Stator Turn-to-Turn Fault Detection of Induction Motor by Non-Invasive Method Using Generalized Regression Neural Network

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Abstract: Condition monitoring and protection methods based on the analysis of the machine's current are widely used according to non-invasive characteristics of current transformers. It should be noted that, these sensors are installed by default in the machine control center. On the other hand, condition monitoring based on mathematical methods has been proposed in literature. However, they are model based and are too complex. Artificial neural network (ANN) methods are robust and less model dependent for fault diagnosis when the fault signature can be directly achieved using the sampling data. In this procedure, the state of internal process will be ignored. Therefore, generalized regression neural network (GRNN) based method is presented in this paper that uses negative sequence currents (calculated from the machine's currents) as inputs to detect and locate an inter-turn fault in the stator windings of the induction motor. Turn-to-turn fault by changing the contact resistance and various numbers of shorted turns for realizing the fault severity has been modeled by Matlab/Simulink. The simulation and experimental results show that the proposed method is effective for the diagnosis of stator inter-turn fault in induction motor under the supply voltage unbalances.

Keywords: Diagnosis, Induction machine, turn-to-turn fault, GRNN, non-invasive method, negative sequence current.

1. Introduction

Induction motors are widely used in a variety of applications as a means of converting electric power to mechanical work and range in size from a few watts to 10000 hp. These motors, indeed, are the workhorse of industrial plants [1]. Their failure and unexpected downtime can cause severe damage to the machine, interruption of production, and pursuing economic loss. Therefore, a condition monitoring system is essential for modern industrial plants and manufacturing systems, which have to work continuously for extended hours [2]. Electrical faults of the induction motor can be classified into the rotor and stator faults and the most common electrical failure in this motor are stator-related faults, which are about 30%-40% [3], [4]. When inter-turn fault happens, the faulted turn will act as the secondary winding of an autotransformer and a very large circulating current will flow in the shorted turns. Therefore, it is very important to have a careful analysis of the internal faults in induction motors to increase their useful life and reliability.

Consequently, during the last two decades, substantial investigations have been performed based on many fault indicators for the development of various methods in the area of fault diagnosis of electrical machines. Reference [4] classified the most important of these indicators as electromechanical, like magnetic leakage and linkage fluxes, currents, voltages, partial discharges, surges and mechanical, like acoustic, speed fluctuations and vibrations. It is worth mentioning that in fault diagnosis systems, the sensing and analysis of fault indicator signals that include specific information is very important. When the most suitable monitoring method is selected, a variety of factors need to be considered. In the following, the most significant of these factors are presented [4], [5]:

The sensor should be simple and non-invasive. Furthermore, the sensor, measurement and fault diagnosis systems must be reliable and consistent. It should be noted, the severity of the fault and remaining run-life of the machine need to be quantified. Another point worth highlighting is, it is very hard and, in most situations, impractical to satisfy all mentioned criteria, due to the complexity of the failure mechanisms and the nature of the fault. On the other hand, since the current transformers are usually installed by default in the machine control cen-
ter for different purposes, the monitoring schemes that depend on the study of these inputs (global external variables) are mostly being notified [4].

In addition, this popularity is since the current sensors are entirely non-invasive. It has been proven that the condition monitoring of electrical machines based on current signature analysis method is an efficient technique for fault detection in industrial plants [6], [7]. This technique has been used successfully for the detection of broken rotor bars [8]–[10], eccentricity [11], bearing faults [12], and inter-turn short circuit faults [13]. It should be noted, a variety of methods are proposed to analyze internal faults based only on the global external variables such as the stator current signature analysis [14]–[16]. Internal fault diagnosis by negative sequence current or impedance is usual methods used due to the significant increase of these components under internal fault [17]. In fact, turn-to-turn faults in stator winding of induction motor can be detected by monitoring of the negative sequence current. More details about this indicator have been explained section 2.

In [18], the monitoring of the third harmonic of the motor supply current was also found to be an effective technique for the detection of the presence of stator faults. However, some motors usually have appreciable levels of inherent asymmetries and it may be possible that the residual asymmetries of the motor may lead to the appearance of the third harmonic component in the supply currents, even when no faults are present in the motor. Therefore, this technique is only recommended when a high degree of inherent asymmetry of the motor is not expected [4]. Furthermore, reference [17] proposed the positive and negative sequence third harmonics (±3f) of line current as a criterion for stator inter-turn fault detection.

On the other hand, Artificial Intelligence (AI) methods for fault diagnosis and remaining useful life prediction of electrical machines have received considerable attention in recent years [19]. Different kinds of fault criteria have been used as ANN inputs in many investigations based on these techniques. The use of three currents [20], three voltages [21], three-phase shifts between the current and the voltage [22], and the magnetic flux linkages [23], [24] were reported.

This popularity is due to their generalization ability during fault detection that means ANNs are able to do satisfactorily even for unobserved fault. In addition, the second is their capability to be trained from the patterns of the relationships between the fault signatures and the related operating situations of the system. It is worth mentioning that in this procedure, the state of internal process is ignored. Consequently, the ANN method is robust and is an approach less model dependent for fault diagnosis when the fault signature can be directly achieved using the sampling data. In the other words, AI methods are of great useful methods in engineering to solve different difficult problems such as fault detection. These techniques significantly improve the accuracy of fault detection. However, the main issues raised by critics about the AI methods are the need of these methods to a large training time for learning the several possible combinations of the operating scenarios of the system. Therefore, in order to overcome the issues associated with the AI methods, a new method based on the using of the generalized regression neural network (GRNN) has been proposed in this paper.

It is worth highlighting that the main characteristic of the GRNN compared to other networks is due to GRNN’s on-line one-pass instantaneously learning [25]. The inherently parallel structure and the fast training procedure of the GRNN make it suitable for fault diagnosis problems in real time (especially when implemented on hardware systems). In this paper, a non-invasive fault indicator based on negative sequence current for the diagnosis of turn-to-turn stator winding fault in an induction motor is presented. In fact, negative sequence current will be produced by various factors, including supply unbalance and non-linearity motor effects. Therefore, before making any decision about the machine situation from monitoring of this criterion, negative sequence current arising from other effects must be eliminated. The aim of this paper is to present a reliable method with simple algorithm which eliminates these nuisance effects. These nuisance effects are eliminated by using GRNN in which, the state of internal process will be ignored. The proposed method does not require the mathematical model and this makes its application simple and straightforward.

2. Monitoring of the negative sequence current for turn-to-turn fault detection

As stated earlier, turn-to-turn faults in stator winding of induction motor can be detected by monitoring of the negative sequence current. However, there are two main concerns for this detection. The first one is the three-phase supply voltage unbalance that generates negative sequence current in a healthy motor. The second one is the non-linearity induction motor effects (saturation, rotor static eccentricity) and load variations that also produce negative sequence current [14]. Therefore, it is essential to separate out the negative sequence currents arising from supply voltage imbalance or from turn-to-turn fault in the motor. Reference [14] classified these causes that are capable of producing a negative sequence current. Measured negative sequence current in the motor can be expressed as follows [14]:

\[ I_n = I_{sn} + I_{an} \]  

(1)

where, \( I_{sn} \) is the negative sequence current arising from imbalance in the supply voltage, and \( I_{an} \) is the negative sequence current caused by the turn-to-turn fault in the motor. In the following, a procedure to calculate these
negative sequence currents has been presented. First, voltages and currents of the stator in the abc reference frame are transferred to the qd0 reference frame and $i_{ds}$, $i_{qs}$, $v_{ds}$, $v_{qs}$ can be obtained. Then positive and negative sequence components of phase voltages and currents have been calculated by the power decomposition method (PDT) [14]. The positive and negative sequence components can be written as follows:

$$I_x = I_{xu} + jI_{xv} \quad I_y = I_{yu} + jI_{yv} \quad (2)$$

$$V_x = V_{xu} + jV_{xv} \quad V_y = V_{yu} + jV_{yv} \quad (3)$$

Furthermore, equivalent circuit of induction motor corresponds to a negative sequence component is presented in Fig. 1 (a). In addition, Fig. 1 (b) illustrates in a healthy motor how the negative sequence voltage $V_{sn}$ affects on the negative sequence current $I_{sn}$. From Figs. 1 (a) and (b), (4)-(6) can be derived as:

$$z_x = R_x + \frac{R_x}{2 - s} + j(X_x + X_{sn}) = R_x + jX_x \quad (4)$$

$$V_x = I_x R_x + \beta_x X_x \quad I_x = \frac{V_x \sin(\theta_x)}{X_x} \quad (5)$$

$$I_{nx} = \frac{1}{X_x} \arctan \left( \frac{X_x}{R_x} \right)$$

Finally, the negative sequence current caused by the turn-to-turn fault ($I_{mn}$) can be calculated as follows:

$$I_{mx} = I_x - I_{nx} \quad (7)$$

It should be noted, negative sequence current may arise because of several asymmetries. Consequently, these effects must be eliminated from the negative sequence current before making any decision. In some references [14], mathematical method is used to remove these effects from the measured negative sequence current and various aspects of this subject under different conditions were investigated. A brief explanation of this method is described here.

To remove the effects according to variations in load and voltage, it must find out how $I_{mn}$ changes with load and voltage. This procedure is named characterization of the motor. In the following, $I_{mn}$ states the dependence of $I_{mn}$ on load variation, and $I_{mnv}$ states the dependence of $I_{mn}$ on voltage variation. Furthermore, behavior of $I_{mn}$ and $I_{mnv}$ is approximated by the positive sequence currents $I_{px}$ and $I_{py}$ respectively. $I_{px}$ estimates the active load. In fact, $I_{px}$ is in phase with supply voltage. $I_{py}$ approximates magnetization current. In fact, $I_{py}$ represents the effects correspond to saturation in the motor, and $I_{py}$ is in quadrature with supply voltage. It is worth to note that, these two components ($I_{px}$ and $I_{py}$) represent the negative sequence currents of the motor under healthy conditions created by load and voltage variation, i.e. [14]:

$$I_{mn} = \beta_0 + \beta_1 I_{px} + \beta_2 I_{px}^2 \quad (8)$$

$$I_{mnv} = \lambda_0 + \lambda_1 I_{py} + \lambda_2 I_{py}^2 \quad (9)$$

By using the (8) and (9), $I_{mnv}$ has been defined as:

$$I_{mnv} = I_{mn} + I_{mnv}$$. Factors $\beta_0$, $\beta_1$, $\beta_2$, $\lambda_0$, $\lambda_1$ and $\lambda_2$ are constants, which have been estimated by using the least squares method with the collected data. Therefore, the negative sequence current caused by turn-to-turn fault can be written as follows:

$$I_{mn} = I_{sn} - (I_{sn} + I_{sn}) = I_{sn} - I_{sn} \quad (10)$$

The final fault signature is given as:

$$I_{mn} = I_x - I_{nx} - I_{exc} \quad (11)$$

On the other hand, the dependence of negative sequence current on supply voltage imbalance, other nonlinear motor effects (saturation, rotor static eccentricity) and load variations that also produce a negative sequence current must be eliminated. For this purpose, the negative sequence reactance can be written as [14]:

$$X^{-1} \approx \gamma + \gamma V_{sn} + \gamma I_{px} + \gamma I_{px}^2 \quad (12)$$

where, $1/\gamma$ is the fundamental value of the negative sequence reactance, $\gamma V_{sn}$ is for small dependence on $V_{sn}$. 

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Fig. 1. (a) Steady state negative sequence equivalent circuit of induction motor. (b) Phasor diagram corresponds to negative sequence components [14].
term $\gamma_2 \sin^2 \phi_n + \gamma_3 \cos^2 \phi_n$ is related to static eccentricity, $\gamma_4 I_{px}$ correspond to the change of the reactance with load and $\gamma_5 I_{py}$ correspond to the change of the reactance due to flux saturation. Finally, by using the equations (8)-(11) and (6), (12), the negative sequence current caused by turn-to-turn fault can be written as follows:

$$I'_{mn} = I_\alpha - V_{\mu} \sin(\theta_\alpha) [\gamma_0 + \gamma_1 V_{\alpha} + \gamma_2 \sin^2 \phi_n + \gamma_3 \cos^2 \phi_n + \gamma_4 I_{px} \cos \psi + \gamma_5 I_{py} \sin \psi \cos \psi],$$

(13)

It should be noted, in reference [14] it has been claimed that this technique is capable to detect single-turn faults. As has been noted by the authors, 2 steps are required for this method. First, factors $\gamma_0, \gamma_1, \gamma_2, \gamma_3, \gamma_4, \gamma_5$ are estimated under changing supply voltage imbalance, and then, factors $\beta_0, \beta_1, \beta_2, \lambda_0, \lambda_1$ and $\lambda_2$ are estimated under the situation of load and voltage variation. In fact, a mathematical method based on equations (8)-(13) for elimination of nuisance load and voltage variation. In fact, a mathematical method based on equations (8)-(13) for elimination of nuisance load and voltage variation. Hence, it can be clearly seen that the use of this method for detection is a complicated and time-consuming procedure that may limit its application [17].

3. Modeling of Induction Motor

The model of a symmetrical three-phase induction machine is well-known and is presented in [1] with sufficient details. On the other hand, turn-to-turn fault is one of the most complicated failures to detect. In fact, the variations of stator inductance due to turn-to-turn short circuit have to be taken into account.

Accurate calculation of the inductances of the faulty windings is the key for modeling the inter-turn short circuit faults. Useful and straightforward model of an asymmetrical induction motor having inter-turn short circuits on the stator winding is presented in [16]. This model is based on general motor parameters; consequently it is not required to know detailed machine geometry or physical layout of the machine windings.

Two orthogonal axis models for simulation of an induction machines considering asymmetrical windings and inter-turn fault in the stator windings is presented in this reference. The first model supposes that an induction machine has a different number of turns on each stator phase and the second model supposes phase a (on the stator winding) has two windings in series, including un-shorted portion and shorted portion. In the other words, in this method mutual interaction between neighboring portions will be considered that is the important factor for modeling the inter-turn short circuit faults. However, magnetic saturation is not considered within this reference [16]. Therefore, this model has been developed by considering the saturation effect for the simulations in this paper. For this machine with a uniform air-gap, it has been assumed that iron saturation affects the q- and d-axis components in the same manner, so that a common saturation characteristic like the one shown in Fig. 2 (a) can be used for both these components. The matrix equation governing the flux linkage-current relationship of the machine can be expressed as follows:

$$\mathbf{\psi} = \mathbf{\Psi} \mathbf{\phi}$$

where $\psi = \omega_b \lambda$, and $\omega_b$ is the base frequency at which the reactance is computed. Furthermore,

$$\frac{1}{X_n} = \left( \frac{1}{x_m} + \frac{1}{x_b} + \frac{1}{x_a} \right)$$

(15)

$$\psi_{ad} = X_n (\frac{\psi_{d'}}{x_{d'}} + \frac{\psi_{d'}}{x_{d'}})$$

(16)
Consequently, the currents of the stator and rotor windings can be calculated as follows:

\[
\begin{align*}
    i_{qs}^r &= \frac{1}{x_s}(\psi_{qs}^r - \psi_{mq}^s), \\
    i_{ds}^r &= \frac{1}{x_s}(\psi_{ds}^r - \psi_{md}^s) \\
    i_{qs}^s &= \frac{1}{x_s}(\psi_{qs}^s - \psi_{mq}^r), \\
    i_{ds}^s &= \frac{1}{x_s}(\psi_{ds}^s - \psi_{md}^r)
\end{align*}
\]  

(17)  

(18)

Denoting the saturated value of the mutual flux linkages by the superscript, sat, the saturated value of the mutual flux linkages per second in the q-axis is given by:

\[
\psi_{mq}^{sat} = \psi_{mq}^s - \Delta \psi_{mq}^r, \psi_{mq}^r = x_s (i_{qs}^r + i_{qs}^s)
\]  

(19)

Grouping like terms and using (16), the above expression can be written as:

\[
\begin{align*}
    \psi_{mq}^{sat} &= X_m \psi_{qs}^s + \frac{X_m}{x_p} \psi_{qs}^s - \frac{X_m}{x_m} \Delta \psi_{mq}^s \\
    \psi_{md}^{sat} &= X_m \psi_{ds}^s + \frac{X_m}{x_p} \psi_{ds}^s - \frac{X_m}{x_m} \Delta \psi_{md}^s
\end{align*}
\]  

(20)

Similarly, the saturated value of d-axis mutual flux linkage is given by:

\[
\psi_{md}^{sat} = X_m \psi_{ds}^s + \frac{X_m}{x_p} \psi_{ds}^s - \frac{X_m}{x_m} \Delta \psi_{md}^s
\]  

(21)

In addition, according to Fig. 2 (b), the following relationships can be obtained.

\[
\Delta \psi_{mq}^r = \frac{\psi_{mq}^{sat}}{\psi_{mq}^r} \Delta \psi_{mq}^s, \Delta \psi_{md}^r = \frac{\psi_{md}^{sat}}{\psi_{md}^r} \Delta \psi_{md}^s
\]  

(22)

\[
\Delta \psi_{mq}^r = \frac{\psi_{mq}^{sat}}{\psi_{mq}^r} \Delta \psi_{mq}^s = \frac{\psi_{md}^{sat}}{\psi_{md}^r} \Delta \psi_{md}^s
\]  

and

\[
\Delta \psi_{mq}^r = \frac{\psi_{mq}^{sat}}{\psi_{mq}^r} \Delta \psi_{mq}^s = \frac{\psi_{md}^{sat}}{\psi_{md}^r} \Delta \psi_{md}^s
\]

Fig. 3. (a) Block diagram of the saturation module [1]. (b) Internal structure of the negative sequence current module.
The relationship between $\Delta \psi$ and $\psi_{m}^{sat}$ can be determined from the no-load test curve of the machine, as shown in Fig. 2 (a). Block diagram of the saturation module is presented in Fig. 3 (a). The part of the machine that is affected by saturation is highlighted in this figure. Based on the above discussions, the model of an induction machine that is presented in [16] has been developed by considering the saturation effect. It should be noted, by changing the number of shorted turns and by a current limiting resistance, the fault severity can be controlled in the model. This model is simulated and implemented in “Simulink” under the environment of Matlab. In this model, there are some main modules: the park transformation module, the torque/speed module, the flux linkage module and the negative sequence current module. For instance, the internal structure of the negative sequence current module (one of the main module in this work) is shown in Fig. 3 (b). The content of this module is given in equations (1)-(7).

4. Simulation and experimental results

In this section, the relation between the different negative sequence currents ($I_n$, $I_{mn}$, $I_{sn}$) and number of shorted turns based on extensive tests under normal and faulty operations have been determined.

4. 1. Structure of the stator turn-to-turn fault detection, simulation measurement

In the following, the structure of turn-to-turn fault detection has been presented. First, faulty phase has been detected by the maximum peak value in the stator current. Then, the fault severity has been quantified based on negative sequence current criteria. The machine used in this study is a 3 hp, 420V, 4-pole, 50 Hz. This induction motor is a star connected, squirrel cage and has 252 turns per phase on the stator.

Figs. 4 (a) and (b) show the simulated RMS value of three-phase current of the stator at no-load and full-load under normal condition, respectively, while Figs. 4 (c) and (d) show these RMS values with 20 shorted turns in phase a respectively. According to Figs. 4 (c) and (d), it can be clearly seen that turn-to-turn fault occurring on one of the three-phases, causes a significant current appears in the corresponding phase. In fact, in the case of a turn-to-turn fault on one of the three-phases; the maximum peak value in the stator current is upon the phase where the fault has happened. With this indicator, the faulty phase can be localized. Furthermore, the effect of this fault on other stator phase currents is smaller than the effect on current of the faulty phase. Then in the next step, by extensive simulations the relation between the different negative sequence currents ($I_n$, $I_{mn}$, $I_{sn}$) and number of shorted turns have been determined.

As representative examples of the many simulations performed on this induction motor, some records due to space limitations are presented in Tables 1 and 2. In fact, the studied machine can be characterized by using these data. These data were obtained during acceleration from standstill to full speed. For example, negative sequence current vs. shorted turns arising from different causes under no-load and full-load conditions for 2.5% supply imbalance is presented in Fig. 5 (a). According to this figure, it is obvious that the negative sequence current caused by the turn-to-turn fault ($I_{mn}$) is proportional to the number NS of shorted turns, i.e.

$$I_{mn} = k(\text{NS})$$

(24)

where $k$ is constant and NS is number of shorted turns.

Furthermore, a zoom in on the negative sequence current vs. shorted turns caused by different supply imbalances under full-load have been presented in Fig. 5 (b). As it can be seen from this figure, $I_{sn}$ is independent of the number of shorted turns in balanced supply condition. This is as predictable because this negative sequence current is related to supplying imbalance.
Furthermore, it can be clearly seen that unbalanced supply conditions can produce a comparable negative sequence current and this current is approximately inversely proportional to the shorted numbers of turns in different supply unbalanced conditions. This means that stator turn-to-turn faults detection under unbalanced supply voltage conditions due to this non-linearity relationship is very difficult. In fact, the fault diagnosis method based on negative sequence current should be able to discriminate between the effects of turn shorts and supply imbalances. It should be noted that In, in Fig. 5 (a) is the total negative sequence current (sum of components Isn and Imn). Fig. 5 (c) shows the Imn vs. shorted turns under different supply imbalances for full-load. Moreover, Fig. 5 (d) illustrates this characteristic under different load conditions. According to these figures, Imn vs. shorted turns under different supply imbalances and different load situation is linear with the fault severity.

4.2 Experimental test setup, implementation of faults and numerical measurement

In order to validate the structure of the proposed method in this paper, experimental data are also used. For this aim, some tests are performed on an experimental test
Experimental test setup is illustrated in Fig. 6. This test bed is designed to study the behavior of induction motor under different stator turn-to-turn fault from both balanced and different unbalanced supply voltages. In fact, a usual commercially accessible motor was disassembled and by rewinding its stator with several taps on each phase, different turn-to-turn fault is produced. The squirrel cage induction motor utilized in these tests is a three-phase, 50 Hz, and 3 hp. This motor is loaded by an AC generator. Designed data acquisition card is used for sampling the stator current signals. Serial port interface has been utilized for connecting the data acquisition card to the computer and these data are communicated to the computer. Then these data are processed and analyzed using the environment of Matlab. In order to compare the experimental and the simulated measurement, the some characteristics of the experimental data for different conditions are presented in Fig. 7. For instance, Figs. 7 (a) and (b) show the experimental RMS value of three-phase current of stator with 20 shorted turns on phase a under different conditions. Simulated one for these data is shown in Fig. 4. In addition, Figs. 7 (c) and (d) show the negative sequence current vs. shorted turns arising from different causes under different conditions. A similar behavior is seen in Figs. 5 (a) and (c) respectively. The small difference between the experimental and the simulated measurement may be caused by the following reasons. The actual machine may have little abnormalities in assembling or construction. In addition, internal errors of sensors, different parameters used in simulation and measurement errors have an effect on this difference. However, regardless of these differences, the curves of the simulated and experimental data have similar behavior.

5. Design of Fault Diagnosis System with the Aid of GRNN

The main issues raised by critics about the ANN based methods are the need of these techniques to an enormous training effort to train for all possible fault scenarios that is a complicated and time-consuming procedure [26]. However, it is worth highlighting that the key feature of the GRNN is the speed at which the neural network can be trained.

In the training procedure of these types of neural networks, there are no training parameters, such as momentum and learning rate as in the case of the multilayered perceptron (MLP) neural network. The main feature of the GRNN compared to other networks is due to GRNN’s one-pass instantaneously learning [25], [27]. In fact, the

![Fig. 6. Experimental test setup.](image)

![Graph](image)

(a) Experimental RMS value of three-phase current of stator with 20 shorted turns on phase a under no-load condition.
inherently parallel structure and the fast training procedure of the GRNN make it suitable for fault detection problems in real time. Some advantages of the GRNN over other artificial neural networks are summarized in the following [27], [28].

• The GRNN networks don’t require pre-decision on the number of layers and hidden neurons.

• There is no require setting the initial weights and no connection exists between learning and recalling procedures in these kinds of neural networks.

Therefore, in this research, GRNN is used in the design of fault diagnosis system and non-invasive criterion, i.e. negative sequence current is considered as efficient indicators of stator fault. GRNN is a kind of RBF neural network suitable for function approximation and performs regression where the target variable is continuous. The structure of the GRNN is presented in Fig. 7. This architecture includes input, pattern, summation and output layer. The first layer is the input-layer and nodes in this layer do not perform any computation. The number of neurons in this layer is equal to the number of independent features and neurons in input-layer merely distribute input features to all the nodes in the pattern layer. Pattern layer calculates the Euclidean distance between input vector values and centers of radial basis functions. The third layer is summation layer and there are two nodes in this layer. One node is the denominator unit, and the other node is the numerator unit. The denominator unit adds together the weight values coming from each of the pattern nodes. The numerator unit adds together the weight values multiplied by the aim value for each pattern node. The fourth layer is the decision or output layer. This layer divides the value collected in the numerator unit by the value in the denominator unit and uses the consequence as the predicted aim value [27]. The foundation for regression is finding relations between output values Y and input patterns X. If it is assumed that X is new input variable containing known inputs, it is possible to define the Euclidean distance as in (25):

\[ d_p^2 = (x - x_p)^T (x - x_p) \]  

(25)

Using this Euclidean distance, GRNN estimates the output vector Y of the pattern X as in (26):
where, $\alpha$ is an adjustable smoothing parameter.

After the GRNN is trained, the next step is to ensure its performance, i.e. how it behaves to an arbitrary input which is not in the training set. In order to verify this performance, various sets of inputs are selected. As representative examples of the many tests performed to evaluate the performance of GRNN, details of the two test cases due to space limitations is presented in Tables 3 and 4.

These test points that are obtained by the simulated measurement with different contact resistance are considered as inputs for testing the GRNN. Then the GRNN estimates the number of shorted turns. Test results show that the GRNN is able to approximate the number of shorted turns in an acceptable error.

5.1 Training database

According to extensive simulations, the following set of diagnostic features has been proposed for data processing.

- $I_{sn}$: is the negative sequence current arising from imbalance in the supply voltage, $I_{mn}$: is the negative sequence current caused by the turn-to-turn fault in the motor, $I_n$: is the total negative sequence current (sum of components $I_{sn}$ and $I_{mn}$), $r_{ext}$: is the contact resistance, $NS$: Number of shorted turns, $L$: Load, $V$: supply voltage, $Si$: supply voltage imbalance.

In the other words, data sets for GRNN have been prepared, based on these diagnostic criteria, i.e. the following vectors are defined as input and target data for training and testing the GRNN:

Input data: $V$, $r_{ext}$, $I_n$, $I_{sn}$, $I_{mn}$, and Target data: $NS$, $L$, $Si$.

Input vectors for training and testing procedure of GRNN have been obtained from simulation’s measurements of the motor under different load conditions and supply voltage imbalances. In addition, stator inter-turn faults with different severity are considered in this motor.

An extensive database, containing 8400 records has been created. Training data contained 5600 input records; however, testing data had 2800 records. These data for training and testing procedure are independent. In order to build these data, the variation range of load conditions, supply voltage imbalances, contact resistance and short circuit turn ratio needs to be determined first. In this research, the variation range of the load is set as 0, 25%, 50%, 75%, and 100%, the variation range of the contact resistance is set as 0, 0.1, 0.2, and 0.5 ohm and the short circuit turn ratio varies from 0% to 40% by 2% step size. Furthermore, supply voltage imbalances have been varied from -2.5% to 2.5% by 0.25% step size. So total, 8400 cases that $8400=5$ (different load conditions) 4 (different contact resistance) 21 (short circuit turn ratio) 20 (supply voltage imbalance) have been considered to build the training and testing data.

5.2 Evaluate the performance of the fault diagnosis system

Designed fault diagnosis system was tested due to the cross-validation technique. The data for training and testing procedure was separated into 3 portions; two of them were used for training procedure; the third was used for the testing procedure. The GRNN training process is usually carried out in 2 steps. A serious aspect of the training process is mainly represented by efficient selection of the center and standard deviation of the Gauss function, as this choice may effectively influence errors made by the estimator [27]. So, in designing of the GRNN, it is very significant to choose the optimum value of the spread parameter. Procedure of approximation begins with finding the best spread value for GRNN to control the spread of the RBF functions. If spread value is small the activation function is very steep, consequently, the neuron with the weight vector nearby to the input will have a greater

### Table 3. Number of shorted turns (NS) predicted by GRNN for Case 1

<table>
<thead>
<tr>
<th>$I_n$ (mA)</th>
<th>$I_{sn}$ (mA)</th>
<th>$I_{mn}$ (mA)</th>
<th>Actual NS</th>
<th>Predicted NS</th>
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<td>197.5</td>
<td>197.4</td>
<td>0.0076</td>
<td>0</td>
<td>0</td>
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<td>138.7</td>
<td>310.2</td>
<td>5</td>
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<td>10</td>
<td>9.92</td>
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<tr>
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<td>113.2</td>
<td>919.8</td>
<td>15</td>
<td>14.85</td>
</tr>
<tr>
<td>1349</td>
<td>110.2</td>
<td>1238</td>
<td>20</td>
<td>20.01</td>
</tr>
<tr>
<td>1678</td>
<td>109.2</td>
<td>1569</td>
<td>25</td>
<td>25.02</td>
</tr>
<tr>
<td>2023</td>
<td>109.4</td>
<td>1913</td>
<td>30</td>
<td>29.83</td>
</tr>
<tr>
<td>2381</td>
<td>110.3</td>
<td>2271</td>
<td>35</td>
<td>34.92</td>
</tr>
<tr>
<td>2755</td>
<td>111.5</td>
<td>2643</td>
<td>40</td>
<td>40.08</td>
</tr>
</tbody>
</table>

### Table 4. Number of shorted turns (NS) predicted by GRNN for Case 2

<table>
<thead>
<tr>
<th>$I_n$ (mA)</th>
<th>$I_{sn}$ (mA)</th>
<th>$I_{mn}$ (mA)</th>
<th>Actual NS</th>
<th>Predicted NS</th>
</tr>
</thead>
<tbody>
<tr>
<td>197.5</td>
<td>197.4</td>
<td>0.0076</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>270</td>
<td>171.7</td>
<td>98.26</td>
<td>5</td>
<td>4.98</td>
</tr>
<tr>
<td>431.7</td>
<td>140.8</td>
<td>290.9</td>
<td>10</td>
<td>9.965</td>
</tr>
<tr>
<td>646.4</td>
<td>122.9</td>
<td>523.5</td>
<td>15</td>
<td>14.89</td>
</tr>
<tr>
<td>896</td>
<td>113.4</td>
<td>782.6</td>
<td>20</td>
<td>19.96</td>
</tr>
<tr>
<td>1172</td>
<td>108.4</td>
<td>1063</td>
<td>25</td>
<td>24.95</td>
</tr>
<tr>
<td>1469</td>
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<td>29.91</td>
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<tr>
<td>1786</td>
<td>105</td>
<td>1681</td>
<td>35</td>
<td>35.05</td>
</tr>
<tr>
<td>2122</td>
<td>105</td>
<td>2017</td>
<td>40</td>
<td>39.87</td>
</tr>
</tbody>
</table>
output than other neurons. The GRNN tends to react with the target vector associated with the nearest design input vector, and the accuracy of the detection will be increased but the generalization ability of the GRNN will be reduced. As smoothing value becomes larger, more neurons contribute to the average and the slope of the activation function becomes smoother. The GRNN then operates as if it is taking a weighted average between target vectors whose design input vectors are nearby to the new input vector. In this condition, the generalization ability of the GRNN will be increased and the accuracy of the detection will be reduced. In this study, the traditional trial-and-error technique is utilized to find the optimum spread value. To evaluate the proficiency of GRNN, its results are compared with MLP neural network. MLP network is trained and then tested with the same data due to a similar process that has been mentioned before. First fault detector uses MLP, and the second detector uses GRNN. The MLP is trained with the Batch Gradient Descent with Momentum. The results of the evaluation are shown in Table 5.

During the testing procedure, the precision of MLP neural network is around 75% (2100/2800) because the results of 700 testing data were incorrect in this neural network. Furthermore, the results of 112 testing data were incorrect in GRNN. Consequently, the accuracy is 96% (2688/2800). In fact; the results illustrate that the performance of GRNN is better than MLP in terms of accuracy.

<table>
<thead>
<tr>
<th>Classification accuracy</th>
<th>ANN</th>
<th>MLP</th>
<th>GRNN</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>75</td>
<td>≥96%</td>
<td></td>
</tr>
</tbody>
</table>

### 6. Conclusion

Detection of stator turn-to-turn faults occurrence and its exact location under supply voltage unbalances are too complex. This mainly because the effect caused by turn-to-turn faults and supply voltage unbalances on the stator current is similar. This paper presents, the application of GRNN to the development of a new approach to detect and locate stator turn-to-turn fault in the induction motor under supply voltage unbalances. On the other hand, ANN based methods suffer from the drawback that they need large learning time for training the all possible fault scenarios. Consequently, in order to overcome this problem, the proposed method uses a GRNN. It is worth highlighting that GRNN networks with high generalization ability, are able to do satisfactorily even for unobserved scenario. Another point worth highlighting is the GRNN trains instantaneously in one-pass which causes them faster to train, compared to other neural networks. The required decision in the proposed method is made using negative sequence current analysis. The main feature of the proposed technique is its ability to detect the stator turn-to-turn fault using the non-invasive method. A possibility of identifying the location of the faulty method, the fault severity and the degree of supply voltage unbalance is the other features of the proposed technique. Finally, the satisfactory operation of the proposed technique has been verified via both simulation and experimental results under the load variations and supply voltage unbalance.

### Acknowledgment

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### References


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