

# A generalized ABFT technique using a fault tolerant neural network

A. Moosavienia and K. Mohammadi

**Abstract:** In this paper we first show that standard BP algorithm cannot yield to a uniform information distribution over the neural network architecture. A measure of sensitivity is defined to evaluate fault tolerance of neural network and then we show that the sensitivity of a link is closely related to the amount of information passes through it. Based on this assumption, we prove that the distribution of output error caused by s-a-0 (stuck at 0) faults in a MLP network has a Gaussian distribution function. UDBP (Uniformly Distributed Back Propagation) algorithm is then introduced to minimize mean and variance of the output error. Simulation results show that UDBP has the least sensitivity and the highest fault tolerance among other algorithms such as WRTA, N-FTBP and ADP. Then a MLP neural network trained with UDBP, contributes in an Algorithm Based Fault Tolerant (ABFT) scheme to protect a nonlinear data process block. The neural network is trained to produce an all zero syndrome sequence in the absence of any faults. A systematic real convolution code guarantees that faults representing errors in the processed data will result in notable nonzero values in syndrome sequence. A majority logic decoder can easily detect and correct single faults by observing the syndrome sequence. Simulation results demonstrating the error detection and correction behavior against random s-a-0 faults are presented too.

**Keywords:** fault tolerance, back propagation, MLP network, function approximation, ABFT, convolutional codes, majority logic decoding.

## 1 Introduction

One of the most attractive features of neural networks is their capability to model nonlinear systems in addition to their intrinsic fault tolerant ability. In fact neural networks have been successfully used for fault diagnosis in nonlinear systems [1], [2], [3]. However recent researches [4], [5], [31], show that these networks are not really fault tolerant. Indeed, there are always many nodes in a large neural network that do not contribute in neural network function, so in contrast to using redundant nodes, fault tolerance is not improved. On the other side, we can often find nodes that are too important and their failure can cause a system crash.

On the other hand, using conventional fault tolerant techniques, such as Triple Modular Redundancy (TMR) and Triple Time Redundancy (TTR) [6], yields to either a very expensive and large system or a long time overhead. Algorithm based fault tolerant techniques are good choices for error detection and correction in linear systems, using cheap and small variations in hardware or software [7].

In this paper we will first introduce a fault tolerant neural network architecture, based on MLP (Multilayer Perceptron) and a new learning algorithm, based on conventional error Back Propagation (BP) algorithm. Then we utilize this neural network in an ABFT architecture using convolutional codes to correct single faults in a nonlinear system.

Two main approaches have been proposed to improve fault tolerance in an artificial neural network: 1)

modified learning algorithms and 2) modified architectures. Most of the reported papers deal with learning phase or algorithm. In fact, it is believed that distributed architecture of neural networks is not suitably utilized by current common learning algorithms such as BP, in order to have or enhance fault tolerance in neural networks. In [8] this enhancement is achieved by manipulating the gradient of sigmoid function during learning phase. [9] and [10] have used the well known method of fault injection during learning procedure and shown that fault behavior of neural network can be greatly improved against stuck-at-0 and stuck-at-1 faults. [11] have introduced a network called "Maximally Fault Tolerant neural Network", which its weight coefficients are estimated through a nonlinear optimization problem to get the maximum allowable fault tolerance in the neural network. There are few reports considering the neural network architecture to improve fault tolerance. [12] studied feedback neural networks with hard limiting outputs. The results show that fault tolerant of such networks can not be improved through adding more nodes. [13] addressed some modification on architecture such as addition/deletion nodes but it is still based on learning procedure. In [14] a method is presented to break critical nodes in a trained MLP to have a predefined level of fault tolerance. In [4] a two layer feed forward neural network is modified to detect faulty links based on the assumption that the weights of all links are known and stored in a memory. The following section of this paper introduces briefly the ABFT concepts. Section 3 describes the convolution code used in this paper. Then in section 4 a Multilayer Perceptron network with conventional BP algorithm is presented. In section 5 we introduce fault model and sources in a neural network. Section 6 and 7 contain our modified architecture and learning algorithm respectively. Simulation details and results are provided in section 8 and finally section 9 concludes the main advantages of the proposed method.

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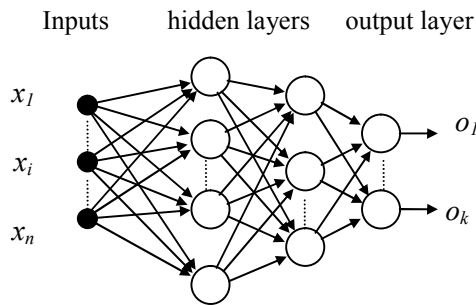


Self-orthogonal codes are one class of codes that are completely orthogonalizable. In such a code, for each information error bit the set of all syndrome bits that involve that bit, form an orthogonal check set on that bit without the need for adding syndrome bits. Using these codes make an easier implementation of majority-logic decoding.

### 3 Data distribution in a MLP network

MLP network consists of several cascaded layers of neurons with sigmoid activation functions [27]. The input vector, feeds into each of the first layer neurons, the outputs of this layer feed into each of the second layer neurons and so on, as shown in Fig. 2.

The layers between input and output are called hidden layers. In this paper feed forward I-H-O neural networks are considered. Which H, O and I denote nodes in input layer, hidden layer and output layer respectively.



**Fig. 2** Architecture of a typical MLP network.

To evaluate the fault tolerance of a MLP network we present two definitions as the following:

**Definition 1:**  $s(w_i)$  is defined as the sensitivity of neural network to weight  $w_i$  that is the effect on mean square error (MSE) when  $w_i$  is forced to zero. Sensitivity can be measured by:

$$s(w_i) = |E(W') - E(W)| \quad (6)$$

In which  $W=(w_1, \dots, w_k)$  denotes the vector of all weights of the neural network and  $W'$  is the new vector in which  $w_i$  is stuck at zero.  $E(W)$  is the MSE for weight vector  $W$ , over all training set.

**Definition 2:** The  $I_{ij}$ , the information package (IP) of link  $w_{ij}$ , is defined as:

$$I_{ij} = oh_i \times w_{ij} \quad (7)$$

Where  $oh_i$  is the output of hidden neuron  $i$  and  $w_{ij}$  is the connecting weight between hidden neuron  $i$  and output neuron  $j$ .

Most often the nodes are fully connected, i.e., every node in layer  $l$  is connected to every node in layer  $l+1$ . In this paper we assume input vector as the first layer in the neural network. MLP networks can easily perform Boolean logic operations, pattern recognition, classification and nonlinear function approximation [28]. Usually output neurons use linear activation functions rather than nonlinear sigmoid, since this tends to make learning easier. MLP is a supervised neural network that learns through examples and BP is the most common used learning algorithm that is a steepest descent gradient-based algorithm. In this paper we assume that the activation function of each neuron is a

bipolar sigmoid by the following equation:

$$f(s_i) = \frac{1 - \exp(-s_i)}{1 + \exp(-s_i)} \quad (8)$$

$$s_i = \sum_j w_{ij} \times x_j - \theta_i \quad (9)$$

$x_j$  is neuron  $j$ 's output and  $\theta_i$  is a bias value for the neuron  $i$ . Standard BP algorithm changes  $w_{ij}$  in order to reduce the output error,  $E$ , defined by:

$$E = \frac{1}{2} \sum_i (t_i - o_i)^2 \quad (10)$$

Where  $t_j$  is  $j$ 'th output target and  $o_j$  is the  $j$ 'th estimated output [29].

Using the steepest descent gradient rule, the change of  $w_{ij}$  is expressed as:

$$\Delta w_{ij} = -\eta \frac{\partial E}{\partial w_{ij}} \quad (11)$$

$\eta$  is a positive number called "learning rate" which determines step size in  $w_{ij}$  changes. Selecting a suitable  $\eta$  value plays an important role in network learning convergence [30].

Back propagation algorithm says that:

$$\Delta w_{ij} = \eta \delta_i^p o_j^p \quad (12)$$

$$\delta_i^p = (t_i^p - o_i^p) \cdot f'(u_i^p) \quad (13)$$

$$\delta_i^p = \left( \sum_k w_{ki} \delta_k^p \right) \cdot f'(u_i) \quad (14)$$

Where equation (13) is for an output layer and equation (14) is for neurons in hidden layer.  $f'()$  is the derivative of the sigmoid and is calculated by:

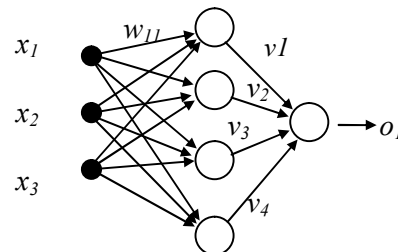
$$f'(x) = 2f(x)(1 - f(x)) \quad (15)$$

To evaluate the fault tolerant behavior of a MLP trained with standard BP we will continue by an example.

**Example 1:** A 3-4-1 neural network as in Fig. 3 is trained to approximate a non-linear function defined in equation (16).

$$o = \frac{1}{x + y + z} \quad (16)$$

The training set is  $T_L = \{0.1, 0.2, \dots, 1.1\}$ . BP is iterated for 30000 epochs with a learning rate of 0.05. The trained network is then subjected to four stuck-at-0 faults according to each node of hidden layer.



**Fig. 3** The 3-4-1 MLP network used in Example 1.

Table 1 shows the sensitivity measures for 10000 input vectors selected randomly from the test set  $T_1 = \{0.10, 0.11, \dots, 1.11\}$ .

**Table 1** Weight sensitivity for MLP trained by standard BP algorithm

Weight in 1 <sup>st</sup> layer	sensitivity	Weight in 2 <sup>nd</sup> layer	sensitivity
$w_{11}$	0.0758	$v_1$	1.8808
$w_{12}$	0.0050	$v_2$	0.0916
$w_{13}$	0.0006	$v_3$	0.0581
$w_{14}$	0.0012	$v_4$	0.5503

In this example  $v_1 - v_4$  are the weights in output layer and  $w_{11} - w_{14}$  are the weights from input node 1 to all nodes in hidden layer. Clearly the network is not too sensitive to the weights in first layer. However, in the output layer there is a large sensitivity to weight  $v_1$ .

It is worth to look at histogram of IPs corresponding to links in output node, shown in Fig. 4. Clearly  $IP_1$  differs significantly from others. It has the biggest peak value and is placed far from origin.

This example shows that the node with maximum sensitivity,  $v_1$  passes most of the information in the neural network architecture, itself.

In other words, if the information distribution becomes uniform, all nodes will have an equal sensitivity.

#### 4 Output error model

Suppose that inputs of a MLP are random variables with a uniform or Gaussian distributed function. Three

theorems are presented to model the effect of stuck at 0 faults in a MLP.

**Theorem 1:** If the inputs of a linear neuron have uniform or Gaussian distributions, then its output will have a Gaussian distribution.

**Proof:** It is a direct application of central limit theorem [33]. ♣

**Theorem 2:** If the inputs of a non-linear neuron with bipolar sigmoid activation function have a uniform or Gaussian distribution, then the distribution of its output is a Gaussian with half mean and variance values of the weighted checksum defined by:

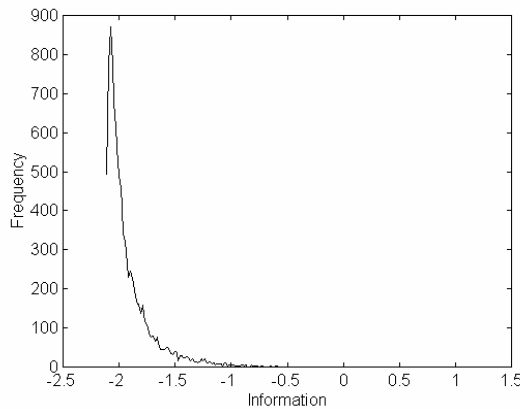
$$S = \sum_{i=1}^n w_i x_k \quad (17)$$

**Proof:** According to theorem 1,  $S$  has a Gaussian distribution with mean  $\mu_s$  and variance  $\sigma_s$ .

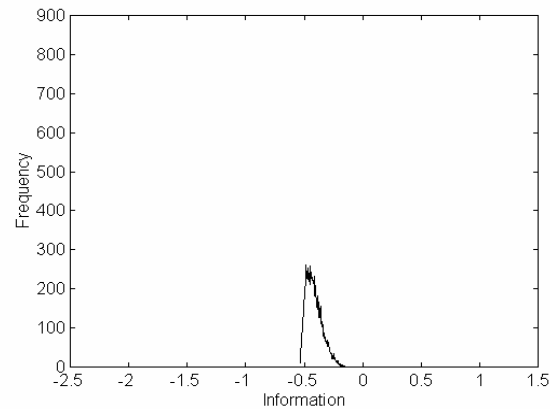
$$P_s(S) = \frac{1}{\sqrt{2n\delta_s}} e^{-\frac{(S-\mu_s)^2}{\delta_s}} \quad (18)$$

The output  $y$  is defined by a bipolar sigmoid function as:

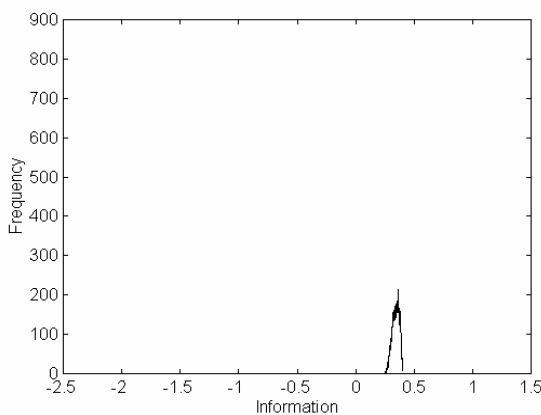
$$y = f(s) = \frac{1 - e^{-S}}{1 + e^{-S}} \quad (19)$$



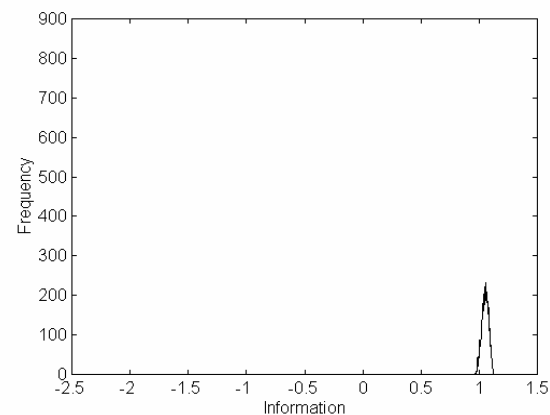
(a)  $IP_1$



(b)  $IP_2$



(c)  $IP_3$



(d)  $IP_4$

**Fig. 4** Distribution function of information packages a)  $IP_1$  b)  $IP_2$  c)  $IP_3$  d)  $IP_4$  in a 3-4-1 MLP trained with conventional BP algorithm

Distribution function of  $y$  can be measured as [33]:

$$P_y(y) = |h'(y)|P_S(h(y)) \quad (20)$$

In which  $h(y)$  is the inverse of equation (19) defined by:

$$s = h(y) = -\ln \frac{1-y}{1+y}, \quad -1 < y < 1 \quad (21)$$

Differentiating equation (21) result:

$$h'(y) = \frac{2}{1-y^2} \quad (22)$$

By substituting (21) and (22) in (20) results:

$$P_y(y) = \left| \frac{2}{1-y^2} \right| \frac{1}{\sqrt{2\pi}\delta_s} e^{-\frac{(\ln(\frac{1+y}{1-y}) - \mu_s)^2}{\delta_s^2}}, \quad -1 < y < +1 \quad (23)$$

With the assumption that  $y$  is usually around origin, the two following approximations are valid:

$$\frac{2}{1-y^2} \approx 2 \quad (24)$$

$$\begin{aligned} \ln \frac{1+y}{1-y} &= \ln(1 + \frac{2y}{1-y}) \\ &\approx \ln(1 + 2y) \\ &\approx 2y \end{aligned} \quad (25)$$

And substituting equations (25) and (24) in (23), we have:

$$P_y(y) = \frac{1}{\sqrt{2\pi} \frac{\sigma_s}{2}} e^{-\frac{(y - \frac{\mu_s}{2})^2}{(\frac{\sigma_s}{2})^2}} \quad (26)$$

which is a Gaussian with  $\mu = \frac{\mu_s}{2}$  and  $\sigma = \frac{\sigma_s}{2}$ . ♣

**Theorem 3:** If inputs to a neural network are random variables with uniform or Gaussian distributions, error introduced by stuck at 0 faults, obey a Gaussian model too.

**Proof:** To simplify the proof, suppose that the hidden neurons are non-linear with bipolar sigmoid activation functions but output nodes are linear. Every output node computes a weighted sum on the hidden layer nodes. Now consider  $oh_k$  as the output of the hidden node  $k$  and  $w_{ki}$  as the connecting weights between hidden neuron  $k$  and output node  $i$ . It is clear that contribution of hidden neuron  $h$  to output is equal to  $w_{ki} * oh_k$ . A stuck at 0 fault in hidden node  $k$ , which forces  $w_{ki} * oh$  to zero, will introduce an absolute error equal to  $w_{ki} * oh_k$ . So the output error is proportional to  $oh_k$ , which has a Gaussian distribution according to theorem 2. Hence the output error will have a Gaussian distribution too. ♣

For a fixed input pattern the error will choose one of the values from the set  $F = \{w_1.oh_1, w_2.oh_2, \dots, w_n.oh_n\}$ . So the expected value and variance of output error are:

$$\mu_f = \frac{1}{N} \sum_{i=1}^n w_i.oh_i \quad (27)$$

$$\delta_f = \frac{1}{N} \sum_{i=1}^n (w_i.oh_i - \mu_f)^2 \quad (28)$$

In equation (27) the term  $\sum w_i.oh_i$  plus the bias value will produce the actual output, which must approximate the target. So  $\mu_f$  depends on target mean and bias value. On the other hand, equation (28) shows the information package variance. We will show that choosing appropriate weights during the learning phase can reduce  $\sigma_f$  and  $\mu_f$ .

## 5 UDBP learning algorithm

Based on the error model introduced in section 4, the UDBP (Uniformly Distributed Back Propagation) algorithm is presented to minimize  $\mu_f$  and  $\sigma_f$  of output error by distributing information packages uniformly in the neural network architecture. A new error function will be defined as:

$$\tilde{E} = \frac{1}{2} \sum_j (o_j - t_j)^2 + v \times \frac{1}{N} \sum_j \sum_i (oh_i \times w_{ij} - \mu_i)^2 \quad (29)$$

$$\mu_i = \frac{1}{N} \sum_n oh_n \times w_{ni} \quad (30)$$

$N$  denotes the number of hidden layer nodes. The second term in (29) is the total variance of information packages in the neural network. Differentiating (29) in respect to  $w_{ij}$  results in:

$$\frac{\partial \tilde{E}}{\partial w_{ij}} = \frac{\partial o_j}{\partial w_{ij}} (o_j - t_j) + \frac{\lambda}{N} oh_i (oh_i w_{ij} - \mu_i) \quad (31)$$

For a linear output the equation is changed to:

$$\frac{\partial \tilde{E}}{\partial w_{ij}} = oh_i [o_j - t_j + \frac{\lambda}{N} (oh_i w_{ij} - \mu_j)] \quad (32)$$

We have introduced a new parameter called  $\lambda$ , which controls the uniformity of information packages. A large value of  $\lambda$  usually tends to a more uniform data distribution in the neural network architecture.

According to these equations the learning is achieved by:

$$w_{ij}(\text{new}) = w_{ij}(\text{old}) - \mu \frac{\partial \tilde{E}}{\partial w_{ij}} \quad (33)$$

In which,  $\mu$  is the learning rate parameter.

Similar equations can be written for a bias learning rule:

$$\frac{\partial \tilde{E}}{\partial b_j} = o_j - t_j + \lambda (b_j - \mu_j) \quad (34)$$

And,

$$b_j(\text{new}) = b_j(\text{old}) - \mu \frac{\partial \tilde{E}}{\partial b_j} \quad (35)$$

The conventional BP algorithm is modified according to equations (34) to (35) for training the output layer weights. The new algorithm, which is called Uniformly Distributed Back Propagation (UDBP), is as the following:

### UDBP algorithm:

- Step 0:** Initialize weights,  $\mu$  and  $\lambda$ .  
**Step 1:** While stopping condition is false do steps 2-9  
**Step 2:** For each input vector do Steps 3-8  
**Step 3:** Each input node receives input signal and broadcast it to hidden layer units.  
**Step 4:** Each hidden node sums its weighted inputs and applies its activation function according to equations (8) and (9).  
**Step 5:** Each output node sums its weighted input signal and produces its output, too.  
**Step 6:**  
**Step 6-1:** For each output node the error information term is computed using equation (31) or (32).  
**Step 6-2:** For each output node the bias gradient term is computed using equation (34).  
**Step 7:** For each hidden node, equations (12) and (13) are computed.  
**Step 8:** For each output and hidden node, weights are updated according to:

$$w_{ij}(\text{new}) = w_{ij}(\text{old}) + \Delta w_{ij} \eta$$

**Step 9:** Test stopping condition.

**Example 2:** To evaluate UDBP algorithm, the 3-4-1 MLP network in Fig. 3 is trained to approximate the non-linear function of equation (16). The training and testing sets and conditions are the same as Example 1 and  $\lambda$  is 0.8 here. Table-2 shows the sensitivity measures for the trained neural network.

**Table 2** Weight sensitivity for 3-4-1 MLP trained by UDBP algorithm

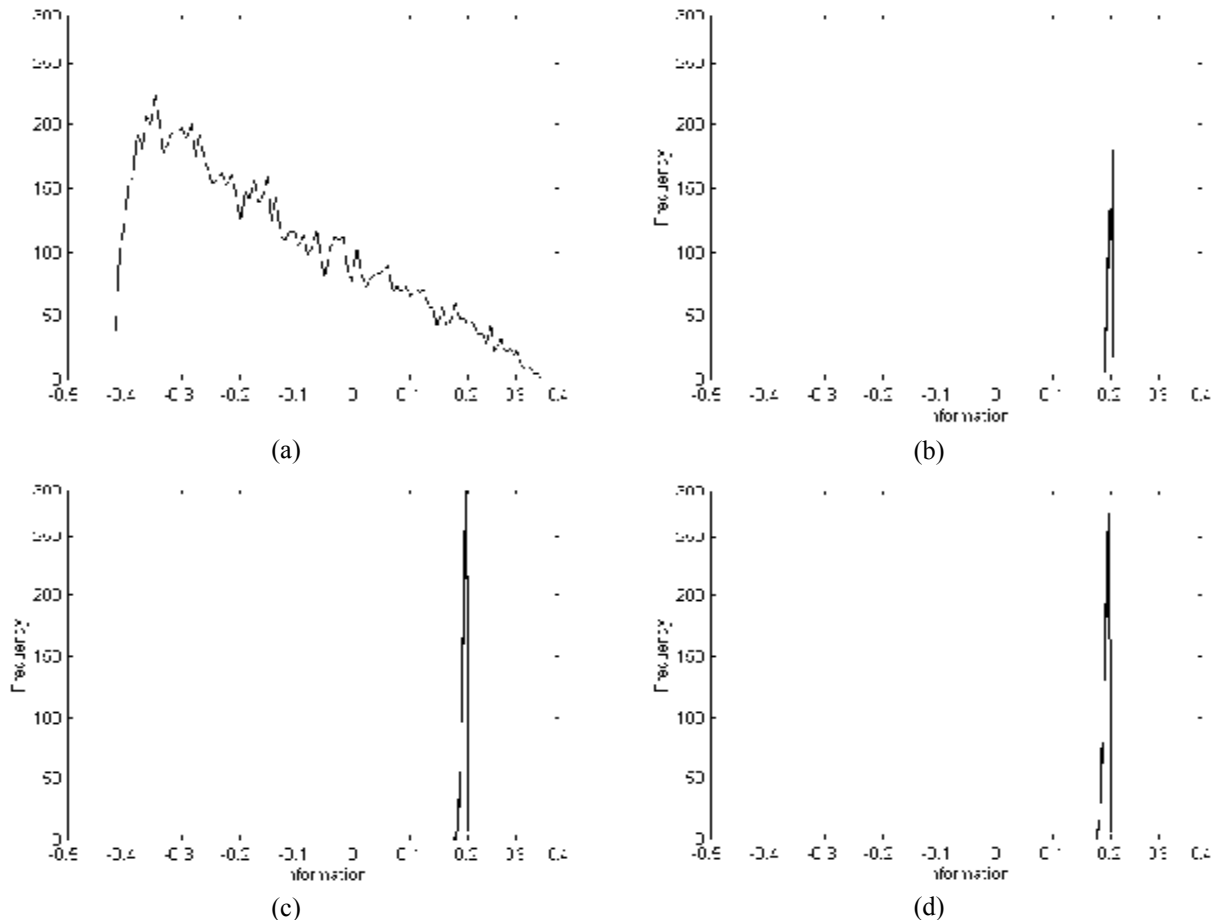
Weight in 1 <sup>st</sup> layer	sensitivity	Weight in 2 <sup>nd</sup> layer	sensitivity
$w_{11}$	0.0343	$v_1$	0.0359
$w_{12}$	0.0054	$v_2$	0.0304
$w_{13}$	0.0053	$v_3$	0.0301
$w_{14}$	0.0051	$v_4$	0.0289

Comparing table 1 and table 2 it seems that the maximum sensitivity of neural network is reduced from 1.8808 to 0.0359. On the other hand it is clear that the sensitivity of all hidden nodes are approximately equal. Although the UDBP is just applied to output layer, the sensitivity of weights in first layer is also improved.

Fig. 5 shows the distribution function of  $IP_1$  to  $IP_4$  for the network trained by UDBP. Comparing with fig. 4 it is clear that all distributions are moved toward origin and their peak values are very close to each other.

### 6 Simulation results

Three other algorithms consisting of WRTA (Weight Restricted Training Algorithm), ADP (Addition/Deletion Procedure) [14] and N-FTBP (N Fault Tolerant Back Propagation) [10] are chosen to be compared with UDBP algorithm. The 3-4-1 MLP network used in examples 1 and 2 is trained again for all algorithms. Table 3 shows the measured sensitivity for all hidden layer nodes after completion of training process for unique initial weights.



**Fig. 5** Distribution function of information packages a)  $IP_1$  b)  $IP_2$  c)  $IP_3$  d)  $IP_4$  In a 3-4-1 MLP network trained with UDBP algorithm

In N-FTBP algorithm one stuck at 0 fault is injected for fifty iterations of BP training algorithm. In WRTA the maximum value of weights for output layer is 1 and for first layer is 5. ADP algorithm performs deletion of the node with least sensitivity and duplication of the one with maximum sensitivity after 100 iteration of BP algorithm. Learning rate is 0.05 for all algorithms. Table-3 shows that UDBP has the most uniform sensitivity among all. The average response of ADP is slightly better. N\_FTBP and WRTA show a moderate improvement compared to standard BP. Standard BP has the worst fault tolerance itself. In another application, a low pass FIR filter [34] with transfer function of:

$$H(z) = -0.0087 + 0.252z^{-2} + 0.5138z^{-3} + 0.252z^{-4} - 0.0087z^{-5} \quad (36)$$

is also approximated with a 6-4-1 MLP. The maximum iteration is 50000 for all mentioned algorithms. Table-4 shows the best computed sensitivity in the output layer obtained for different algorithms.

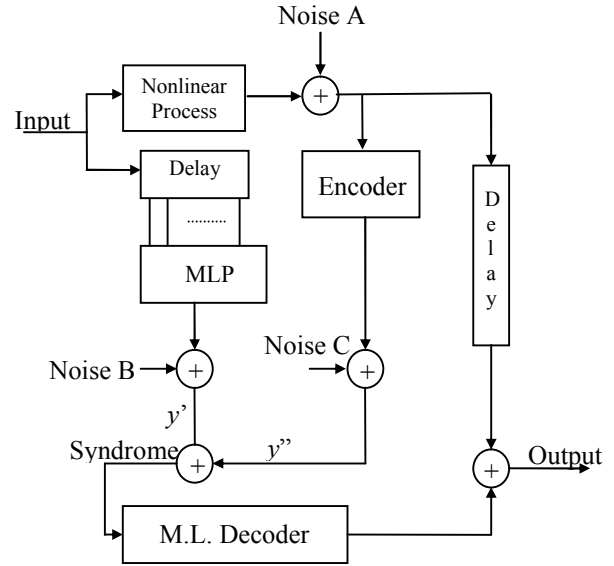
The 6-4-1 MLP network trained to approximate the FIR filter is a dynamic neural network indeed. Data stream moves from one input node to next one in each time step. This will help the network to produce a more uniform data distribution compared to static neural networks. Table-4 shows that the average sensitivity for a dynamic neural network is less than a static neural network. UDBP has the least sensitivity however the ADP and N\_FTBP have moderate responses. WRTA response is near to UDBP.

### 7 Fault correction using UDBP

Convolutional codes are usually used over the transmission channels, through which both information and parity bits are sent. To achieve fault detection and correction properties of this code in a nonlinear process with the minimum overhead computations, we propose the block diagram in fig 5.

The main architecture is similar to a normal ABFT scheme except of the neural network and delay line in the information pass which replace the parity generator part of a systematic convolutional encoder. The upper way is the normal Process data flow which passes through the nonlinear process block and then fed to the convolutional encoder to make parity sequence  $y''$ . On the other hand MLP network is trained by UDBP algorithm to have a direct parity,  $y'$ , equal to  $y''$  in the absence of any noise and faults in system. So the

syndrome sequence is a stream of zero or near zero values in normal operation.



**Fig. 5** Block diagram of the neural based ABFT

We have modeled faults in a nonlinear process block with module noise A while the encoder and neural network noises are modeled with modules B and C. Since these two last noises contribute in syndrome additively we can delete one of them without any degradation.

#### 7-1 Example and Simulations

A (3, 2, 2) systematic convolutional code with generators of:

$$g_1^{(3)} = 1 + D \quad (37)$$

$$g_2^{(3)} = 1 + D^2 \quad (38)$$

is used to evaluate the error detect ability and correct ability of our proposed method jointed with a MLP with 4 inputs 21 nodes in hidden layer and one output. A block processing SINE function with two inputs is chosen as the nonlinear process to be protected. The generator matrix of the code for its first constraint length is as:

**Table 3** Sensitivity measures for a 3-4-1 MLP network trained by different algorithms

Algorithm	Sensitivity of nodes in hidden layer				
	$v_1$	$v_2$	$v_3$	$v_4$	Average
BP	1.8808	0.0916	0.0481	0.5503	0.6452
UDBP	0.0359	0.0304	0.0301	0.0289	0.0313
WRTA	0.2100	0.0867	0.0722	0.0734	0.1150
N-FTBP	0.0111	0.0014	0.0002	0.4205	0.1083
ADP	0.0367	0.0193	0.0375	0.0276	0.0302

**Table 4** Sensitivity measures for a 6-4-1 MLP trained by different algorithms

Algorithm	Sensitivity of nodes in hidden layer				
	$v_1$	$v_2$	$v_3$	$v_4$	Average
BP	0.0003	0.0048	0.0351	0.0014	0.0104
UDBP	0.0032	0.0051	0.0052	0.0046	0.0045
WRTA	0.0060	0.0059	0.0059	0.0056	0.0059
N-FTBP	0.0186	0.0129	0.0002	0.0003	0.0080
ADDROP	0.0010	0.0191	0.0125	0.0010	0.0083

$$G = \begin{bmatrix} 1 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 0 \\ & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 1 \\ & & & 1 & 0 & 1 & 0 & 0 & 1 \\ & & & & 1 & 1 & 0 & 0 & 0 \\ & & & & & & 1 & 0 & 1 \\ & & & & & & & 1 & 1 \end{bmatrix} \quad (39)$$

And according to equation 2-3 the parity check matrix for the first constraint length is:

$$H = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 0 & 0 & 1 & 1 & 1 \\ 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 & 1 \end{bmatrix} \quad (40)$$

We have two parity triangles for each generator as:

$$\begin{bmatrix} s_0 \\ s_1 \\ s_2 \end{bmatrix} = \begin{bmatrix} 1 \\ 1 & 1 \\ 0 & 1 & 1 \end{bmatrix} \begin{bmatrix} e_0^{(1)} \\ e_1^{(1)} \\ e_2^{(1)} \end{bmatrix} + \begin{bmatrix} 1 \\ 0 & 1 \\ 1 & 0 & 1 \end{bmatrix} \begin{bmatrix} e_0^{(2)} \\ e_1^{(2)} \\ e_2^{(2)} \end{bmatrix} \quad (41)$$

It is clear that the code is self orthogonal and we can form a set of two orthogonal check sums on the information error bit, hence,  $t_{ML}=1$  and the code can correct single faults in each constraint length of code which is three here. Fig 6a shows the main process which is a two input SINE block. The outputs  $y_1$  and  $y_2$  are subjected to single s-at-0 faults modeled with noise modules A1 and A2. The faulty outputs now shown with  $b_1$  and  $b_2$  are then fed to convolutional encoder as in fig 6b. The generated code stream,  $y''$ , is compared with MLP output  $y'$  as shown in fig 6c. The majority logic now produces two error signals which are fed back to delayed output streams in fig 6a and correct outputs.  $y_1$  and  $y_2$  are corrected outputs which their validity is governed by majority logic decoding rule.

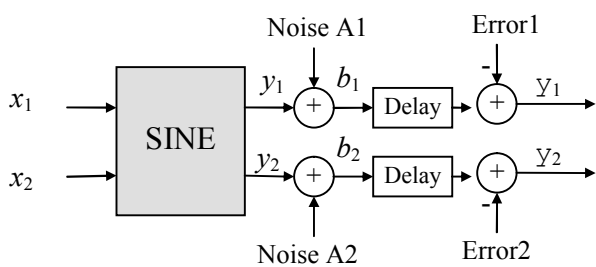


Fig. 6c SINE block input -output

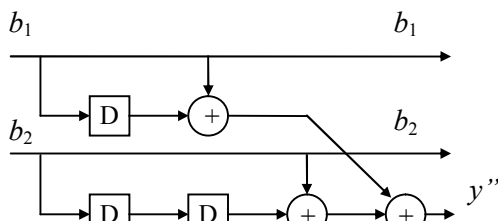


Fig. 6a Systematic (3, 2, 2) convolutional encoder

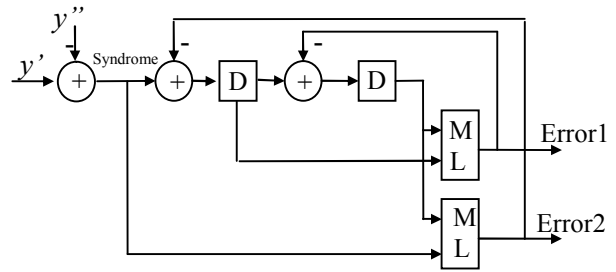


Fig. 6a Complete Majority Logic Decoder for used in this example - ML is the Majority Logic gate

The MLP inputs are selected according to equations (1) and (2). The network is then trained in the absence of any noise so that it's output approximates the SINE block function followed by the (3,2,2) convolution encoder.

Fig. 7 shows the simulation results after 50000 training iterations. In fig-7a the syndrome sequence in the absence of any faults is shown, which is due to neural network limited accuracy. This error value in most times is less than 0.005. However there are also few errors as great as 0.01. Therefore we will select a threshold value equal to 0.05 for error detection purposes.

The whole system is then subjected to s-a-0 faults every 10 steps at SINE block outputs (module noise A1 or A2 in fig 6) and at MLP or Encoder output (module noise C or B in fig 5). Fig-7b shows the syndrome sequence for faults in first output of SINE block,  $y_1$ . It is clear that there are two equal nonzero values after each fault occurrence. In fig-7c the same sequence is shown for faults in the second output of SINE block,  $y_2$ . Again there are two nonzero values for each fault but the recent values are separated by a single space gap. Fig-6d shows on the other hand, the syndrome for faults in encoder and neural net blocks. It is clear that the syndrome contains single nonzero values for injected faults. Therefore we have three distinct sequences for each fault source which is benefit of convolutional coding used. If there is only a single fault in every constraint length (3 in this case) the majority logic decoding can correct the fault.

## 8 Conclusions

In this paper we first showed that standard BP algorithm can not yield to a uniform data distribution over the neural network architecture. A measure of sensitivity defined to evaluate fault tolerance of neural network and then we showed that the sensitivity of a link is closely related to the amount of information passes through it. Based on the assumption of using input variables with uniform or Gaussian distribution functions, we proved that the distribution of output error caused by stuck at 0 faults in a MLP network is approximately a Gaussian too. UDBP algorithm then introduced to minimize mean and variance of the output error. Simulation results show that UDBP has the least sensitivity and the highest fault tolerance among other algorithms such as WRTA, N-FTBP and ADP. UDBP has just one extra parameter compared to standard BP. It requires three extra multiplications and two extra additions in each iteration compared to BP. Then we coupled a MLP neural network trained with UDBP algorithm to a convolutional encoder in an ABFT scheme to demonstrate the feasibility and



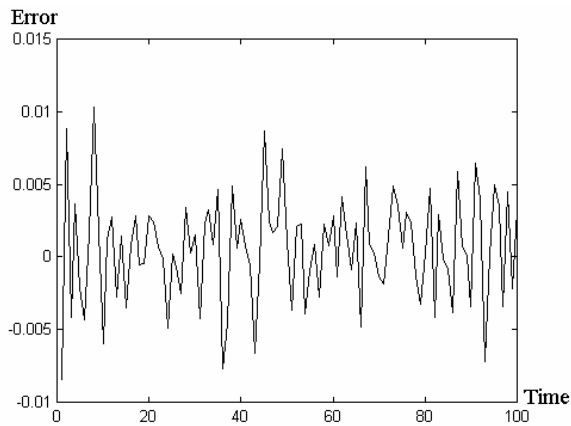


Fig. 7a Syndrome sequence for no fault condition

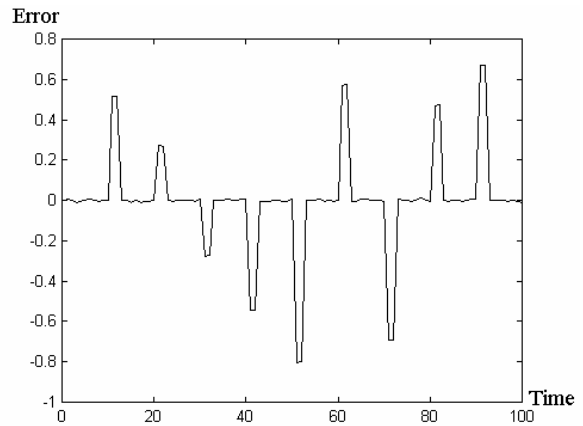


Fig. 7b Syndrome sequence for faults due to Noise source A1

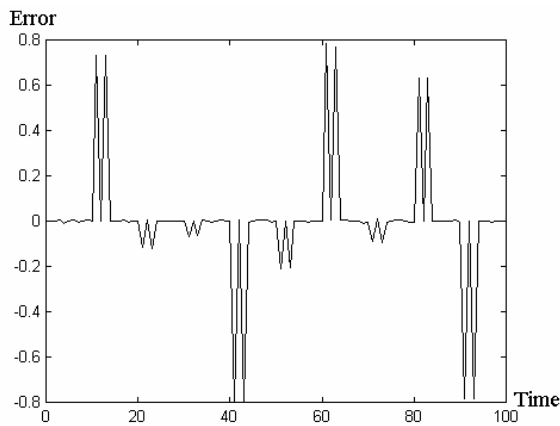


Fig. 7c Syndrome sequence for faults due to Noise source A2

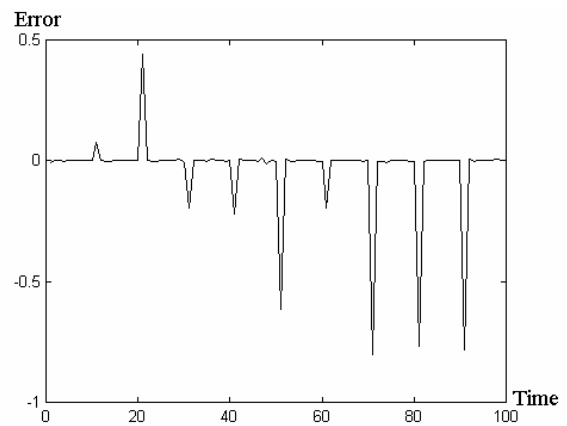


Fig. 7d Syndrome sequence for faults due to Noise sources C or B

expandability obtained for fault detection and correction in nonlinear block processes. The trained neural network can itself tolerate single faults, and the used majority logic gates are very simple. So unlike the other ABFT techniques there is no need to apply extra hardware or software to protect these additional blocks. In addition, neural network learn ability permits to change process block functionality without much consideration. Which can not be obtained through conventional ABFT techniques?

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