

# Identification of Two Main Independent Components of Fibrillating Heart Muscle

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**Abstract:** Fibrillation is a hazardous phenomenon in cardiac muscle and so any new work towards the understanding of this process is important to the development of new methods in diagnosis and therapy. In this work we have used surface and intra cardiac ECGs of patients with chronic atrial fibrillation (AF). By means of the blind source separation (BSS) algorithm, which is a well-known method in signal processing, the AF process has been deconstructed into its independent components and we can show that from the point of view of these components the surface ECGs contain the same information as the intra atria electrogram. Then the important components have been related to the ionic currents of the cell. We show that one of these independent components can be influenced by the sodium-calcium exchange current, (iNaCa) and hence by controlling iNaCa we may be able to control the fibrillation process. This new idea can bring about new strategies in drug therapy.

**Keywords:** Fibrillation, Independent Component, Ionic Current.

## 1 Introduction

Fibrillation is a dangerous episode in cardiac muscle. Ventricular fibrillation, (VF), is the most common arrhythmia which directly leads to sudden cardiac death. Atrial fibrillation, (AF), while not usually lethal, also causes significant fatality. So any new work towards the understanding of this process may lead to the development of new methods in prevention, diagnosis and therapy and save many people's lives. Most studies in this context have been done by using invasive data from human or animal heart muscle. Invasive observations are burdensome and expensive and the required equipment is not available to every researcher especially biomedical engineers, therefore noninvasive methods are preferred. Firstly in this study we carry out our method with the use of the surface ECG of patients with AF, and then redo the study with intracardiac electro gram of the same patients. Since the results are the same, we conclude that our noninvasive method can be used instead of the invasive method and this is an advantage of our study.

The nature of fibrillation is a matter of controversy [1], some authors believe that it is a random process and

others believe that it is deterministic but chaotic. Our method has no dependence on these beliefs but adds a new point of view to this phenomenon.

The surface ECG is an observation on a dynamic system; heart muscle. A sufficiently long time observation on a dynamic system contains enough information for its characterization [2]. A dynamic system is characterized by its state variables. State variables are independent variables, which combine to create the behavior of the system.

The mechanical activity of heart results from the action potential and action potential occurs as a result of ionic currents so it is evident that state variables of heart i.e. independent dynamic variables can be connected to ionic currents. Arrhythmia in heart can be interpreted as changes in heart dynamics and so heart diseases could be called dynamic diseases [4]. The dynamics of a system is influenced by its state variables and so identification of state variables can lead to identification of normal and abnormal behavior and better controlling of arrhythmia. Figure 1 illustrates the action potential and two main currents in the rabbit atrial cell [3]. In our recent paper we have shown that we can extract almost the all information about cell's electrical activity (dynamics) from its action potential (AP), on the other hand iCa and iNaCa are the two main state variables of the cell's dynamics [11].

In this study we first investigate the independent components of the atrial activity of normal subjects. The results show that the calcium current (iCa) may be the main independent component in normal activity. We

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next consider the surface ECG of patients with AF; these results show that the sodium-calcium exchange current ( $i_{NaCa}$ ) may be the main independent component in the AF case. As a test for the credibility of these conclusions from the surface ECG and in order to justifying our noninvasive method we repeat our study with intracardiac electro gram of the same patients. We get the same results; hence our noninvasive method works as well as an invasive method and is a more favorable choice.

## 2 Methods

We have used the ECG records of normal subjects from lead II, the specifications of these records are in [5]. Nearly two seconds records can reflect AF and VF dynamics [1, 9] so using two seconds single lead ECG data, we make Toeplitz observation matrix as described in [6] (see appendix A). A typical eigenvalues (EVs) spectrum of several normal subjects of either sex and a variety of ages is illustrated in Fig. 2. It is evident from Fig. 2 that EVs are separated into three distinct levels; of course the biggest EV is related to the most powerful component i.e. ventricular activity. The second component reflects atrial activity and the third includes possible noises and other weak components [10].

In Fig. 3, a two second ECG record of a normal case is illustrated. We have used the blind source separation (BSS) method in [7] for independent source computations (see appendix B). From justified literatures we know that the action of BSS on an observation gives its independent components which are as independent as possible [12] so we expect to see ionic currents morphology in independent components. In Fig. 4 to Fig. 6, the first, second and third independent components (sources) have been depicted respectively and from the morphology of the second component it is reasonable to relate it to the ionic current  $iCa$ .

Now we investigate lead II ECGs of patients with AF. The specifications for them are in [8]. We make an observation matrix as above. The typical EVs spectrum for three patients is depicted in Fig. 7. We see that EVs are separated into three distinct levels but the distribution of the third level is more than Fig. 2, i.e. it seems that the third level itself is composed of two close levels. Figure 8 illustrates a lead II surface ECG of a patient with AF. Figure 9 shows the first component, which is indicative of ventricular activity. The second component is depicted in Fig. 10 which clearly has triphasic morphology and it is completely different from Fig. 5. Figure 11 shows the third component. It does not have clear morphology but it seems to be biphasic and certainly different from Fig. 6. The triphasic morphology of Fig. 10 together with the fact that the ECG observation is made from a dynamical system and it originates from the action potential and the action potential originates from ionic currents, leads to this conclusion that: in AF  $iNaCa$  which has a triphasic

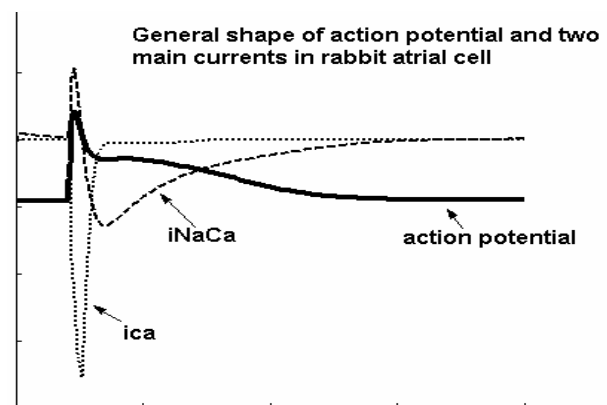
morphology (dynamics) is the main state variable but in normal ECG  $iCa$  is the main component.

Now for confirmation of the above results, which were based on noninvasive data (surface ECGs) and creditability test; we repeat our study by using intracardiac data from the above patients which have been recorded from the interior of their right atrium [8]. We make an observation matrix as mentioned beforehand and obtain EVs spectrum. A typical EVs spectrum is illustrated in Fig. 12. It can be seen that in this case, unlike Fig. 7, the separation of the last levels i.e. levels two and three is more obvious.

Figure 13 shows the recorded electrogram from the interior wall of the right atrium of a patient with AF and Fig. 14 illustrates its first independent component. It is clear that the first independent component has triphasic morphology (here we use electrogram so we do not have ventricular activity). Figure 15 shows the second component, which has a biphasic morphology. Figure 16 shows the third component which represents possible noises and other weak components. Considering the above results we conclude again: In AF the sodium – calcium exchange current ( $iNaCa$ ) may be the most powerful independent variable i.e. when atrial muscle is affected by fibrillation, its dynamics are influenced more by  $iNaCa$ . This finding is in agreement with previous findings about fibrillation. The previous studies apart from randomness or chaotic nature of fibrillation, show that when a muscle encounters fibrillation, its dynamics became more complex. Reasoning as above we can conclude that in fibrillation  $iNaCa$ , which has more complex dynamics, affects the dynamics of the muscle.

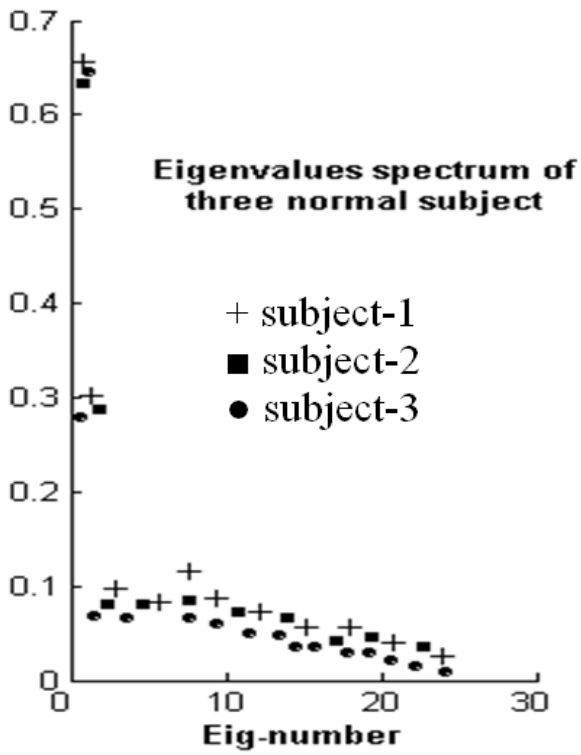
We have used about one hundred of two seconds records of [5] and [8] for validity testing of our results that the results are same in all cases.

In our recent novel research [13], we discovered that AP can be explained as a combination of three classes of state variables which  $iNaCa$  and  $iCa$  are the members of the first class, so we expect to see  $iNaCa$  or  $iCa$  as the main component of any observations (like ECG) which is originated from AP.

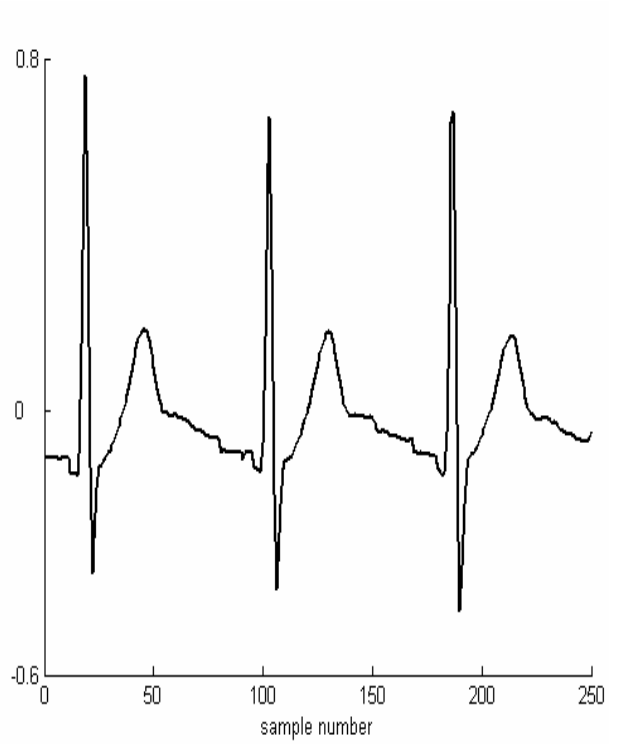


**Fig. 1** action potential and two main ionic currents in rabbit atrial cell [3].

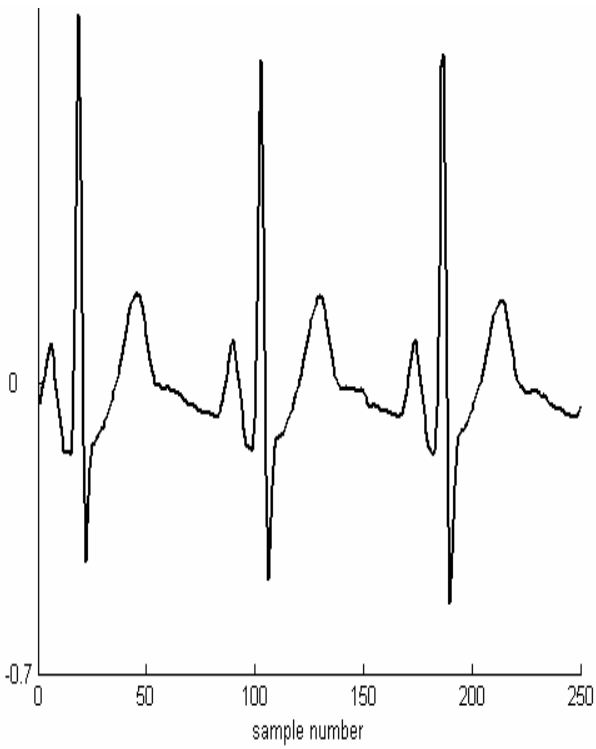
$iCa$ ,  $iNaCa$  have bi- and tri- phasic dynamics respectively.



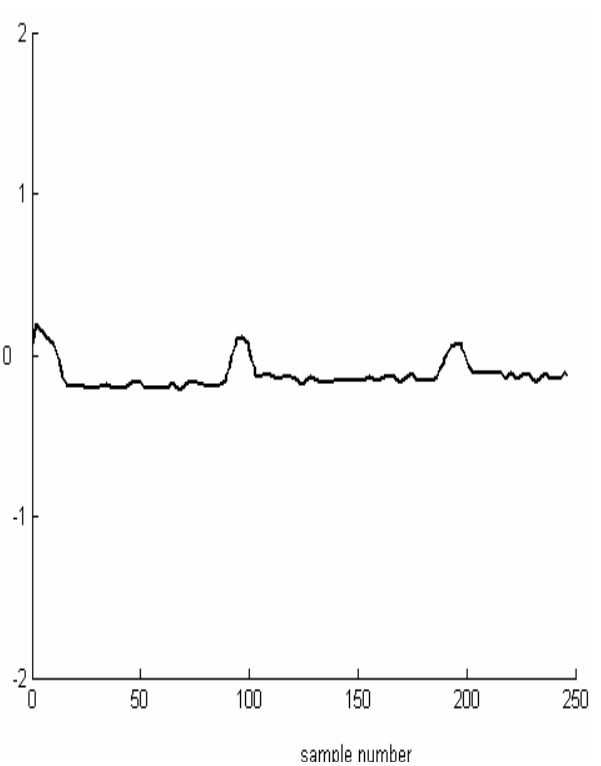
**Fig. 2** Eigenvalues spectrum of three normal subjects. Three distinct levels are observable.



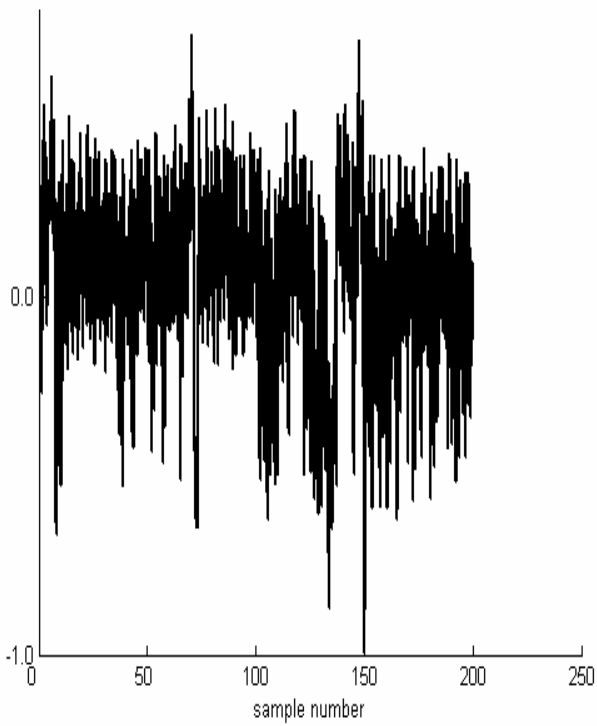
**Fig. 4** first component of normal ECG.



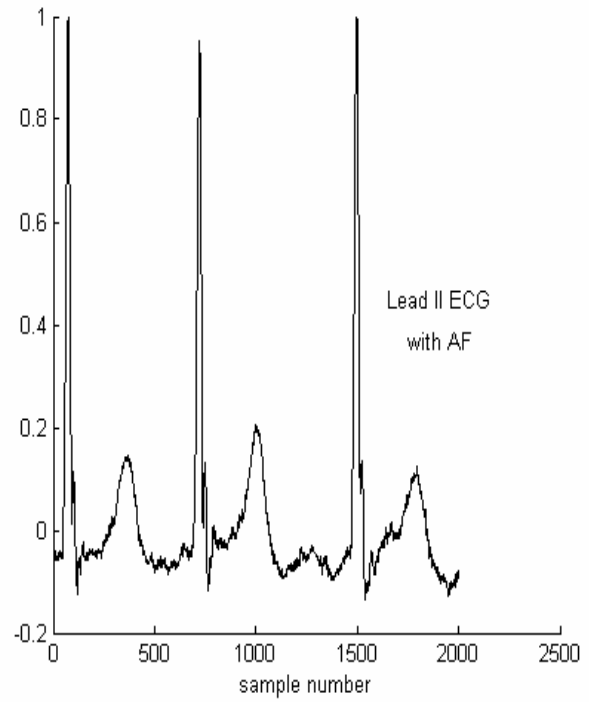
**Fig. 3** A normal ECG from lead II.



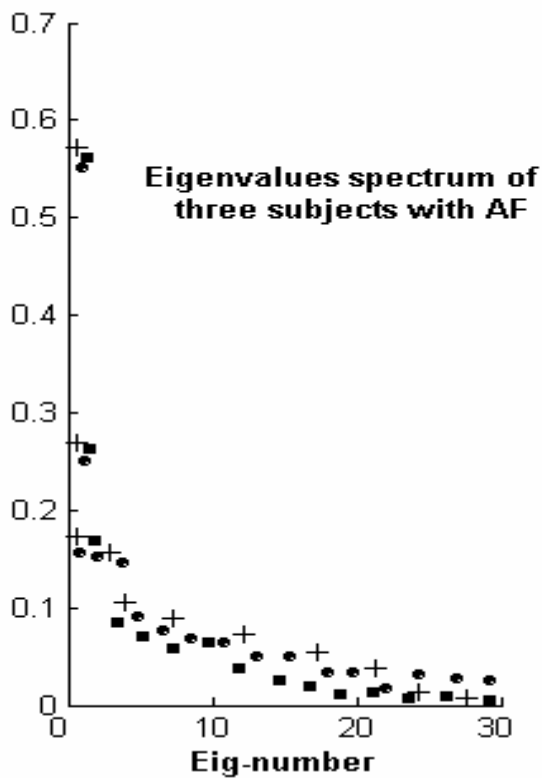
**Fig. 5** second component of normal ECG.



**Fig. 6** third component of normal ECG.



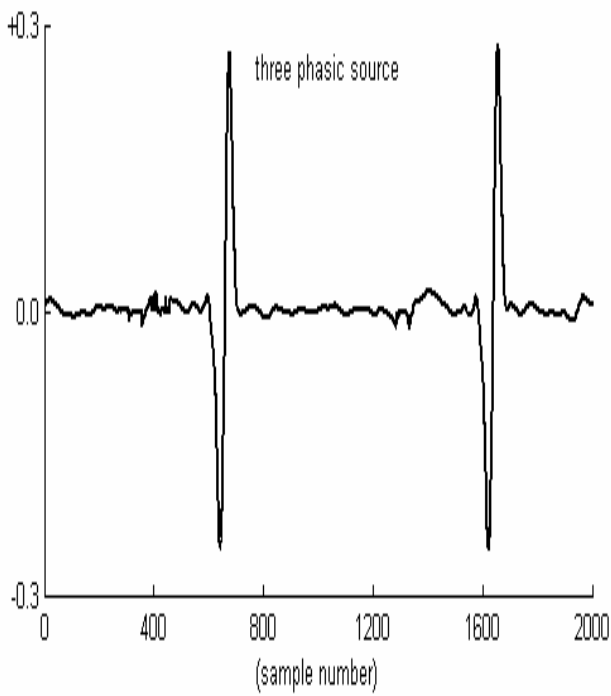
**Fig. 8** Lead II ECG of a patient with AF.



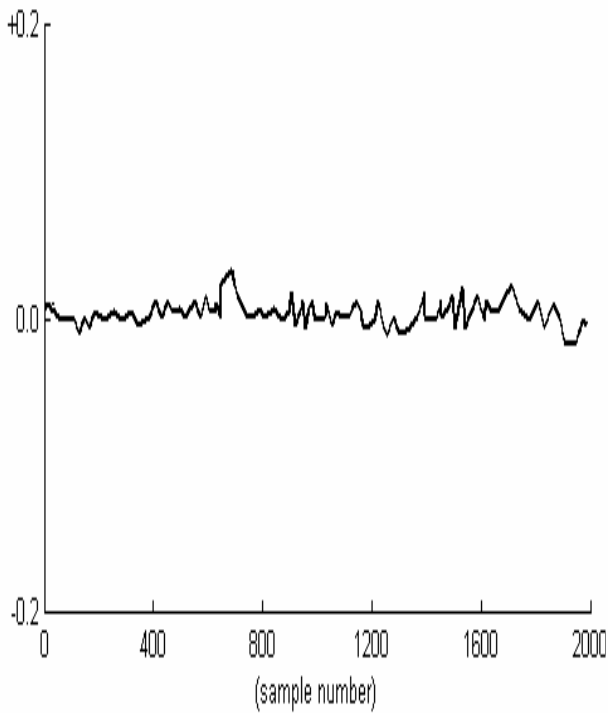
**Fig. 7** Eigenvalue spectrum of patients with AF. Dispersion of values in the last level is clearer than Fig. 2.



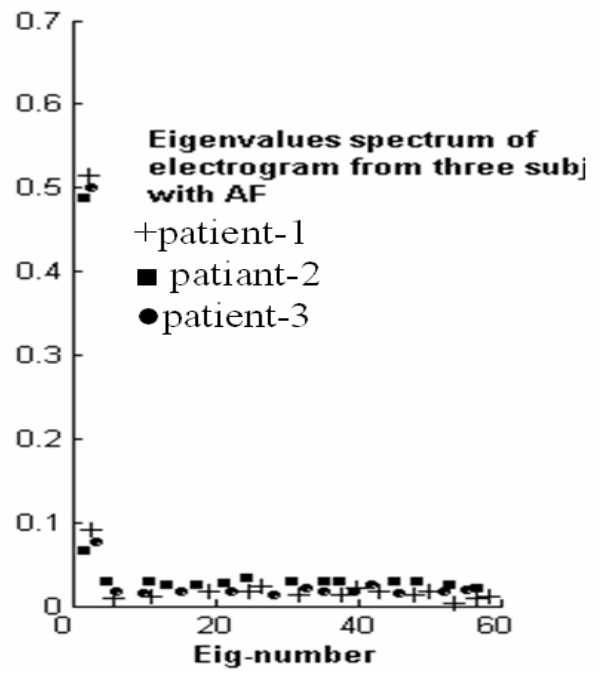
**Fig. 9** General morphology of first component of the Fig. 8 signal, which shows ventricular activity.



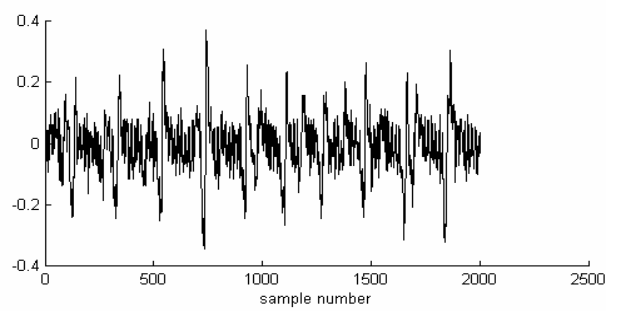
**Fig. 10** General morphology of the second component of Fig. 8 signal. Tri-phasic morphology is clear.



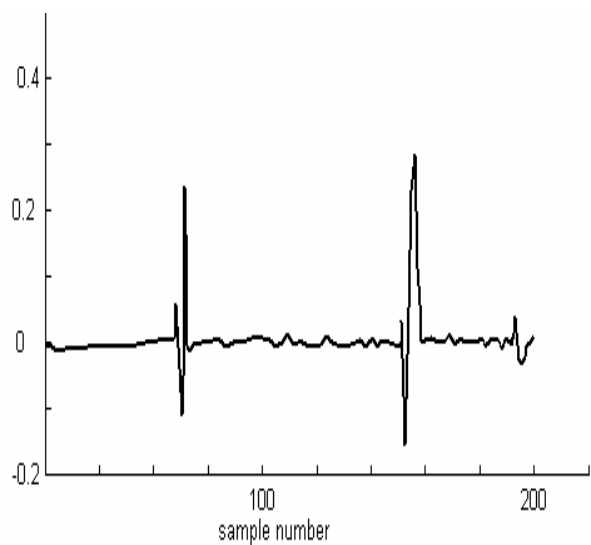
**Fig. 11** General morphology of third component of signal Fig. 8. It seems bi-phasic.



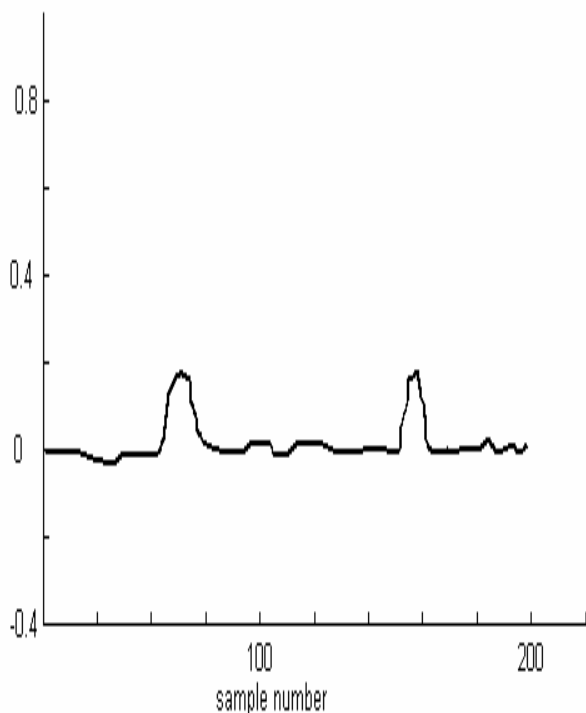
**Fig. 12** Eigenvalues spectrum of electrograms of patients with AF. Last levels are more separated than Fig. 7.



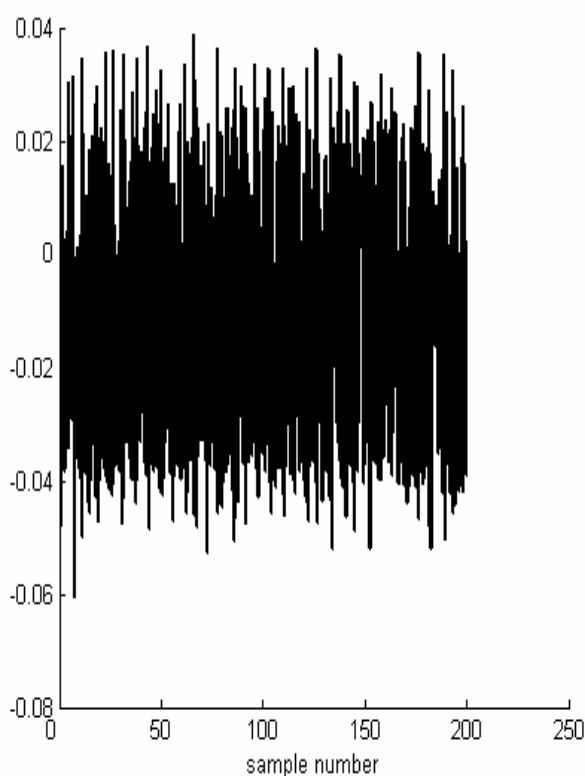
**Fig. 13** Recorded electrogram from right atrium of a patient with AF.



**Fig. 14** First component of the Fig. 13 signal. Tri-phasic morphology is clear.



**Fig. 15** Second component of the Fig. 13 signal. Bi-phasic morphology is clear.



**Fig. 16** Third component of the Fig. 13 signal. This component has no clear morphology.

### 3 Conclusions

In this study we showed that for blind source separation purposes we can use surface ECG instead of electrogram. So we have proposed a noninvasive method. In this study we showed that in normal subjects  $iCa$  could be the most powerful state variable of the atrial activity. We also showed that in patients with AF (and maybe VF)  $iNaCa$  is the most powerful independent component. According to these results it seems that we may control AF (or VF) better by means of  $iNaCa$  and this may lead to new drug therapies. These findings are in agreement with our recent researches [11, 13].

### References

- [1] D. T. Kaplan, R. J. Cohen, "Is fibrillation chaos?", *Circu. Res.*, Vol. 67, No4, oct. 1990.
- [2] J.Stark,"Delay embeddings for forced systems", *J.Nonlinear Sci*, Vol.9,1999.
- [3] Earm, Y. E & Noble D. "A Model of the Single Atrial Cell: Relation Between Calcium Current and Calcium Release", *Proc. R. Soc.* 240: 83-96, 1990.
- [4] J. Belair, L. Glass, U. Heiden, J. Milton, "Dynamical disease: identification, temporal aspects and treatment strategies of human illness", *Chaos*, vol.5, 1995.
- [5] physionet, multi-parameter database.
- [6] R.J. Semnani, BF Womack, KR Diller, "Applications of rank - reduction to ECG analysis", *Comp in cardio*, Vol 25, 1998.
- [7] L. Tong, V. C. Soon, Y. F. Huang, R. Liu, "AMUSE: A new blind identification algorithm", *IEEE ISCAS Pro.* 1990.
- [8] Physiobank, Intracardiac Atrial Fibrillation Database.
- [9] Garfinkel, P.S Chen, D.O.Walter, "Quasi periodicity and chaos in cardiac fibrillation", *Journal of clinical Inv*, Vol 99, No2, 305-314, Jan-1997.
- [10] R.J. Semnani and B.F. Womack. "Rank-Adaptive Signal Processing (RASP). A subspace approach to biological signal processing, Part II Applications", 0-7803-6514-3/00/\$10.00©2000 IEEE.
- [11] S. H. Sabzpoushan, A. Ayatollahi, D. Noble, P.J. Noble, "A survey on linear relations between main electrical components during action potential in ventricular cell", *Applied Mathematics and Computation*, Elsevier Inc. to be published in 2007.
- [12] A. Hyvarinen, J. Karhunen, E. Oja, *Independent Component Analysis*, Wiley, New York, 2001.
- [13] S. H. Sabzpoushan, P. J. Noble, "Simplifying the action potential model in the ventricular cell as a linear combination of three classes of state variables", *Biosystems*, Elsevier Inc. to be published in 2007.

## Appendix (A)

Blind source separation (BSS) algorithms relies on spatial diversity i.e. multi-lead (channels) observations, but if we have had sufficiently long time records, by building toeplitz observation matrix (we may use any linearly structured matrix such as Hankel) we can use temporal diversity instead of spatial diversity this reduces the need of multi- leads records .

Consider vector  $X$  which contains  $m$  times single lead ECG observation i.e.

$X=[x(1), x(2), \dots, x(m)]$  we make toeplitz observation matrix as:

$$X = \begin{bmatrix} x(n) & x(n-1) & \dots & x(1) \\ x(n+1) & x(n) & \dots & x(2) \\ \vdots & \vdots & \vdots & \vdots \\ x(m) & x(m-1) & \dots & x(m-n+1) \end{bmatrix}$$

The above observation matrix is equivalent to observations from  $(n-m+1)$  channels each  $n$  points long. For making a toeplitz matrix, we must decide on the number of rows, which is an estimate of the number of independent sources responsible for generating the observation. We make covariance matrix  $R_x = E(XX^t)$  and compute its singular values, a look at these values leads us to the number of rows.

## Appendix (B)

Blind source separation (BSS) is an important subject in systems identification and signal processing. It consists of recovering unobserved signals or "sources" from several observed mixtures. Typically, the observations are obtained at the output of a set of sensors, where each sensor receives a different combination of the source signals. The adjective "blind" stresses the fact that 1) the source signals are not observed and 2) no information is available about the mixture. The simplest BSS model assumes the existence of  $n$  independent signals  $s_1(t), \dots, s_n(t)$  and the observation of as many mixtures  $x_1(t), \dots, x_n(t)$  so that

$$x_i(t) = \sum_{j=1}^n a_{ij} s_j(t), \quad i=1, \dots, n$$

This is represented compactly by the mixing equation  $X(t)=A.S(t)$ , where  $S(t)=[s_1(t), \dots, s_n(t)]^t$  is an  $n \times 1$

column vector collecting the source signals, vector  $X(t)$  similarly collects the  $n$  observed signals, and the square  $n \times n$  "mixing matrix"  $A$  contains the mixture coefficients. The BSS algorithm can be formulated as the computation of an  $n \times n$  separating matrix  $B$  whose output  $Y(t)=BX(t)$  is an estimate of the vector  $S(t)$ .



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**P. J. Noble** photograph and biography not available at the time of publication.

**F. Towhidkhan** photograph and biography not available at the time of publication.