# **Controlling the Both DC Boost and AC Output Voltages of a Z-Source Inverter Using Neural Network Controller with Minimization of Voltage Stress Across Devices**

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**Abstract:** This paper presents a method to control both the dc boost and ac output voltages of Z-source inverter using neural network controllers. The capacitor voltage of the Z-source network has been controlled linearly in order to improve the transient response of the dc boost voltage of the Z-source inverter. The peak value of the line to line ac output voltage is used to control and keep the ac outputs to their desired values. A modified space vector pulse-width-modulation method is also applied to control the shoot-through duty ratio for boosting dc voltage. This modified method lets to minimize the dc voltage stress across the inverter switches. The neural network control technique is verified with simulation results and compared with the traditional PI controller responses.

Keywords: Power Converters, Z-Source Inverter, Space Vector PWM, Neural Network.

# 1 Introduction

Power electronic inverters are increasingly being used in modern energy conversion systems, including uninterruptible power supplies, motor drives and active interfaces for localized and distributed generation. Most of these applications would require the inverters to have both voltage-buck and boost capabilities for riding through load current and supply voltage variations [1], [2]. A common way of implementing buck-boost inverters is to cascade a dc-dc converter to either a buck voltage source or boost current source inverter to form a two-stage power conversion solution, but this cascaded topology usually results to increase system complexity and reduces reliability. The Z-source inverter described in [3] overcomes the conceptual and theoretical barriers and limitations for the traditional inverters and provides a novel power conversion concept.

Figure 1 shows the general Z-source inverter (ZSI) structure. The Z-source inverter employs a unique impedance network to couple the inverter main circuit to the dc power supply.

This two-port impedance network consists of a splitinductor  $L_1$  and  $L_2$  and capacitors  $C_1$  and  $C_2$  connected in X shape [4]. In Fig. 1, the three-phase Z-source inverter bridge has nine permissible switching states (vectors) unlike the three-phase V-source inverter that has eight. The V-source inverter has six active vectors and two null vectors. However, the three-phase Z-source inverter bridge has one extra zero state when the both devices of any leg are gated on. This third zero state is called the shoot-through state, which can be generated by seven different ways: shoot-through via any one phase leg, combinations of any two phases leg, and all three phase legs. The Z-source network makes the shoot-through zero state possible. This shoot-through zero state provides the unique buck-boost feature to the inverter [5]-[7].

All the traditional pulse-width-modulation (PWM) schemes can be used to control the Z-source inverter and their theoretical input-output relationships still hold. The carrier-based PWM control methods are simple boost control method, maximum boost control method [8], and maximum constant boost control method [9] respectively. Since space vector PWM techniques are more suitable to control the shoot-through duty ratio in the Z-source inverter, it has been developed in recent papers. This paper aims to achieve good performance of both the dc boost and the ac output voltage control of the Z-source inverter using neural network controllers and comparing the obtained results with traditional PI controller.

An algorithm is proposed to linearly control of the capacitor voltage in order to improve the transient response of the dc boost voltage.

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Fig. 1 General structure of the Z-source inverter.

The peak value of line to line ac output voltage is used to control the output voltage and keep it to its reference value. A modified space vector PWM is also used to control effectively the shoot-through duty ratio for boosting dc capacitor voltage. Using this modified method, the dc voltage stress across the inverter switches is also minimized.

## 2 Designing of Impedance Network Parameters

Since in voltage source and current source inverters, PWM method or other switching methods are applied without any shoot-trough state, then the capacitor voltages,  $V_{C1}$  and  $V_{C2}$ , are constants and equal to  $V_{dc}$ . Therefore, in this case, the inductances  $L_1$  and  $L_2$  have a dc current. But in Z source inverters, these inductances are used to limit the current ripples and increase voltage level in non-shoot-through states. In shoot-through states, currents of these inductances increase linearly and their voltages,  $V_{L1}$  and  $V_{L2}$ , are equal to the capacitor voltages. In non-shoot-through states, inductance currents decrease and inductance voltages are the differences between  $V_{dc}$  and capacitor voltages. The mean current through the inductances of the Zsource network is equal to the mean current of diode.

$$\overline{I}_{L} = \frac{S_{Load}}{V_{dc}} = \frac{\sqrt{3} V_{Load} I_{Load}}{V_{dc}}$$
(1)

where  $S_{Load}$  is total output power,  $V_{Load}$  is output line voltage and  $I_{Load}$  is load current. Due to the special characteristic of Z-source network, appropriate value must be chosen for inductances. Otherwise, the inverter may have undesired functions. Many researches have been done to find the optimal value for these inductances. In this paper, the value for inductances are chosen in order to limit the current ripples in maximum output power. Fig. 2 shows the current variation of inductances, for a switching period,  $T_s$ , in steady state. By linearization these equations for a period of  $\Delta t$ ,  $V_L$ and  $I_C$  can be written as follow:

$$\overline{V}_{L} = L \frac{\Delta I_{L}}{\Delta t}$$
(2)

$$\overline{I}_{c} = C \frac{\Delta V_{c}}{\Delta t}$$
(3)







Fig. 3 Capacitor voltage variations during a switching cycle.

Considering the shoot-trough period, as shown in Fig. 2, and having the same voltages for the inductances and the capacitances in this state, the values for the inductances of Z network can be obtained as follows:

$$L \ge \frac{D_{sh} V_{c}}{2f_{s} \Delta I_{L}}$$
(4)

where  $\overline{V}_c$  is the mean value of capacitor voltage,  $\Delta I_L$  is the inductance current ripples in maximum power,  $D_{sh}$  is shoot-through duty ratio and  $f_s$  is the switching frequency. The mean value of the capacitors voltage can be obtained as follows:

$$\bar{V}_{c} = \frac{1 - (T_{sh}/T_{s})}{1 - (2T_{sh}/T_{s})} V_{dc}$$
(5)

The maximum current ripple is set to 5% in [10], 20% in [11] and 30% in [12]. In this paper, the maximum current ripple for inductances is set to 10%. The role of the capacitors in Z-source network is to reduce the current ripples and to ensure a soft dc voltage at the inverter input. By applying the shoot-through states, the capacitors,  $C_1$  and  $C_2$  charge the inductances,  $L_1$  and  $L_2$ , which results to decrease linearly their voltages. In this state, the capacitor currents are equal to inductance currents. During non-shoot-trough state, the

voltages of the capacitors increase linearly. Fig. 3 shows the variation of the capacitor voltage during a switching cycle  $T_s$ . Regarding to this figure, and using the Eq. (3), the capacitor's values  $C_1$  and  $C_2$  can obtained as below:

$$C \ge \frac{D_{sh} I_{L}}{2f_{s} \Delta V_{c}}$$
(6)

where  $D_{sh}$  is shoot-through duty ratio,  $\overline{I}_L$  is the mean value of inductance current,  $f_s$  is the switching frequency and  $\Delta V_c$  is the capacitor voltage ripples in maximum power. It must be said that the maximum voltage ripple is consider between 1% to 5% in [10] and [12]. In this paper this ripple is limited to 1%.

# 3 Modified Space Vector PWM

Space vector PWM switching techniques have been widely used in industrial inverter because of their lower current harmonics and higher modulation index [13]. The SVPWM is more suitable to control the shootthrough time in the Z-source inverter. The eight space vectors V0-V7, illustrated in Fig. 4, are used in SVPWM, where  $V_1$ - $V_6$  are active vectors, and  $V_0$  and  $V_7$  are null vectors. If the reference voltage vector,  $V_{\text{ref}}$ is located between the arbitrary vector  $V_i$  and  $V_{i+1}$ , the reference voltage vector is divided into two adjacent voltage vectors ( $V_i$  and  $V_{i+1}$ ) and null vectors ( $V_0$  and  $V_7$ ). In a sampling interval  $T_s$ , voltage vectors  $V_i$  and  $V_{i+1}$  are applied during  $T_1$  and  $T_2$ , respectively, and the null vectors are applied during  $T_0=T_s-(T_1+T_2)$ . Consequently, the reference voltage vector V<sub>ref</sub> can be obtained as follows [14]:

$$\vec{\mathbf{V}}_{\text{ref}} = T_1 \, \vec{\mathbf{V}}_{\text{i}} + T_2 \, \vec{\mathbf{V}}_{\text{i+1}} + T_0 (\vec{\mathbf{V}}_0 \text{ or } \vec{\mathbf{V}}_7) \tag{7}$$

The time intervals  $T_1$  and  $T_2$  can be obtained as [15]

$$T_{i} = \sqrt{3} \frac{\left|\vec{V}_{ref}\right|}{\hat{V}_{i}} T_{s} \sin(n\frac{\pi}{3} - \alpha)$$
(8)

$$T_{2} = \sqrt{3} \frac{\left| \vec{\nabla}_{ref} \right|}{\hat{V}_{i}} T_{s} \sin(\alpha - \frac{(n-1)}{3}\pi)$$
(9)

where  $\alpha$  is the angle between the reference voltage vector,  $V_{ref}$  and voltage vector  $V_1$ , and n is the number of sector in which reference vector is located.

The symmetrical pulse pattern of voltage vectors  $V_1$ ,  $V_2$  and zero vectors  $V_0$  and  $V_7$  during one sampling period at the modified space vector PWM is illustrated in Fig. 5. Unlike the traditional SVPWM, the modified SVPWM has an additional shoot-through period  $T_{sh}$  besides time intervals  $T_1$ ,  $T_2$  and  $T_0$ . The zero voltage period  $T_0$  should be modified for generating the shoot-through time interval  $T_{sh}$ . The shoot-through time interval is evenly assigned to each phase with  $T_{sh}/6$ , which the active state time intervals  $T_1$  and  $T_2$  are not changed.



Fig. 4 Basic space vector PWM.

#### 4 Minimization of Voltage Stress across Devices

In order to obtain the voltage gain of the modified SVPWM, switching pattern, which is shown in Fig. 5, is used. As it can be seen in this figure, the time interval of the second null vector,  $V_7$ , is equal to  $T_0/4-2T_{sh}/6$ . Since this interval must be positive and more than zero, therefore the shoot trough interval is limited to  $3T_0/4$ .

$$T_{sh} = \frac{3}{4}T_{0} \implies \frac{T_{sh}}{T_{s}} = \frac{3}{4}\frac{T_{0}}{T_{s}}$$
$$= \frac{3}{4}\left(\frac{T_{s} - (T_{1} + T_{2})}{T_{s}}\right) = \frac{3}{4}\left(1 - \frac{(T_{1} + T_{2})}{T_{s}}\right)$$
(10)

Using the Eq. (8) and (9), the total time interval of active switching,  $T_a$ , in section 1, can be calculated as bellow:

$$n = 1 \implies T_a = T_1 + T_2 = \sqrt{3} \frac{\left| \vec{V}_{ref} \right|}{\hat{V}_i} T_s \sin(\alpha + \frac{\pi}{3}) \qquad (11)$$

As it can be seen, this active time interval,  $T_a$ , varies during any section of space vectors. This variation is regular during any  $\pi/3$  interval. Therefore in order to obtain the voltage gain, it is enough to calculate the average of  $T_a$  in section 1, between 0 and  $\pi/3$  [16]:



Fig. 5 Switching pattern for both traditional SVPWM and modified SVPWM.

$$(T_{a})_{avg} = \frac{1}{(\pi/3)} \int_{0}^{\frac{\pi}{3}} \sqrt{3} \frac{\left|\vec{V}_{ref}\right|}{\hat{V}_{i}} T_{s} \sin(\alpha + \frac{\pi}{3}) d\alpha$$
  
$$= \frac{3\sqrt{3}}{\pi} T_{s} \frac{\left|\vec{V}_{ref}\right|}{\hat{V}_{i}}$$
(12)

Since the value of reference voltage,  $\bar{V}_{ref}$  is equal to maximum value of the output phase voltage, hence the average of  $T_a$  can be expressed as the following:

$$(T_{a})_{avg} = \frac{3\sqrt{3}}{\pi} T_{s} \frac{\hat{V}_{ac}}{\hat{V}_{i}} = \frac{3\sqrt{3}}{2\pi} T_{s} \frac{\hat{V}_{ac}}{\hat{V}_{i}/2}$$
(13)

and then:

$$\frac{\hat{V}_{ac}}{\hat{V}_{i}/2} = M \implies (T_{a})_{avg} = \frac{3\sqrt{3}M}{2\pi}T_{s}$$

$$\Rightarrow \quad \frac{T_{sh}}{T_{s}} = \frac{3}{4}\left(1 - \frac{(T_{a})_{avg}}{T_{s}}\right) = \frac{3}{4}\left(1 - \frac{3\sqrt{3}M}{2\pi}\right) \qquad (14)$$

$$\Rightarrow \quad \frac{T_{sh}}{T_{s}} = \frac{3}{4}\left(\frac{2\pi - 3\sqrt{3}M}{2\pi}\right)$$

where M is the modulation index. The value of boost factor, B, based on the modulation index can be deduced as follows:

$$B = \frac{1}{1 - (2T_{sh}/T_s)} = \frac{4\pi}{9\sqrt{3}M - 2\pi}$$
(15)

Therefore the voltage gain, G of the modified SVM can be written as below:

$$G = MB = \frac{\hat{V}_{ac}}{V_{dc}/2} = \frac{4\pi M}{9\sqrt{3}M - 2\pi}$$
(16)

Also for given voltage gain, G, the modulation index is:

$$M = \frac{2\pi G}{9\sqrt{3}G - 4\pi}$$
(7)

In Fig. 6, the voltage gain of the modified SVM based on the modulation index is shown.

## 5 Control Algorithm of the DC Boost Voltage

The dc-link voltage  $V_i$  is a square waveform due to the shoot-through states. During the non-shoot-through states, the dc-link voltage is in its peak value,  $\hat{V}_i$ , and it is zero in the shoot-through states. Therefore, the peak value of dc-link voltage is not suitable for using as a feedback signal. Most of the papers have used the Zsource capacitor voltage as a feedback signal, and have controlled the capacitor voltage in a constant value. Regarding to Eq. (5), the capacitor voltage V<sub>C</sub> is related to the dc-link voltage of the inverter and can be boosted by controlling the shoot- through duty ratio. Fig. 7 shows the relationship between  $V_C/V_{dc}$  and the shoot-through time duty ratio  $T_{sh}/T_s$ . As the relationship has nonlinear characteristics, the shoot-through time cannot linearly control the capacitor voltage. The nonlinearity may deteriorate the transient response of the capacitor voltage. In order to overcome this problem, in this paper an algorithm is used for controlling linearly the capacitor voltage using neural networks controller as shown in Fig. 8. The output of the neural network controller of  $V_C$  is called K and it can be defined as [13]

$$K = \frac{V_c}{V_{dc}}$$
(18)

In order to have  $V_C$  greater than  $V_{dc}$ , the parameter K must be greater than 1. Using Eq. (5), the shoot-through period,  $T_{sh}$  can be calculated from the following equation:



Fig. 6 Relationship between voltage gain and modulation index, M in modified space vector PWM.



**Fig. 7** Relationship between capacitor voltage and voltage stress and shoot-through duty ratio.



Fig. 8 Capacitor voltage controller using neural network.

$$T_{sh} = \frac{K - 1}{2K - 1} T_s$$
(19)

As the capacitor voltage is linearly controlled by K, a good transient performance of capacitor voltage can be obtained.

# 6 Control Algorithm of the AC Output Voltage

Figure 9 shows the block diagram of the voltage control of Z-source inverter, which consists in the dc boost voltage control unit, using the linearization method and the ac output voltage control unit. As shown in Fig. 9, the peak value of the output voltage is used to control the ac output voltage. After detecting the three-phase line voltages, the three-phase voltages are transformed into two-axis voltages in the stationary reference frame V<sub>ds</sub> and V<sub>qs</sub>, and then the peak output voltage V<sub>sp</sub> can be derived as below [13]:

$$V_{sp} = \sqrt{(V_{ds}^{s})^{2} + (V_{qs}^{s})^{2}}$$
(20)

The output of the neural networks controller  $(V_{sp})$  forms the reference voltage for modified SVPWM. The phase angle  $\theta_e$  determines the sector in which the reference voltage vector is located, and six PWM signals are generated from the reference voltage and shoot-through time interval in each sampling period.

#### 7 Neural Network Controller Design

Neural networks have been applied very successfully in identification and control of many dynamic systems. The universal approximation capabilities of the multilayer perceptron have made it a popular choice for modeling nonlinear systems and for implementing general-purpose nonlinear controllers [17]. In [17] a neural network has been used to determine the parameters K<sub>P</sub> and K<sub>I</sub> of a PI controller to control only the dc boost voltage in wide range. As the inverter's output voltages are the final outputs of the system, and it is more important to control these outputs, in this paper, two neural network predictive controllers have been used in parallel, to predict and control the both dc boost voltage and ac output voltages of the Z-source inverter.

The proposed neural network predictive controller uses a neural network model of a nonlinear plant to predict future plant performance. The controller then calculates the input signal that will optimize plant performance over a specified future time horizon. The first step in model predictive control is to determine the neural network plant model (system identification). Next, the plant model is used by the controller to predict future performance. The neural network plant model is trained offline, in batch form, using the Backpropagation training algorithms. The controller applies an algorithm, which requires significant amount of



Fig. 9 Block diagram for voltage control of the Z-source inverter.

online computations, to produce the optimal input signal at each sample time. The following subsection describes the system identification process. Then it is followed by a description of the optimization process [15].

# 7.1 System Identification

The first stage of model predictive control is to train a neural network to represent the forward dynamics of the plant. The prediction error between the plant output and the neural network output is used as the neural network training signal. The process is represented in Fig. 10. The neural network plant model uses previous inputs and previous plant outputs to predict future values of the plant outputs. The structure of the neural network plant model is given in the Fig. 11. This network has been trained offline in batch mode, using training samples collected during the plant operations. In this paper the Levenberg-Marquardt training algorithm (trainlm) has been used.

As it can be seen in Fig. 11, the neural network has one hidden laver. The number of neurons in the hidden layer of the plant model network for the both dc boost and ac output voltage controllers is equal to 20. The number of the two tapped delay lines coming into the plant model for both inputs and outputs is equal to 2. The sampling Interval at which the program collects data from the Simulink plant model is 1 millisecond. The number of training samples generated for training, validation, and test sets is 10000. The minimum and maximum plant input for the dc boost voltage controller are 1 and 3 and for the ac output voltage controller is 0 and 50 respectively. The random plant input is a series of steps of random height occurring at random intervals. These fields set the minimum and maximum height and interval. The minimum and maximum value of time interval is 0.1 and 0.2 seconds respectively. The number of iterations of plant training to be performed (training epochs) is 100.



Fig. 10 Model predictive control process.



Fig. 11 The structure of the neural network plant model.

## 7.2 Neural Network Predictive Controller Design

The model predictive control method is based on the receding horizon technique [18]. The neural network model predicts the plant response over a specified time horizon. The predictions are used by a numerical optimization program to determine the control signal that minimizes the following performance criterion over the specified horizon.

$$J = \sum_{j=N_1}^{N_2} (y_r(t+j) - y_m(t+j))^2 + \rho \sum_{j=1}^{N_u} (u'(t+j-1) - u'(t+j-2))^2$$
(21)

Where  $N_1$ ,  $N_2$  and  $N_u$  define the horizons over which the tracking error and the control increments are evaluated. The variable u' is the tentative control signal,  $y_r$  is the desired response, and  $y_m$  is the network model response. The value of  $\rho$  determines the contribution that the sum of the squares of the control increments has on the performance index.

Fig. 12 illustrates the neural network controller structure. The controller consists of the neural network plant model and the optimization block. The optimization block determines the values of u' that minimize Jacobian matrix J, and then the optimal u is applied to input of the plant. The Jacobian matrix contains first derivatives of the network errors with respect to the weights and biases. The controller block is implemented in Simulink environment. The cost horizon N<sub>1</sub> is fixed at 1. The cost horizon N<sub>2</sub> that is the number of time steps over which the prediction errors are minimized, is equal to 5 and 8 for the dc boost and ac output voltage controllers respectively.



Fig. 12 Neural network predictive controller structure.

The control horizon  $N_u$  is fixed to 2 for the both controllers. The control weighting Factor  $\rho$  which multiplies the sum of squared control increments in the performance function is 0.02 and 0.04 for the dc boost and ac output voltage controllers respectively. The parameter  $\alpha$  is used to control the optimization. It determines how much reduction in performance is required for a successful optimization step. It is equal to 0.001 for the both controllers. The number of iterations of the optimization algorithm to be performed at each sample time is 2 for the both controllers. Also the linear minimization routine srchbac (backtracking search routine) has been used by the optimization algorithm.

# 8 Simulation Results

In this part of paper, the values of the inductances and the capacitors of the impedance network are calculated, based on the relations given in section 2. It must be mentioned that the load of the Z-source inverter is a three phases RL with 2 kW nominal power, and power factor of 0.8. Line to line nominal voltage is 400V and the output frequency is set to 50 Hz. Also a 100V dc voltage source supplies the input of the Zsource inverter. The switching frequency of the modified SVPWM is set to 5 kHz. Note that the parameters of the impedance network are calculated for nominal power, but the system is simulated for different conditions. The output nominal current of the Z-source inverter can be calculated as below:

$$P_{\text{Load}} = \sqrt{3} V_{\text{Load}} I_{\text{Load}} \cos \phi \implies I_{\text{Load}} = 3.6 \text{ A}$$
(22)

With 400V line to line output voltage, the value of the amplitude of the output voltage is given as the following:

$$\hat{V}_{ac} = \frac{V_{L-L}\sqrt{2}}{\sqrt{3}} = \frac{400\sqrt{2}}{\sqrt{3}} = 326.6 \text{ V}$$
(23)

Therefore by using the modified SVPWM, the value of voltage gain, G, of the Z-source inverter becomes:

G = MB = 
$$\frac{V_{ac}}{V_{dc}/2}$$
 = 6.53 =  $\frac{4\pi M}{9\sqrt{3}M - 2\pi}$  (24)

Thus the value for modulation index, M for this switching method is equal to 0.46.

Using Eq. (14), the value of nominal ratio of shoot-trough can be written as below:

$$D_{sh} = \frac{T_{sh}}{T_s} = \frac{3}{4} \left( \frac{2\pi - 3\sqrt{3}M}{2\pi} \right) = 0.4646$$
(25)

Using this shoot-trough duty ratio, the mean value of capacitor voltage can be calculated as the following:

$$\bar{V}_{c} = \frac{1 - (T_{sh}/T_{s})}{1 - (2T_{sh}/T_{s})} V_{dc} = 756 V$$
(26)

Also by using Eq. (1), the mean value for inductance current can be deduced as below:

$$\overline{I}_{L} = \frac{S_{Load}}{V_{dc}} = \frac{\sqrt{3} V_{Load} I_{Load}}{V_{dc}} = 25 \text{ A}$$
(27)

By using Eq. (4) and considering a maximum of 10% ripple for inductance current, the value of inductances in Z network can be taken out as the following:

$$L \ge \frac{D_{sh} V_{c}}{2f_{s} \Delta I_{L}} = \frac{0.4646 \times 756}{2 \times 5000 \times (0.1 \times 25)} \Longrightarrow L \ge 1.4 \,\text{mH}$$
(28)

Also by using Eq. (6) and considering a maximum of 1% ripple for capacitor voltage, the value of capacitors in Z-source network can be calculated as below:

$$C \ge \frac{D_{sh} \overline{I}_{L}}{2f_{s} \Delta V_{c}} = \frac{0.4646 \times 25}{2 \times 5000 \times (0.01 \times 756)}$$
$$\implies C \ge 153 \,\mu\text{F}$$
(29)

The calculated values for the inductances and capacitances are the minimum values. In order to have fewer ripples, two 2 mH inductances and two 470  $\mu$ F capacitors are selected for Z-source network.

Fig. 13 shows the transient response of the value of line to line peak voltage of the Z source inverter output using PI controllers. As can be seen from Fig. 13, the voltage  $V_{sp}$  arrives to its reference, 200V, in 0.2 second. The transient response of the capacitor voltage using PI controllers has been shown in Fig. 14. As it is shown, this voltage arrives to 236 V after 0.5 second and follows its reference.

Fig. 15 shows the transient response of the value of line to line peak voltage of the Z source inverter output. As discussed before, a predictive neural network controller is used. As it is shown, the voltage  $V_{sp}$  arrives to its reference, 200V, in less than 0.05 second, and follows it very well. A filtered line to line output voltage of the Z-source inverter is presented in Fig. 16. As it can be seen, the maximum value of line to line output voltages is shown in Fig. 17. This voltage arrives to 236 V after 0.2 second and follows its reference very well.



Fig. 13 Peak ac line to line output voltage response using PI controller.



Fig. 14 Z-source network capacitor voltage response using PI controller.



Fig. 15 Peak ac line to line output voltage response using neural network controller.



Fig. 16 line to line output voltage response using neural network controller.

During the shoot-trough states the inverter switches have a zero voltage. During active states, the value of applied dc voltage to the inverter switches  $\hat{V}_i$  can be calculated as the following:



Fig. 17 Z-source network capacitor voltage response using neural network controller.



Fig. 18 line to line switched voltage of Z-source inverter.

$$\hat{V}_{i} = \frac{1}{1 - (2T_{sh}/T_{s})} \times V_{dc}$$

$$= \frac{1}{1 - (2 \times 0.35)} \times 100 = 357 \text{ V}$$
(30)

The line to line switched voltage of Z-source inverter is given in Fig. 18. It can be observed that the instantaneous amplitude arrives to 360 V.

Figure 19 shows the variation of the peak value of line to line output voltage using PI controllers when the reference value of  $V_{sp}^*$  varies from 180 V to 250 V. The variation of the capacitor voltage in order to provide the considering output voltage using PI controllers has been shown in Fig. 20. Fig. 21 shows the variation of the peak value of line to line output voltage when the reference value of  $V_{sp}^*$  varies from 180 V to 250 V. Also the variation of line to line output voltage from 180 V to 250 V is shown in Fig. 22. One of the capacitor voltages is presented in Fig. 23. In order to provide the output voltage, this voltage varies from 208 V to 308 V.

# 9 Conclusion

In this paper, structure, equivalent circuit and main equations of a Z-source inverter are studied. The dc-link voltage and the ac output voltages are controlled simultaneously. At first stage, in order to have a good performance, the values of inductances and capacitors are calculated by linearization of the inductances currents and capacitors voltages. Then a modified space vector PWM is presented to perform the inverter switching. Since the peak value of dc-link voltage is related to capacitors voltages, by controlling the capacitor voltages, the control of dc-link voltage is performed. Also, the shoot-through ratios are determined by this linearization of the capacitor voltage control. Moreover, in this paper, the peak value of the line to line ac output voltage is controlled by using a modified switching algorithm. This algorithm lets to minimize the dc voltage stress across the inverter switches. As it is shown by simulation, PI controllers cannot offer good performances; in this paper two predictive neural network controllers are applied to ameliorate the dynamic performance of simultaneous control of dc boost voltage and ac output voltages. Simulation results show a higher performance, rapid response and fewer ripples in both input and output sides of inverter.



Fig. 19 variation of the peak value of line to line output voltage from 180 V to 250 V using PI controller.



**Fig. 20** Variation of capacitor voltages from 208 V to 308 V using PI controller.



Fig. 21 variation of the peak value of line to line output voltage from 180 V to 250 V using NN controller.



**Fig. 22** Variation of the line to line ac output voltage from 180 V to 250 V using NN controller.



Fig. 23 Variation of capacitor voltages from 208 V to 308 V using NN controller.

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