$ (23)

3.2 Design of Reduced-State CFSSMCC for BDC in Step-Down Mode

The sliding surface of the controller can be written as follows:

$$
S = \alpha_1 x_1 + \alpha_2 x_2 + \alpha_3 x_3 + \alpha_4 x_4
$$ (24)

where $\alpha_1 - \alpha_4$ are sliding coefficients and $x_1 - x_4$ are state variables as follows:

$$
\begin{align}
x_1 &= i_{\text{ref}} - i_{L_2} \\
x_2 &= V_{\text{ref}} - v_L \\
x_3 &= \int [x_1 + x_2] \, dt \\
x_4 &= \int \left( \int [x_1 + x_2] \, dt \right) \, dt
\end{align}
$$ (25)

The reference of inductor $L_2$ current in step-down mode is

$$
i_{\text{ref}} = K (V_{\text{ref}} - \beta v_L)
$$ (26)

![Fig. 3 Current-flow path of BDC in the step-down mode: (a) Mode I and (b) Mode II.](image-url)
The derivative of sliding surface can be gained as follow
\[
\frac{dS}{dt} = \alpha_1 \left[ -K_1 i_{cl} + \frac{C_L}{v_H - v_C} \right] + \alpha_2 \left[ -\frac{\beta}{C_L} i_{cl} \right] + \alpha_3 \left[ (K+1)(V_{mf} - \beta v_L) - i_{l2} \right] + \alpha_4 \int [(K+1)(V_{mf} - \beta v_L) - i_{l2}] dt
\]
(27)

By solving \( dS/dt = 0 \), the equivalent control input \( u_{eq} \) can be obtained as follow
\[
\frac{dS}{dt} = 0 \Rightarrow u_{eq} = \frac{-K_1 i_{cl} - K_1(x_1 + x_2) - K_3(x_1 + x_2) dt}{v_H}
\]
(28)

where
\[
K_1 = \frac{\alpha_1 L_2}{\alpha_1}, K_2 = \frac{\alpha_2 L_2}{\alpha_1}, K_3 = \frac{\beta L_2 (K_1 + \alpha_2)}{\alpha C_L}
\]
(29)

By knowing the sliding surface and its derivation, the existence condition can be checked whether the sliding surface is proper for controlling the converter. It is worth noting that this converter in step-down mode does not have RHPZ. Therefore, just output voltage error can be considered as state variable in the sliding surface. However, in this case, the inductor current \( L_2 \) will be oscillated very much which causes the other components endures excess current stresses. Therefore, considering inductor \( L_2 \) current error as another state variable would be more proper.

### 3.2.1 Existence Condition

The existence condition for a sliding surface can be expressed like step-up mode. When \( S > 0, \dot{S} < 0, u = 1 \)
\[
\alpha_1 \left[ -K_1 i_{cl} + \frac{v_H - v_C}{C_L} \right] + \alpha_2 \left[ -\frac{\beta}{C_L} i_{cl} \right] + \alpha_3 \left[ (K+1)(V_{mf} - \beta v_L) - i_{l2} \right] + \alpha_4 \int [(K+1)(V_{mf} - \beta v_L) - i_{l2}] dt < 0
\]
(30)

When \( S < 0, \dot{S} > 0, u = 0 \)
\[
\alpha_1 \left[ \frac{K \beta}{C_L} i_{cl} + \frac{v_C}{L_2} \right] + \alpha_2 \left[ \frac{\beta}{C_L} i_{cl} \right] + \alpha_3 \left[ (K+1)(V_{mf} - \beta v_L) - i_{l2} \right] + \alpha_4 \int [(K+1)(V_{mf} - \beta v_L) - i_{l2}] dt > 0
\]
(31)

### 3.2.2 Stability Condition

The steps which followed in step-up mode for checking the stability condition should also be followed in step-down mode. Therefore, in order to avoid repetition, just the results of calculations are discussed. The equilibrium point of BDC in step-down mode can be obtained as
\[
\begin{align*}
V_C &= \sqrt{v_H V_L} \\
I_{L1} &= \frac{V_L}{R_L} \\
I_{L2} &= \frac{V_L}{R_L} \sqrt{\frac{V_H}{V_L}}
\end{align*}
\]
(33)

The characteristic equation of the linearized system around the equilibrium point can be achieved like equation (19) with the replacement of \( v_H \) by \( v_L \) and \( C_H \) by \( C_L \). Therefore,
\[
\begin{align*}
a_{t_1} &= -K_1, b_{t_1} = 0, c_{t_1} = \frac{1}{L_1}, d_{t_1} = \frac{1}{L_2}, e_{t_1} = 1; \\
a_{t_2} &= \frac{K_1 + K_2}{L_1}, b_{t_2} = 0, c_{t_2} = \frac{1}{L_1}, d_{t_2} = \frac{1}{L_2}, e_{t_2} = \frac{V_L}{R_L} \\
a_{t_3} &= \frac{K_1 + K_2}{L_1}, b_{t_3} = 0, c_{t_3} = \frac{1}{L_1}, d_{t_3} = \frac{1}{L_2}, e_{t_3} = \frac{V_L}{R_L} \\
a_{t_4} &= \frac{K_1}{L_1}, b_{t_4} = 0, c_{t_4} = \frac{1}{L_1}, d_{t_4} = \frac{1}{L_2}, e_{t_4} = \frac{V_L}{R_L} \\
a_{t_5} &= \frac{K_1}{L_1}, b_{t_5} = 0, c_{t_5} = \frac{1}{L_1}, d_{t_5} = \frac{1}{L_2}, e_{t_5} = \frac{V_L}{R_L}
\end{align*}
\]
(34)
By applying the Routh-Hurwitz criterion to the characteristic equation in (33) and considering the existence conditions, the sliding coefficients can be found in this mode.

4 Derivation of Control Equations for CFSMCC

In order to simulate or implement CFSMCC for a converter, the translation of equivalent control signal ueq to duty ratio should be derived. While control equation depends on ueq, it is different for step-up and step-down mode. Since the frequency of the controller is fixed, control signal should be compared with a triangular or saw-tooth carrier wave. Therefore, a signal control and the peak value of carrier should be obtained. As aforementioned before, ueq is bounded by 0 and 1. Therefore, signal controls and the peak value of carriers in step-up and step-down modes is selected as follows:

Step-up mode:
\[ u_S = k_1 \left( \int [(k + 1)(V_{nf} - V_H) - i_{L1}]dt \right) + k_2 \left( (k + 1)(V_{nf} - V_H) - i_{L1} \right) - k_s C_{CH} + v_c - v_L \]
\[ v_{amp} = v_c \]

Step-down mode:
\[ u_C = k_1 \left( \int [(k + 1)(V_{nf} - V_L) - i_{L2}]dt \right) + k_2 \left( (k + 1)(V_{nf} - V_L) - i_{L2} \right) - k_s C_{CL} + v_c \]
\[ v_{amp} = V_H \]

5 Simulation Results

In order to justify the feasibility of the designed CFSMCC for BDC, simulation results by MATLAB/Simulink are discussed in this section. Fig. 4 shows CFSMCC for BDC in step-up and step-down modes. The switching frequency is fixed and equals 40KHz. The converter is simulated under 400W which is changed with step changes of output voltages and output power in stages 2 and 3, respectively. During the simulation, the low voltages, high voltages and load resistance RL are changed in order to verify the performance of CFSMCC according to transient responses.

The simulation results are divided into 3 stages. In these stages, the transient responses of the converter’s voltages and currents with step changes of them are studied. The step changes are applied to the converter at \( t = 0.05s \) and \( t = 0.1s \).

5.1 Simulation Results in Step-Up Mode

Stage 1:

In stage 1, the input voltage of BDC in step-up mode is changed. The transient response of the converter’s voltages and currents are shown in Fig. 5. This picture shows the simulation results of BDC in step-up mode for input voltage \( V_i \) step changes from 25V to 30V at \( t = 0.05s \) and 30V to 25V at \( t = 0.1s \) with load resistance of 50Ω. \( V_H \) in this mode is 150V and output power is 450W. As shown in Fig. 5(a), at \( t = 0.05s \), the output voltage \( V_H \) has overshoot of 11V (7.7%). The steady state output voltage error is 8V which is about 5%. At \( t = 0.1s \), undershoot of output voltage is 12V (8.5%). The steady state error and the ripple of output voltage are about 8% (4%) and 0.75V (0.5%), respectively. The inductor L2 current is shown in Fig. 5(b). The overshoot in second step change is about 10A (50%).

Stage 2:

In this stage, the reference value of output voltage is changed from 150V to 140V at \( t = 0.05s \) and 140V to 150V at \( t = 0.1s \) with load resistance of 50Ω. The simulation results of this stage are shown in Fig. 6. As shown in Fig. 6(a), the output voltage sets at its reference value with steady state error of about 6%, voltage ripple of 1V (0.7%) and no overshoot and undershoot. The overshoot, undershoot and setting time of inductor \( L_2 \) current is same as output voltage (Fig. 6(b)).

Stage 3:

In this stage, the load resistance is changed from 50Ω to 75Ω at \( t = 0.05s \) and from 75Ω to 50Ω at \( t = 0.1s \). Since the output voltage is fixed at 142V, the output power is changed from 400W to 270W and vice versa. The simulation results of this stage are shown in Fig. 7. Since the components of the converters are considered as ideal, the output voltage changes are negligible (Fig. 7(a)). Fig. 7(b) shows the inductor \( L_2 \) current. As shown in this picture, the overshoot and undershoot of \( i_{L2} \) is negligible.

5.2 Simulation results in step-down mode

Stage 1:

In this stage, the input voltage VH of BDC in step-down mode is changed from 150V to 140V at \( t = 0.05s \) and from 140V to 150V at \( t = 0.1s \) with load resistance of 2Ω. The simulation results of this stage are shown in Fig. 8.

As shown in Fig. 8(a), the output voltage \( V_L \) has overshoot and undershoot of 0.5V (2%), steady state error of 0.5V (2%) and voltage ripple of 0.03V. the low voltage ripple in this mode and low overshoot and
undershoot is because of inductor $L_1$ which is connected to the output. The inductor $L_1$ current is shown in Fig. 8(b). As shown in this picture, the inductor $L_1$ current is about 12A with ripple of 0.5A. The transient changes of this current are negligible.

**Stage 2:**

In this stage, the reference value of output voltage is changed from 30V to 25V at $t = 0.05s$ and from 25V to 30V at $t = 0.1s$ with load resistance of 2Ω. As shown in Fig. 9(a), the output voltage $V_L$ tracks the reference value with steady state error of about 0.8% and voltage ripple of 0.02V (0.066%) and no overshoots and undershoots. Fig. 9(b) shows the inductor $L_1$ current. As shown in this picture, undershoot of the current at $t = 0.05s$ is about 8A (38%) and the overshoot at $t = 0.1s$ is about 6A (40%).

![Simulated circuit of reduced-State CFSMCC for BDC: a) Step-up mode and b) Step-down mode.](image-url)
Fig. 5 Simulation results of BDC in step-up mode, stage 1: a) Output voltage $V_H$ and b) Inductor current $i_{L2}$.

Fig. 6 Simulation results of BDC in step-up mode, stage 2: a) Output voltage $V_H$ and b) Inductor current $i_{L2}$.  

Fig. 7 Simulation results of BDC in step-up mode, stage 3: a) Output voltage $V_H$ and b) Inductor current $i_{L2}$.

Fig. 8 Simulation results of BDC in step-down mode, stage 1: a) Output voltage $V_H$ and b) Inductor current $i_{L2}$. 
Fig. 9 Simulation results of BDC in step-down mode, stage 2: a) Output voltage $V_L$ and b) Inductor current $i_{L2}$.

Stage 3:

In this stage, load resistance is changed from $2\Omega$ to $1\Omega$ at $t = 0.05s$ and vice versa at $t = 0.1s$. The output power then is changed from 300W to 200W and vice versa. The simulation results of this stage are shown in Fig. 10. As shown in Fig. 10(a) the output voltage $V_L$ has overshoot of 0.5V at $t = 0.05s$, undershoot of 0.5V at $t = 0.1s$, steady state error of 0.6V and negligible voltage ripple. The inductor $L_1$ current waveform is shown in Fig. 10(b). As shown in this picture, the inductor $L_1$ current is changed from 12A to 8A at $t = 0.05s$ and vice versa at $t = 0.1s$ with ripple of 0.5A. The transient changes are negligible. From studied simulation results, it can be concluded that the designed CFSMCC for BDC has good performance. The transient responses steady state errors are acceptable.

In Fig. 11, a PI controller is applied to BCD in step-down mode. The output load is $2\Omega$. The reference is changed from 30V to 25V and 25V to 30V at $t = 0.02s$ and $t = 0.04s$, respectively. The output load is also changed from $2\Omega$ to $1\Omega$ and vice-versa at $t = 0.06s$ and $t = 0.08s$, respectively. As shown in this figure, the overshoots and setting times of this controller is higher than SMC.

6 Conclusion

In this paper, SM control for BDC is discussed. The proposed proper control for BDC in this paper is reduced-state CFSMCC. The controller is designed for both step-up and step-down modes individually. The sliding surfaces are chosen using state space model of the converter. The dynamic models of the converter in both step-up and step-down modes are studied. According to sliding surfaces and their derivative equations and also dynamic models of BDC, the feasibility of them is proved by checking existence and stability conditions. At the end, the signal controls and the carriers are obtained. Finally, the designed controller is applied to the converter in MATLAB/Simulink under various high and low voltages and output powers. The transient response of the simulated converter is studied and the feasibility of the designed controller is justified.
Fig. 10 Simulation results of BDC in step-down mode, stage 3: a) Output voltage $V_H$ and b) Inductor current $i_{L2}$.

Fig. 11 Simulation results of BDC in step-down mode with PI controller: a) Output voltage $V_L$ and b) Inductor current $i_{L1}$. 
References


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