

Analytical Modeling of Magnetic Field Distribution in Inner Rotor Brushless Magnet Segmented Surface Inset Permanent Magnet Machines

A. Jabbari^{*(C.A.)}

Abstract: Brushless permanent magnet surface inset machines are interested in industrial applications due to their high efficiency and power density. Magnet segmentation is a common technique in order to mitigate cogging torque and electromagnetic torque components in these machines. An accurate computation of magnetic vector potential is necessary in order to compute cogging torque, electromagnetic torque, back electromotive force and self/mutual inductance. A 2D analytical method for magnetic vector potential calculation in inner rotor brushless segmented surface inset permanent magnet machines is proposed in this paper. The analytical method is based on the resolution of Laplace and Poisson equations as well as Maxwell equation in a quasi- Cartesian polar coordinate by using sub-domain method. One of the main contributions of the paper is to derive an expression for the magnetic vector potential in the segmented PM region by using hyperbolic functions. The developed method is applied on the performance computation of two prototype surface inset magnet segmented motors with open circuit and on load conditions. The results of these models are validated through FEM method.

Keywords: 2D Analytical Modeling, Segmented Permanent Magnet, Surface Inset DC Machine, Sub-Domain Method, Hyperbolic Functions.

1 Introduction

Brushless permanent magnet motors are interested in industrial applications due to their high efficiency and power density [1-3]. Magnet segmentation is an effective and simple technique for cogging torque reduction in high power permanent-magnet brushless machines. An accurate prediction of air-gap magnetic field distribution is necessary in order to calculate machine performance.

Several researches has been carried out to compute the effect of magnet segmentation on machine performance. An analytical approach is used to predict cogging torque harmonics [4]. The key idea was to set the distribution

of the air-gap flux density by segmenting the magnet pole into several elementary magnet blocks.

An experimental examination and three-dimensional numerical analysis by the finite element method is applied to investigate the cogging torque force in a magnet segmented permanent magnet linear synchronous motor [5].

An analytical method was proposed to evaluate the effect of both circumferential and axial segmentations on losses' reduction in various conditions, concerning the skin effect in a magnet segmented synchronous machine [6]. Finite-element calculation confirms the results of the analysis.

Finite-element analysis (FEA) is used to optimize segmented magnet size in permanent magnet synchronous motor using a multiobjective optimization framework [7].

The effect of eddy current loss reduction by magnet segmentation in synchronous motors with concentrated windings was studied in [8] by using 3-D finite element analysis with Fourier transformation.

A method for the calculation of eddy current losses in

Iranian Journal of Electrical & Electronic Engineering, 2018.
Paper first received 06 November 2017 and accepted 08 February 2018.

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the permanent magnets, which takes into account the reaction of induced eddy currents was proposed in [9]. The developed quasi-3-D analytical method considers the effects of axial and circumferential segmentation of magnets.

In [10], the 1D airgap magnetic fields of multiple multilayer 2D finite element simulations are combined to a 2D airgap magnetic field using static simulations. The introduced multilayer-2D - 2D coupled model is used to study the effect of segmentation on the eddy-current loss in the permanent magnets of an axial-flux PM machine simulating different segmentation grades.

The axial segmentation of the PMs is employed to cut off the eddy-current axial paths in axial flux permanent magnet motor [11]. A nodal method based network-field coupled multislice time-stepping finite element method (TS-FEM) is proposed to analyze the steady-state and dynamic characteristics of the high-speed PM machine.

Segmentation of magnets was proposed to reduce magnet eddy current loss, and finally a new structure based on segmentation was proposed to optimize the eddy current loss [12].

A newly developed high torque density interior permanent magnet motor with a flux concentration configuration design for electric racing cars considering magnet segmentation was proposed in [13].

Magnet segmentation is proposed to meet the overheating challenge [14].

A closed-form 3D analytical model developed for the estimation of eddy current losses in a magnet segmented interior permanent magnet synchronous machine [15].

A two-dimensional (2D) analytical subdomain model is proposed based on virtual PM blocks in magnet segmented PMSM [16].

A closed-form 2D analytical model developed for the estimation of eddy current loss in segmented magnet interior permanent magnet machines [17]. The proposed model can be directly used to evaluate the eddy current magnet loss for magnet segmentation in the circumferential direction.

An investigation of magnet segmentation and its susceptibility to demagnetization in an in-wheel motor for an electric vehicle was carried out in [18]. The analyzed motor is a high torque density, low speed, surface-mounted permanent magnet (SMPM) modular motor with fractional slot concentrated winding (FSCW) and an outer rotor.

Verified simulation models both in 2D and 3D are used to compare a radial flux machine (IPM) with a transverse flux machine (TFM) for a traction application [19]. It also shows the practical handling of loss modelling in 2D and 3D respectively, including a stacking factor for the core lamination and magnet segmentation.

An analytical approach for studying rotor losses in permanent magnet surface mounted synchronous machines considering magnet segmentation was proposed in [20].

A switched flux permanent magnet (SFPM) machine with radially segmented permanent magnets (PMs) is presented in [21]. The thickness of each segment is optimized to maximize the torque performance and reduce the total magnet material volume.

A new structure based on segmentation was proposed to optimize the eddy current loss in [22].

Sub-domain model [23-27] is reported to model electrical machines and are useful in first step of performance evaluation and design optimization stage. The sub-domain model is more accurate than the other analytical models [23].

To the author's knowledge, a few analytical models are presented to calculate magnetic vector potential in surface inset permanent magnet motors [23-27]. No references in the literature addressing the issue of an analytical model for surface inset magnet segmented machines considering magnet segmentation were found.

The focus of this paper is to develop an analytical model based on resolution of Laplace and Poisson equations in surface inset permanent magnet machines by using the sub-domain method considering magnet segmentation and slotting effects. It is shown that the developed model can effectively estimate magnetic vector potential, magnetic flux density, cogging torque and electromagnetic torque. This model is applied on the performance calculation of two prototypes, i.e., a 4 segmented 4P-18S PM surface inset brushless DC motor and a 2 segmented 6P-18S surface inset brushless DC motor. It's shown that the results of analytical model are in close agreement with the results of FEM.

The problem definition and assumptions are presented in Section 2. Analytical expressions of magnetic vector potential in each sub-domain are developed in Section 3. Performance calculation and model validation is described in Section 4.

2 Problem Definition

The geometrical representation of the investigated permanent magnet motor with magnet segmented outer rotor layout is shown in Fig. 1. The machine model is divided into three sub-domains including the armature slots region (domain l) which has G_1 slots, the air-gap region (domain I) and the permanent magnet region (domain i) which has G_2 magnets. The machine parameters including the rotor slot inner radius, R_1 , the rotor outer radius, R_2 , the stator surface radius, R_3 , the stator yoke radius, R_4 .

The angular position of the j -th armature slot and k -th stator permanent magnet are defined as (1) and (2), respectively.

$$\theta_l = -\frac{\beta}{2} + \frac{2l\pi}{G_1} \quad \text{with } 1 \leq l \leq G_1 \quad (1)$$

$$\theta_i = -\frac{\alpha}{2} + \frac{2i\pi}{G_2} \quad \text{with } 1 \leq i \leq G_2 \quad (2)$$

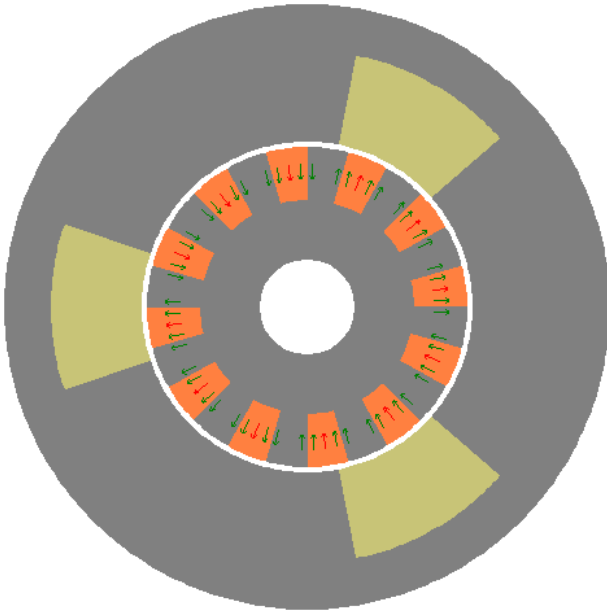


Fig. 1 The schematic representation of an inner rotor segmented surface inset PM machine.

3 Magnetic Vector Potential Calculation

General solution of Laplace or Poisson equation in each sub-domain is developed in this section. The Laplace equation can be described in polar form as

$$\frac{\partial^2 A}{\partial r^2} + \frac{1}{r} \frac{\partial A}{\partial r} + \frac{1}{r^2} \frac{\partial^2 A}{\partial \theta^2} = 0 \quad \text{for} \quad \begin{cases} R_1 \leq r \leq R_2 \\ \theta_1 \leq \theta \leq \theta_2 \end{cases} \quad (3)$$

Replacing r by $R_1 e^t$, one obtains

$$\frac{\partial^2 A}{\partial t^2} + \frac{\partial^2 A}{\partial \theta^2} = 0 \quad \text{for} \quad \begin{cases} \ln\left(\frac{R_1}{R_2}\right) \leq t \leq 0 \\ \theta_1 \leq \theta \leq \theta_2 \end{cases} \quad (4)$$

3.1 Magnetic Vector Potential in the Rotor Permanent Magnet Sub-Domain (Region i)

The Poisson equation in the stator permanent magnet sub-domain is given by

$$\frac{\partial^2 A_i}{\partial t^2} + \frac{\partial^2 A_i}{\partial \theta^2} = -\frac{\mu_0 e^t}{R_1} \left(M_{\theta k} - \frac{\partial M_{ri}}{\partial \theta} \right) \quad \text{for} \quad \begin{cases} t_2 \leq t \leq t_1 \\ \theta_i \leq \theta \leq \theta_i + \alpha \end{cases} \quad (5)$$

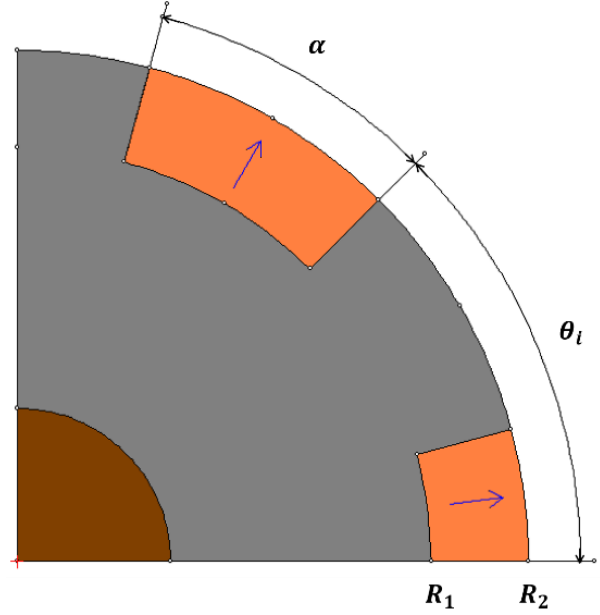


Fig. 2 Two segmented permanent magnet region (domain i) with its boundaries.

where $t_1 = 0$ and $t_2 = \ln(R_1/R_2)$.

The radial and tangential components of radial magnetization for segmented surface inset permanent magnet design can be expressed as

$$M_{ri} = (-1)^{\lfloor \frac{i}{m+0.8} \rfloor} \frac{B_r}{\mu_0} \quad \text{with} \quad i = 1, 2, \dots, G_1 \quad (6)$$

$$M_{\theta i} = 0 \quad (7)$$

where m is the number of magnet segmentations.

Neumann boundary conditions at the bottom and both sides of the permanent magnet slot are obtained as

$$\left. \frac{\partial A_i}{\partial \theta} \right|_{\theta=\theta_i} = q(t) = R_1 e^{-t} (-1)^{\lfloor \frac{i}{m+0.8} \rfloor} B_r \quad (8)$$

$$\left. \frac{\partial A_i}{\partial \theta} \right|_{\theta=\theta_i+\alpha} = q(t) = R_1 e^{-t} (-1)^{\lfloor \frac{i}{m+0.8} \rfloor} B_r \quad (9)$$

$$\left. \frac{\partial A_i}{\partial t} \right|_{t=t_1} = 0 \quad (10)$$

The general solution of (5) is given by

$$A_i(t, \theta) = a_0^i + R_1 (e^{-t} + t) (-1)^{\lfloor \frac{i}{m+0.8} \rfloor} B_r \left(\theta - \theta_i - \frac{\alpha}{2} \right) + \sum_{h=1}^{\infty} \left(\frac{\cosh(z(t-t_1))}{\cosh(z(t_2-t_1))} a_h^i - X_h^i R_1 \left(e^{-t} + \frac{1}{z} e^{zt} \right) \right) \cos(z(\theta - \theta_i)) \quad (11)$$

$$X_h^i = \begin{cases} \frac{4(-1)^{\lfloor \frac{i}{m+0.8} \rfloor} B_r}{\alpha z^2 (z^2 - 1)} & \text{if } h = 1, 3, 5, \dots \\ 0 & \text{if } h = 2, 4, 6, \dots \end{cases} \quad (12)$$

where $z = h\pi/\alpha$, h is a positive integer and the coefficients a_0^i and a_h^i are determined based on the continuity and interface conditions.

The continuity of the magnetic vector potential between the sub-domain i and the regions I leads to

$$A_i(t_2, \theta) = A_I(t_3, \theta) \quad \text{for } \theta_i \leq \theta \leq \theta_i + \alpha \quad (13)$$

Interface condition (13) gives:

$$a_0^i = R_1 (-1)^{\lfloor \frac{i}{m+0.8} \rfloor} B_r \left(\theta - \theta_i - \frac{\alpha}{2} \right) + \frac{1}{\alpha} \int_{\theta_i}^{\theta_i + \alpha} A_I(t_3, \theta) d\theta \quad (14)$$

$$a_h^i = \frac{2}{\alpha} \int_{\theta_i}^{\theta_i + \alpha} A_I(t_3, \theta) \cdot \cos(z(\theta - \theta_i)) d\theta \quad (15)$$

3.2 Magnetic Vector Potential in the Air-Gap Sub-Domain (Region I)

The Laplace equation in the air-gap sub-domain is given by

$$\frac{\partial^2 A_I}{\partial t^2} + \frac{\partial^2 A_I}{\partial \theta^2} = 0 \quad \text{for } \begin{cases} t_3 \leq t \leq t_4 \\ 0 \leq \theta \leq 2\pi \end{cases} \quad (16)$$

where $t_3 = 0$ and $t_4 = \ln(R_2/R_3)$.

The general solution of (16) considering periodicity boundary conditions is obtained as (17), where n is a positive integer.

The coefficients a_n^I , b_n^I , c_n^I and d_n^I are determined considering the continuity of magnetic vector potential between the internal airgap sub-domain I and the region j and k using a Fourier series expansion of interface condition (14) and (15) over the air-gap interval.

The continuity of the magnetic vector potential between the internal air-gap sub-domain I and the regions l and i leads to

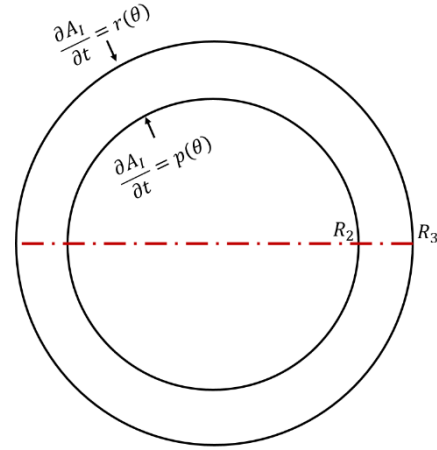


Fig. 3 Air-gap region (domain I) with its boundaries.

$$\left. \frac{\partial A_I}{\partial t} \right|_{t=t_3} = p(\theta) = \begin{cases} \left. \frac{\partial A_I}{\partial t} \right|_{t=t_2} & \text{for } \theta_i \leq \theta \leq \theta_i + \alpha \\ 0 & \text{elsewhere} \end{cases} \quad (18)$$

$$\left. \frac{\partial A_I}{\partial t} \right|_{t=t_4} = r(\theta) = \begin{cases} \left. \frac{\partial A_I}{\partial t} \right|_{t=t_3} & \text{for } \theta_i \leq \theta \leq \theta_i + \beta \\ 0 & \text{elsewhere} \end{cases} \quad (18)$$

Interface condition (18) gives:

$$a_n^I = \frac{2}{2\pi} \int_{\theta_i}^{\theta_i + \alpha} p(\theta) \cdot \cos(n\theta) d\theta \quad (20)$$

$$c_n^I = \frac{2}{2\pi} \int_{\theta_i}^{\theta_i + \alpha} p(\theta) \cdot \sin(n\theta) d\theta \quad (21)$$

Interface condition (19) gives:

$$b_n^I = \frac{2}{2\pi} \int_{\theta_i}^{\theta_i + \beta} r(\theta) \cdot \cos(n\theta) d\theta \quad (22)$$

$$d_n^I = \frac{2}{2\pi} \int_{\theta_i}^{\theta_i + \beta} r(\theta) \cdot \sin(n\theta) d\theta \quad (23)$$

$$A_I(t, \theta) = \sum_{n=1}^{\infty} \left(\frac{1 \cosh(n(t-t_4))}{n \sinh(n(t_3-t_4))} a_n^I + \frac{1 \cosh(n(t-t_3))}{n \sinh(n(t_4-t_3))} b_n^I \right) \cos(n\theta) + \sum_{n=1}^{\infty} \left(\frac{1 \cosh(n(t-t_4))}{n \sinh(n(t_3-t_4))} c_n^I + \frac{1 \cosh(n(t-t_3))}{n \sinh(n(t_4-t_3))} d_n^I \right) \sin(n\theta) \quad (17)$$

3.3 Magnetic Vector Potential in the Stator Slot Sub-Domain (Region I)

The Poisson equation in the armature slot sub-domain is given by

$$\frac{\partial^2 A_I}{\partial t^2} + \frac{\partial^2 A_I}{\partial \theta^2} = -\mu_0 J \quad \text{for} \quad \begin{cases} t_5 \leq t \leq t_6 \\ \theta_l \leq \theta \leq \theta_l + \beta \end{cases} \quad (24)$$

where $t_5 = 0$ and $t_6 = \ln(R_3/R_4)$.

Neumann boundary conditions at the bottom and at each side of the slot are obtained as

$$\left. \frac{\partial A_I}{\partial \theta} \right|_{\theta=\theta_l} = 0 \quad \text{and} \quad \left. \frac{\partial A_I}{\partial \theta} \right|_{\theta=\theta_l+\beta} = 0 \quad (25)$$

$$\left. \frac{\partial A_I}{\partial t} \right|_{t=t_6} = 0 \quad (26)$$

The general solution of (24) using the separation of variables method is given by (27), where h is a positive integer and the coefficients a_0^I and a_h^I are determined based on the continuity and interface conditions.

The continuity of the magnetic vector potential between the sub-domain j and the region I leads to

$$A_I(t_5, \theta) = A_I(t_4, \theta) \quad \text{for} \quad \theta_l \leq \theta \leq \theta_l + \beta \quad (28)$$

Interface condition (28) gives:

$$a_0^I = \frac{1}{2} \mu_0 J_i \left(e^{-t_6} + \frac{1}{2} e^{-2t+t_6} \right) + \frac{1}{\beta} \int_{\theta_l}^{\theta_l+\beta} A_I(t_4, \theta) d\theta \quad (29)$$

$$a_h^I = \frac{2}{\beta} \int_{\theta_l}^{\theta_l+\beta} A_I(t_4, \theta) \cdot \cos\left(\frac{h\pi}{\beta}(\theta - \theta_l)\right) d\theta \quad (30)$$

$$A_I(t, \theta) = a_0^I - \frac{1}{2} \mu_0 J_i \left(e^{-t_6} + \frac{1}{2} e^{-2t+t_6} \right) + \sum_{h=1}^{\infty} \left(\frac{\cosh\left(\frac{h\pi}{\alpha}(t - t_6)\right)}{\cosh\left(\frac{h\pi}{\alpha}(t_5 - t_6)\right)} \right) a_h^I \cdot \cos\left(\frac{h\pi}{\beta}(\theta - \theta_l)\right) \quad (27)$$

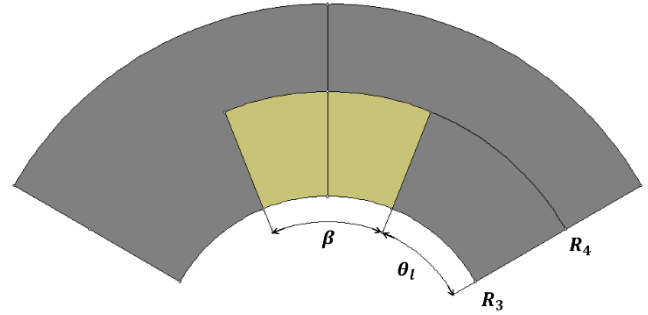


Fig. 4 Stator slot region (domain I) with its boundaries.

4 Performance Calculation and Model Evaluation

In this section, the proposed analytical model is used to study performance characteristics of two prototype motors, i.e., 4P-18S and 6P-18S, in magneto-static and transient modes. The results of analytical method are then verified by the results of finite element method. The motors parameters are given in Table 1. The schematic representation model of two investigated surface inset PM motors and their corresponding magnetic flux distribution obtained by FEA are shown in Fig. 5 and Fig. 6, respectively. The electromagnetic torque is obtained using the Maxwell stress tensor and expressed as

$$T_e = \frac{L_s}{\mu_0} \int_0^{2\pi} BI_r(t_e, \theta) \cdot BI_\theta(t_e, \theta) d\theta \quad (31)$$

where BI_r is radial flux density in I region, BI_θ is tangential flux density in I region, L_s is the axial length of the motor and t_e is calculated by

$$t_e = \ln\left(\frac{R_2}{R_e}\right) \quad (32)$$

$$R_e = (R_2 + R_3) / 2$$

Table 1 Parameters of the investigated brushless motors.

Symbol	Quantity	4P-18S Motor S=4	6P-18S Motor S=2
R_1	Inner radius of the rotor PM	30.2mm	30.2mm
R_2	Outer radius of the rotor PM	37.2mm	37.2mm
R_3	Inner radius of the stator slot	38.9mm	38.9mm
R_4	Outer radius of the stator slot	74.75mm	74.75mm
θ_l	Angular position of the first PM	23	30
θ_l	Angular position of the first slot	22	22
α	PM width angle	16	15
β	Slot width angle	18	18
p	Pole pairs-number	2	3
β_r	Remanence of the PMs	0.5T	0.5T
L_s	Axial length	80mm	80mm

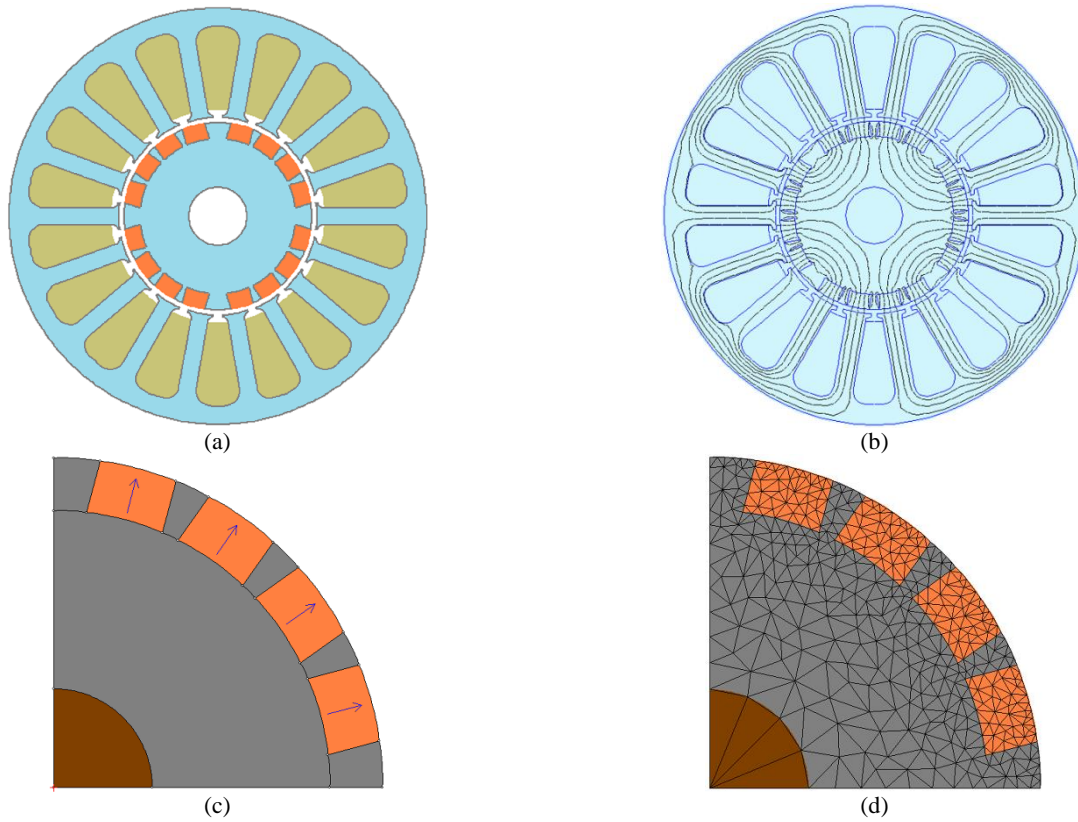


Fig. 5 Four segmented surface inset PM motor: a) The schematic representation, b) magnetic flux distribution, c) magnet segmented rotor and d) rotor mesh density.

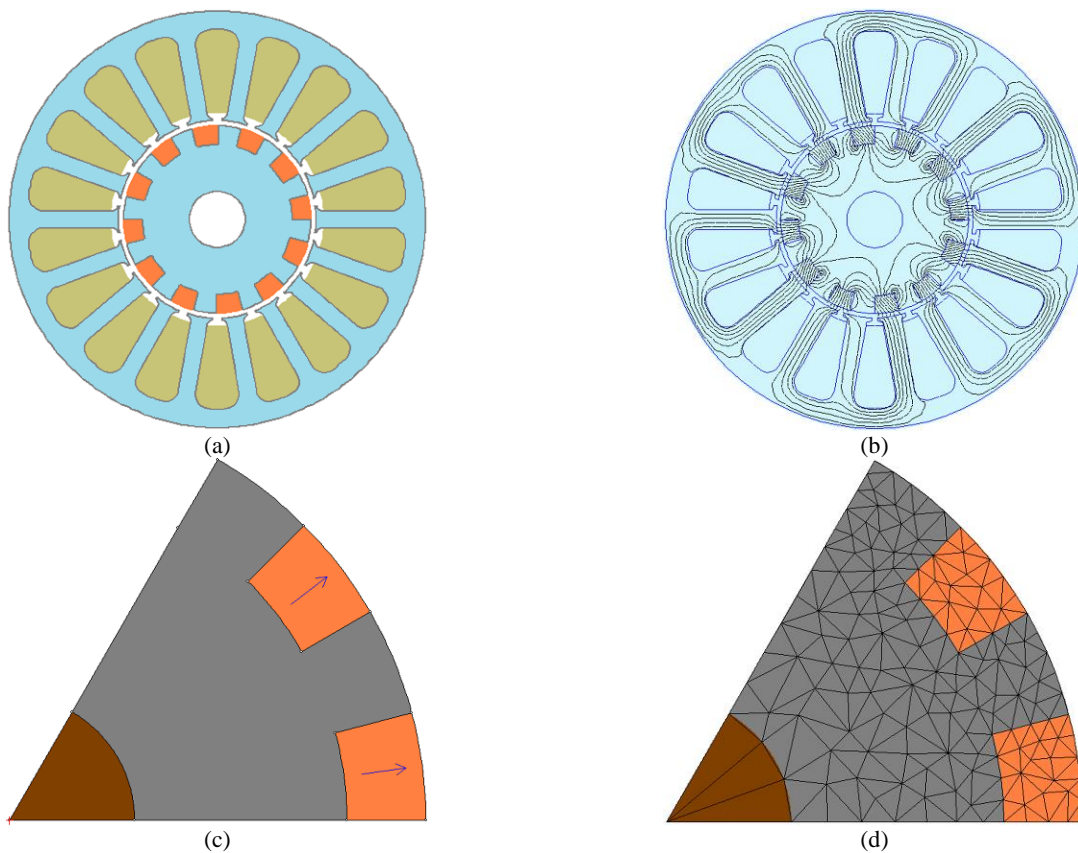


Fig. 6 Two segmented surface inset PM motor: a) The schematic representation, b) magnetic flux distribution, c) magnet segmented rotor, d) rotor mesh density.

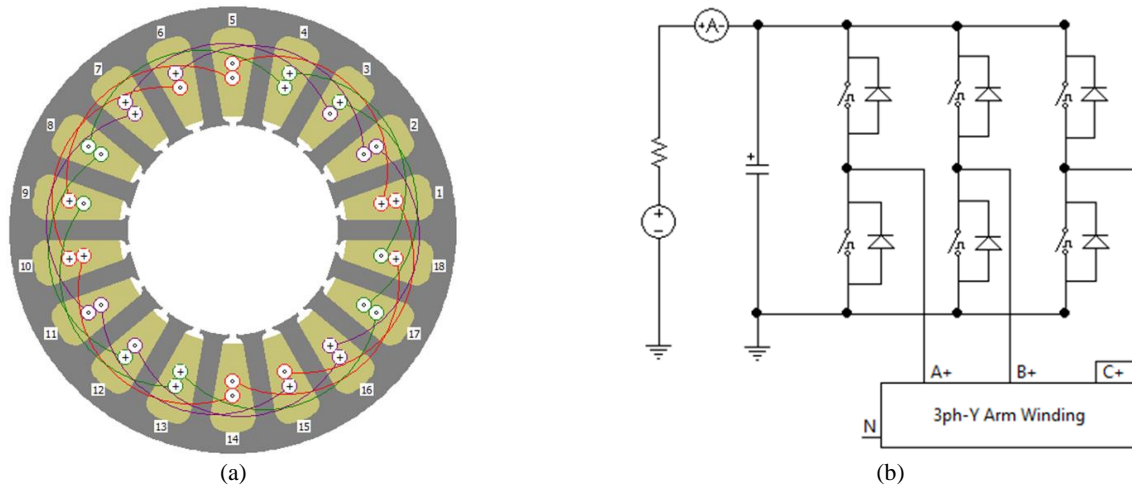


Fig. 7 Stator winding and drive circuit: a) three phase winding, b) full bridge drive circuit.

2D finite element method is applied on performance calculation of the two prototype motors, i.e., 4P-18S and 6P-18S motors. An open circuit analytical and numerical comparison of radial flux density distribution in mid-airgap diameter of 4P-18S and 6P-18S motors are shown in Fig. 8(a) and (b), respectively. A comparison of on load analytical and numerical results of tangential flux density in the investigated motors are shown in Fig. 9(a), and (b). As shown in Fig. 10(a) and (b), cogging torque waveforms are compared using analytical and numerical models. The results of analytical and numerical computation of radial and tangential components of flux density under rated load condition are shown in Fig. 11 and 12, respectively. At this condition, a comparison of electromagnetic torque and back EMF waveforms in the studied motors are compared analytically and numerically as shown in Fig. 13 and 14, respectively. The effect of magnet segmentation on cogging torque in 4P-18S motor is shown in Fig. 15.

The open circuit and on load radial components of the flux density distribution in the middle of the air gap (at $r = 38$ mm) are shown in Fig. 8 and Fig. 10, respectively. The effect of magnet segmentation on the radial component waveform of the flux density is clear. The effect of slot opening on the flux density waveform 2 segmented and 4 segmented topologies is very clear. However, in case of two segmented motor, the flux density waveforms distortions at the locations of the rotor slots diminished. The analytical results are in an excellent agreement with results of fine element method. It can be seen that the presented analytical model can compute the cogging torque, back-emf and electromagnetic torque with an excellent precision for

segmented surface inset topologies. Fig. 13 shows the electromagnetic torque waveforms in terms of rotor position in the surface inset topologies. At each rotor position, the current values in the different slots updated to have a sinusoidal current waveform.

5 Conclusion

An exact analytical model for performance prediction in surface inset permanent magnet machines considering slotting effects and magnet segmentation has been developed in this paper. Fourier analysis method based on sub-domain method is applied to derive analytical expressions for calculation of magnetic vector potential, magnetic flux density, cogging torque and electromagnetic torque in surface inset permanent magnet machines. This model is applied for performance computation of two prototype motors and the results of proposed model are verified by using FEM method.

Appendix

The Laplace equation can be described in quasi-Cartesian coordinate system as

$$\frac{\partial^2 A}{\partial t^2} + \frac{\partial^2 A}{\partial \theta^2} = 0 \quad \text{for} \quad \begin{cases} \ln\left(\frac{R_1}{R_2}\right) \leq t \leq 0 \\ \theta_1 \leq \theta \leq \theta_2 \end{cases} \quad (33)$$

The general solution of (33) is obtained as (34), where n is a positive integer.

The coefficients a_n , b_n , c_n and d_n are determined considering the continuity of magnetic vector potential between two adjacent subdomains.

$$A(t, \theta) = a_0 + \sum_{n=1}^{\infty} \left(\frac{1 \cosh(n(t-t_2))}{n \sinh(n(t_1-t_2))} a_n + \frac{1 \cosh(n(t-t_1))}{n \sinh(n(t_2-t_1))} b_n \right) \cos(n\theta) + \sum_{n=1}^{\infty} \left(\frac{1 \cosh(n(t-t_2))}{n \sinh(n(t_1-t_2))} c_n + \frac{1 \cosh(n(t-t_1))}{n \sinh(n(t_2-t_1))} d_n \right) \sin(n\theta) \quad (34)$$

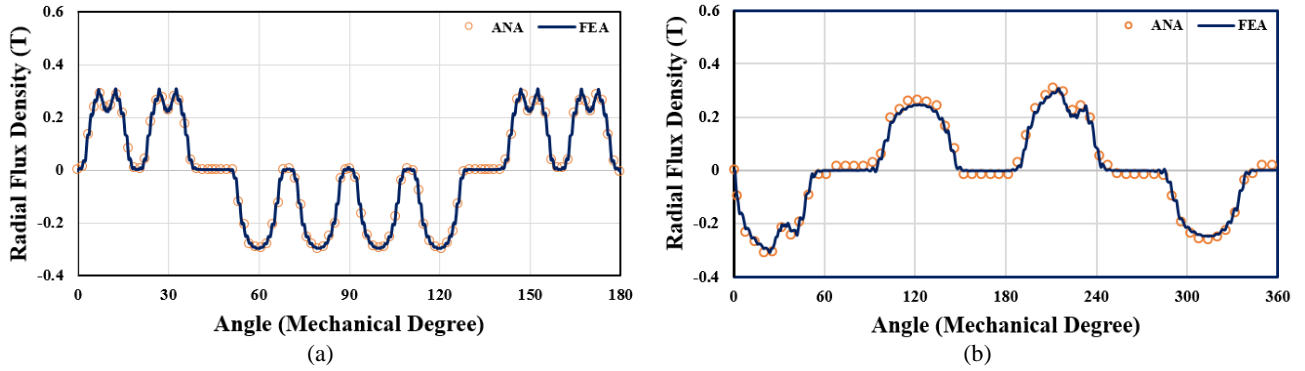


Fig. 8 No load analytical and numerical comparison of radial flux density distribution in a) 4P-18S motor and b) 6P-18S motor.

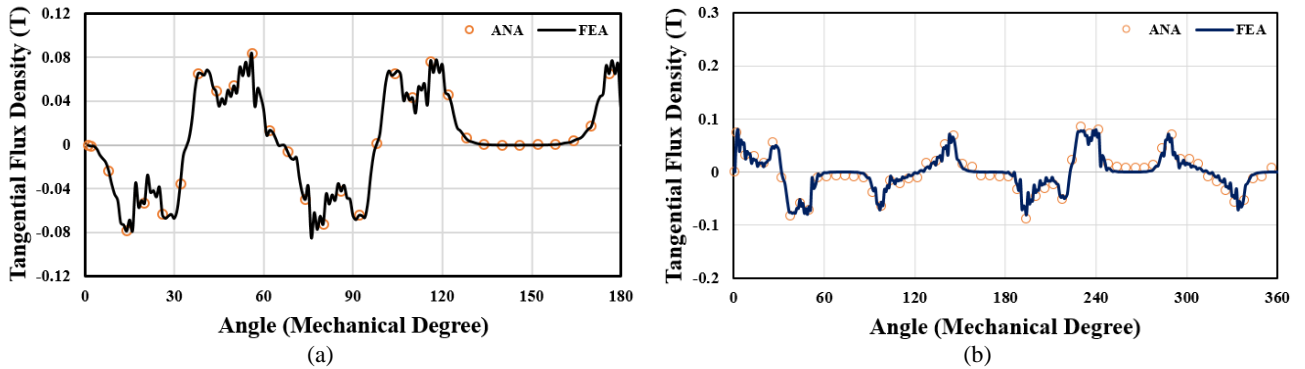


Fig. 9 No load analytical and numerical comparison of tangential flux density distribution in a) 4P-18S motor and b) 6P-18S motor.

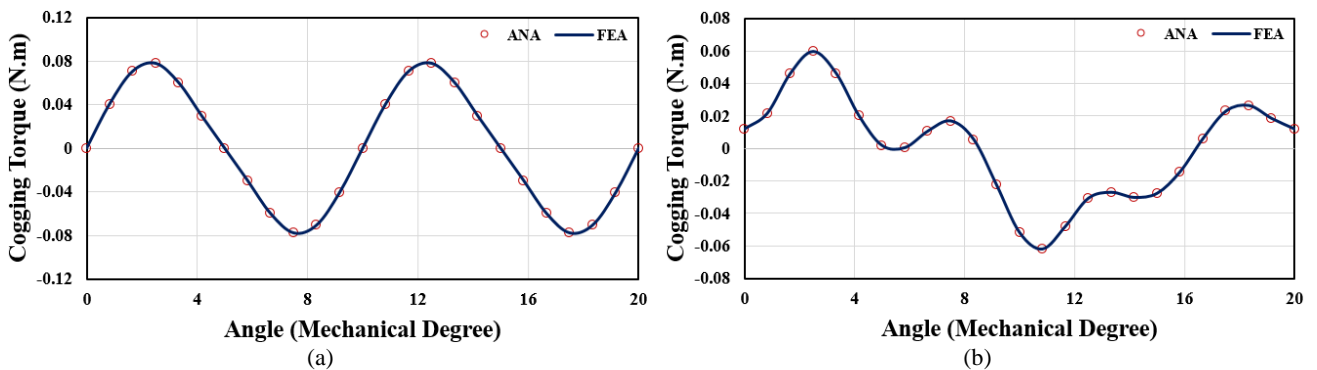


Fig. 10 Open circuit analytical and numerical comparison of cogging torque for a) 4P-18S motor and b) 6P-18S motor.

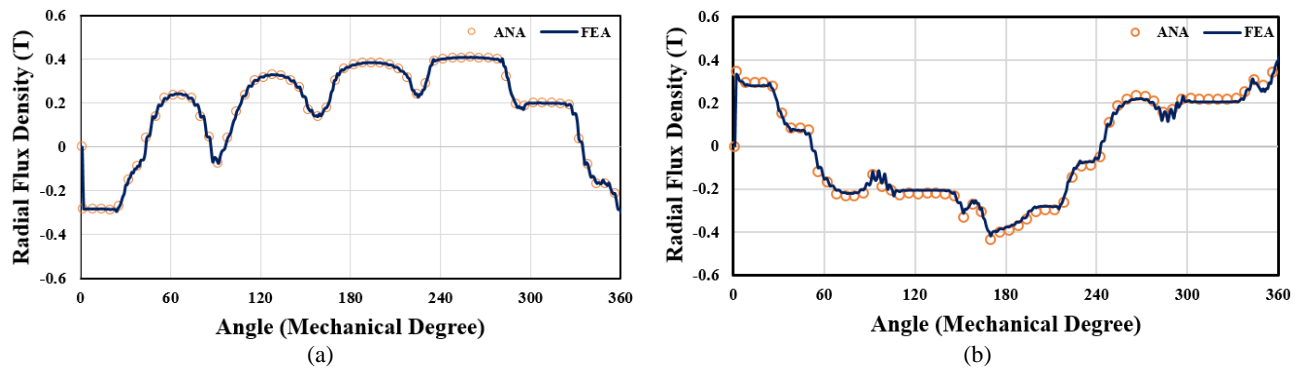


Fig. 11 On load analytical and numerical comparison of radial flux density for a) 4P-18S motor and b) 6P-18S motor.

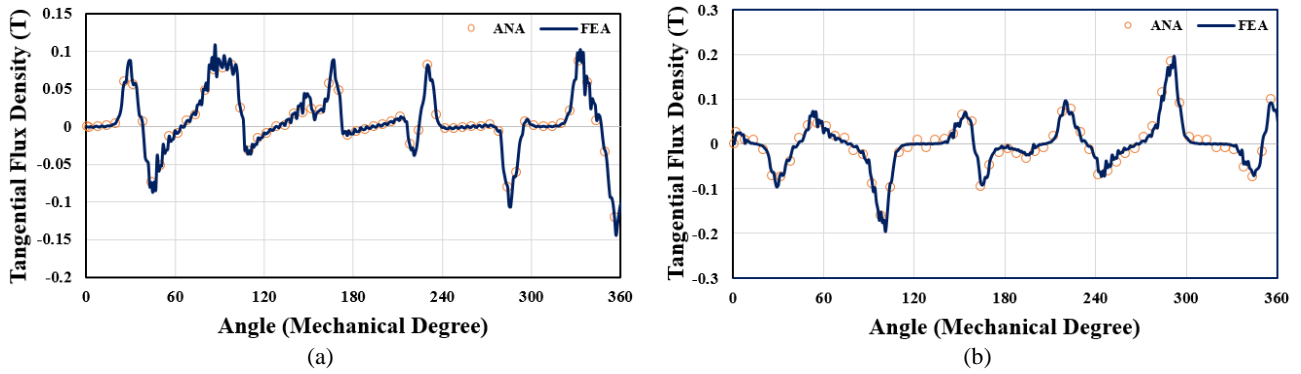


Fig. 12 On load analytical and numerical comparison of tangential flux density for a) 4P-18S motor and b) 6P-18S motor.

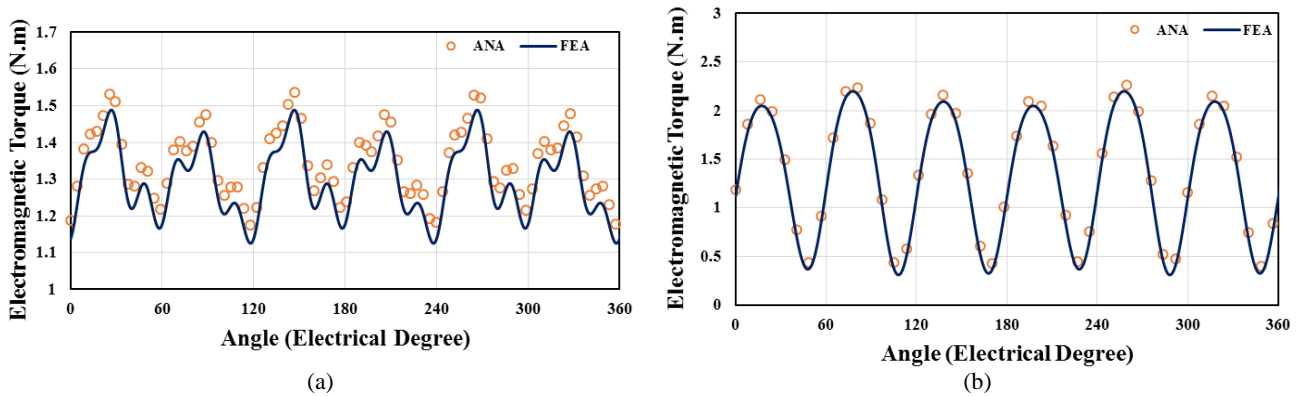


Fig. 13 On load analytical and numerical comparison of electromagnetic torque for a) 4P-18S motor and b) 6P-18S motor.

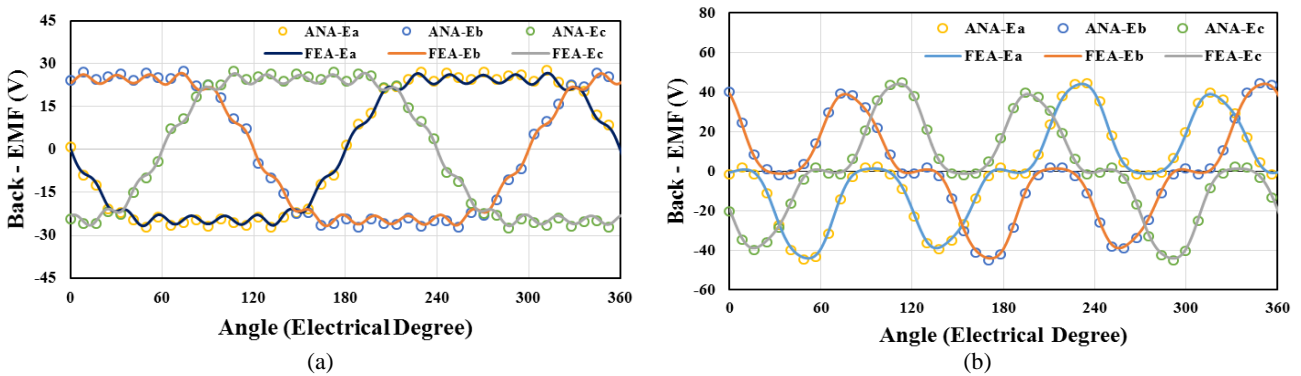


Fig. 14 On load analytical and numerical comparison of back - EMF for a) 4P-18S motor and b) 6P-18S motor.

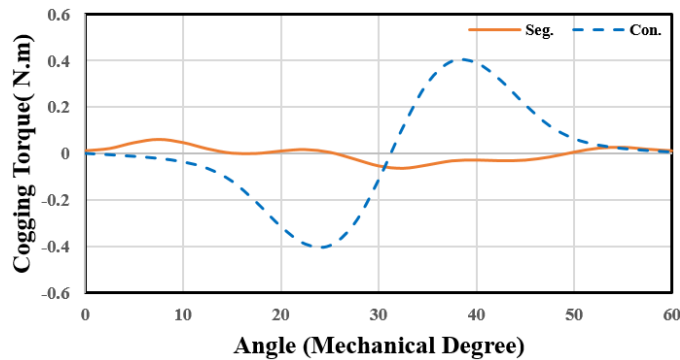


Fig. 15 Cogging torque comparison between 4P-18S conventional (Con.) and segmented (Seg.) motors.

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