## Islanding Detection of Synchronous Machine-Based DGs using Average Frequency Based Index

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**Abstract:** Identification of intentional and unintentional islanding situations of Dispersed Generators (DGs) is one of the most important protection concerns in power systems. Considering safety and reliability problems of distribution networks, an exact diagnosis index is required to discriminate the loss of the main network from the existing parallel operation. Hence, this paper introduces a new islanding detection method for synchronous machine–based DGs. This method uses the average value of the generator frequency to calculate a new detection index. The proposed method is an effective supplement of the Over/Under Frequency Protection (OFP/UFP) system. The analytical equations and simulation results are used to assess the performance of the proposed method under various scenarios such as different types of faults, load changes and capacitor bank switching. To show the effectiveness of the proposed method, it is compared with the performance of both ROCOF and ROCOFOP methods.

**Keywords:** Islanding detection, Non-detection zone, Passive methods, Synchronous machine-based Distributed Generation (DG).

### 1 Introduction

Nowadays, DG has been broadly used in distribution power systems. It can supply electricity secure to customers, be active in a deregulation of the electricity increase the reliability decrease market. and environmental concerns [1, The islanding 2]. identification for the connection of distributed generators to distribution networks is an important issue. According to IEEE standard 1547-2003, the islanding condition is defined as a situation in which a part of an electric power system is solely energized and separated from the rest of the system [3]. Failure to islanding detection can lead to several negative impacts to the generators and connected loads, as follows [4, 5]:

- 1. The islanded grid cannot control its frequency and voltage. This earns result in equipment damages.
- 2. This condition may cause safety hazards to utility workers and customers.

Therefore, the islanding situation must be detected as soon as possible. Many islanding detection methods

Iranian Journal of Electrical & Electronic Engineering, 2013.

have been proposed, which can be classified into two main categories. Remote methods, such as power line communication [6] and supervisory control and data acquisition [7] methods. They do not have Non-Detection Zone (NDZ) and are more reliable than the local methods but more expensive. NDZs are defined as a loading condition for which an islanding detection method would fail to operate in a timely manner [8].

The local methods can be classified into two major groups: active and passive methods. According to the active methods, islanding is detected based on adding a perturbation signal into the system. The perturbation signals in parallel operation have no significant effect; but in the case of the loss of main grid, these signals are detected. Some of active methods, which have been recently introduced, include positive feedback for active and reactive power loops in governor and excitation system of synchronous DGs [9], injection a negative sequence of current through the interface Voltage-Sourced Converter (VSC) [10], Sandia frequency and voltage shift methods [11] and harmonic amplification factor, which is based on the voltage change at the Point of Common Coupling (PCC) [4].

Passive methods are based on measuring local parameters of DG and comparing it with preset value. Passive methods, which have been proposed, include Over/Under Frequency/Voltage Protections (OFP/UFP and OVP/UVP) and rate of change of frequency over the time [12-14]. Vector surge relay is the other

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solution, which has been explained in [15]. Some of passive methods use two parameters simultaneously, e.g., rate of change of frequency over the active power [16] and rate of change of phase angle difference [17]. For inverter-based DGs, two new islanding detection methods based on using DC voltage and reference power of the DG has been considered in [8] and [18], respectively. Artificial Neural Network (ANN), Kalman Filtering (KF), estimation based methods, application of adaptive fuzzy and duffing oscillators are the other major methods, which are very efficient to detect the islanding situation. These methods, in both inverterbased and synchronous-machine based DGs, have been investigated in [19-24]. Although these methods are very effective but also have a lot of complexity. Classification-based islanding detection schemes, which have been recently developed, are passive methods reviewed in [25, 26]. The combination of different types of islanding detection techniques which are known as hybrid methods have been introduced in [5, 27, 28]. In [5, 27], the combination of both active and passive methods have been investigated whereas [28] expresses the combination of both communication and passive methods. Although the active methods have smaller NDZ than the passive methods but degrade the power quality of the system [18].

Most of the passive methods, monitoring only one parameter, have a large NDZ, while simultaneous monitoring of two parameters further decreases the NDZ of passive methods and have a small NDZ [16, 17]. In this paper, the average value of the frequency is used to reduce NDZ of OFP/UFP. The proposed method uses only one parameter to detect islanding situation and from the viewpoint of reducing the NDZ, it has the same performance and capability as two parameters monitoring methods.

The paper is organized as follows: the proposed method is described in section 2. Section 3 shows the results of simulations and discussions. In section 4 comparison of proposed method with two passive methods is carried out and finally section 5 represents the conclusions.

### 2 Proposed Method

### 2.1 Frequency Deviation for Grid-Connected and Islanded Modes

For a Synchronous Distributed Generator (SDG), which is operating in parallel with a utility main network and feeds the local load, the following swing equation is defined [30, 31]:

$$\frac{2H}{\omega_b}\frac{d\omega}{dt} = P_m - P_e - D\omega \tag{1}$$

where, H,  $\omega_{b}$ , D,  $P_{m}$  and  $P_{e}$  are generator inertia

constant, synchronous speed of DG, damping coefficient, mechanical and electrical power of the DG,



Fig. 1 Synchronizing coefficient in different conditions.

respectively. The swing equation must be solved for two different modes; parallel operation with main network and loss of main network.

1) Grid-Connected Mode of SDG

In this mode, based on the manipulation of Eq. (1), presented in appendix, the following equation can be written:

$$\frac{2H}{\omega_b} \frac{d^2 \Delta \delta}{dt^2} + D \frac{d \Delta \delta}{dt} = -P_{\text{max}} \cos(\Delta \delta)$$
(2)

where, the term  $P_{\max} \cos(\Delta \delta)$  is known as synchronizing coefficient. This parameter has a very important role in the dynamic behavior of the synchronous generator. Fig. 1, shows the values of the synchronizing coefficient in different conditions of the power system. By solving Eq. (2) and considering  $\Delta \delta(0) = \Delta \delta_0$  and  $\Delta \omega(0) = 0$  as initial conditions, following responses for frequency and rotor angle deviations can be obtained:

$$\Delta\delta(t) = \frac{\Delta\delta_0}{\sqrt{1-\zeta^2}} e^{-\zeta\omega_n t} \sin(\omega_d t + \theta)$$
(3)

$$\Delta f(t) = \frac{-\omega_n \Delta \delta_0}{2\pi \sqrt{1-\zeta^2}} e^{-\zeta \omega_n t} \sin(\omega_d t)$$
(4)

where, we have:

$$\omega_n = \sqrt{\frac{P_{\max}\cos(\delta_0).\omega_b}{2H}}$$
(5)

$$\varsigma = \frac{D}{2} \sqrt{\frac{\omega_b}{2H.P_{\text{max}} \cos(\delta_0)}}$$
(6)

$$\omega_d = \omega_n \sqrt{1 - \varsigma^2} \tag{7}$$

$$\theta = \cos^{-1}(\zeta) \tag{8}$$

Considering Eq. (3) and Eq. (4), it can be said that the frequency and rotor angle deviations have a damped sinusoidal waveform and after a while the amplitude of these signals will be equal to the zero.

### 2) Loss of Main Grid:

In this mode, the response of the frequency to a loss of main grid is determined. In the islanding situation, the transmitted power between DG and main network reaches to zero (see Fig. 1). It means that the synchronizing coefficient  $P_{max} \cos(\Delta \delta)$  must be equal to zero. Therefore, in Eq. (2), we have:

$$\frac{2H}{\omega_b}\frac{d^2\Delta\delta}{dt^2} + D\frac{d\Delta\delta}{dt} = 0$$
<sup>(9)</sup>

By solving Eq. (9) with  $\Delta\delta(0) = \Delta P \omega_b / 2H$  and  $\Delta\omega(0) = 2\pi\Delta P / D$  as initial conditions, the following response for frequency deviations can be obtained:

$$\Delta f(t) = \frac{\Delta P}{D} \left( 1 - e^{-2\varphi \omega_s t} \right) \tag{10}$$

Here,  $\Delta P$  is the active power imbalance. By comparing Eq. (4) and Eq. (10), it can be seen that frequency deviations in grid-connected and islanded modes are different. When the real power mismatches ( $\Delta P$ ) causes transients in the islanded portion, the frequency of DG increases or decreases. Therefore, the aforementioned frequency deviations can be used to detect the islanding condition.

### 2.2 Fundamentals of Proposed Method

In this section, the average value of the frequency (i.e.,  $\Delta f_{mean}$ ) is determined and a new detection index is introduced. The average value of the frequency deviation is written, as follows:

$$\Delta f_{mean} = \frac{1}{T_d} \int_0^{T_d} \Delta f(t) dt$$
(11)

where,  $T_d$  is the fundamental period of the frequency deviation determined by Eq. (7), as follows:

$$\omega_{d} = 2\pi f_{d} = \frac{2\pi}{T_{d}} \Longrightarrow T_{d} = \frac{2\pi}{\omega_{n}\sqrt{1-\varsigma^{2}}}$$
(12)

Now, Eq. (11) should be calculated for both operation modes.

a) For grid-connected mode, by Eq. (4) and Eq. (11), the frequency deviation will be determined, as follows:

$$\Delta f_{mean-on} = \frac{1}{T_d} \int_0^{T_d} -\frac{\omega_n \Delta \delta_0}{2\pi \sqrt{1-\varsigma^2}} e^{-\varsigma \omega_n t} \sin(\omega_d t) dt$$
$$= \frac{1}{T_d} \frac{-\omega_n \Delta \delta_0}{2\pi \sqrt{1-\varsigma^2}} \left[ \frac{\omega_d \left(1-e^{-\varsigma \omega_n T_d}\right)}{\left(\varsigma \omega_n\right)^2 + \omega_d^2} \right]$$
(13)

Using Eq. (7), the simpler form can be obtained, as follows:

$$\Delta f_{mean-on} = \frac{-\Delta \delta_0}{2\pi T_d} \left[ 1 - e^{-\varsigma \omega_n T_d} \right]$$
(14)

where,  $\Delta \delta_0$  is the initial rotor angle deviation which can be created in different disturbances of the power systems.

b) For islanding condition, by Eq. (10) and Eq. (11), the frequency deviation will be calculated, as follows:

$$\Delta f_{mean-off} = \frac{1}{T_d} \int_0^{T_d} \frac{\Delta P}{D} \left( 1 - e^{-2\varsigma \omega_n t} \right) dt$$
$$= \frac{\Delta P}{T_d \cdot D} \left[ T_d + \frac{1}{2\varsigma \omega_n} e^{-2\varsigma \omega_n T_d} - \frac{1}{2\varsigma \omega_n} \right]$$
(15)

To analyze the performance of the proposed method and assessment of its Non–Detection Zone (NDZ), the critical power imbalance of the method must be calculated. The critical power imbalance is the minimum power deviation which one islanding detection method can discriminate between two operation modes using it. The mentioned power deviation is described as a difference between produced and absorbed electrical power by DGs and loads, respectively.

The critical power imbalance of the proposed method is determined by the following inequality:

$$\left|\frac{\Delta f_{mean-off}}{\Delta f_{mean-on}}\right| > 1 \tag{16}$$

Eq. (16), can be rewritten, as follows:

$$\frac{\frac{\Delta P}{T_d \cdot D} \left[ T_d + \frac{1}{2\varsigma \omega_n} e^{-2\varsigma \omega_n T_d} - \frac{1}{2\varsigma \omega_n} \right]}{\frac{-\Delta \delta_0}{2\pi T_d} \left[ 1 - e^{-\varsigma \omega_n T_d} \right]} > 1$$
(17)

This inequality can be also written in the following form:

T

$$\Delta P > \left| \frac{\Delta \delta_0 D}{2\pi} \frac{\left[ 1 - e^{-\varsigma \omega_n T_d} \right]}{\left[ T_d + \frac{1}{2\varsigma \omega_n} e^{-2\varsigma \omega_n T_d} - \frac{1}{2\varsigma \omega_n} \right]} \right| = \left| \psi \right|$$
(18)

Then, the non-detection zone of proposed method is introduced, as follows:

$$-\psi < \Delta P_{NDZ} < \psi \tag{19}$$

To study the performance of the proposed method, the critical power imbalance (i.e.,  $\Delta P_{critical} = \psi$ ) and the coefficient  $k = \zeta \omega_n T_d$  should be considered. The time

T



**Fig. 2** Variation of f(k) versus k.

constant of the frequency deviation signal is represented by  $\tau = 1/\zeta \omega_n$  and for all damped sinusoidal signals, the settling time is about four times of the time constant (i.e.,  $t_{settling} = 4/\zeta \omega_n$ ) [32]. In the other words, the settling time of the frequency deviation signal is about 2 to 8 times of the fundamental period. Therefore, we have:

$$0.5 < \varsigma \omega_n T_d < 2 \quad or \quad 0.5 < k < 2 \tag{20}$$

Using Eq. (18), the critical active power imbalance can be expressed by the following equation:

$$\psi = \frac{\Delta \delta_0 D}{\pi T_d} f(k) \tag{21}$$

where, f(k) is defined, as follows:

$$f(k) = \frac{k(1 - e^{-k})}{(2k - 1) + e^{-2k}}$$
(22)

Fig. 2, shows f(k) versus k. According to this figure, the maximum value of f(k) is 0.5733 at k = 2.2. So, the worst case is f(2) = 0.5729 for  $\psi$ . In Eq. (21),  $\Delta \delta_0$  is the initial rotor angle deviation that occurs in the presence of a disturbance in the power network. This parameter is in radian and it can be converted into degree. Then, Eq. (21) can be rewritten, as follows:

$$\psi = \frac{\Delta \delta_0}{180} \frac{D}{T_d} \times 0.5729 \tag{23}$$

In Eq. (23),  $D/T_d$  is an important parameter which has a vital role to reduce NDZ of the proposed method. Although,  $D/T_d$  is characterized by all of parameters of the synchronous distributed generator and has different values but its range can be estimated. To achieve a NDZ smaller than 5 percent in the proposed method for different types of synchronous distributed generators,  $D/T_d$  is better to be lower than 1. In the following paragraphs, it will be shown that  $D/T_d$  in existing synchronous distributed generators is smaller than 1. From Eq. (5) and Eq. (6) the following equations can be written:

$$\varsigma \omega_n = \frac{D\omega_b}{4H} \Rightarrow D = \frac{4H.\varsigma\omega_n}{\omega_b}$$
or,  $T_d D = \frac{4H(T_d \varsigma \omega_n)}{\omega_b} = \frac{4H}{\omega_b} k$ 
or,  $\frac{D}{T_d} = \frac{4k}{\omega_b} \left(\frac{H}{T_d^2}\right)$ 
(24)

where,  $\omega_b$  and *H* are synchronous speed of DG and inertia constant, respectively. For k = 2 and  $\omega_b = 2\pi.60$ , the worst case for the biggest value of  $D/T_d$  is, as follows:

$$\frac{D}{T_d} \cong 0.0212 \left(\frac{H}{T_d^2}\right) \tag{25}$$

In this equation, *H* is an important parameter to evaluate the  $D/T_d$ . According to [30, 31],  $0.5^{\rm s} \le H \le 10^{\rm s}$ . This constant depends on the machine size. Hence, *H* of synchronous distributed generators in distribution networks is lower than four [9, 13, 25, 29]. Then, the fundamental period of the frequency deviation or  $T_d$ , is changed from 0.15 to 1.5s. For example, in the case study, which will be presented in the next section, H = 1.5s and  $T_d = 0.33$ s. Thus, we have:

$$\frac{D}{T_d} \cong 0.0212 \left(\frac{1.5}{0.33^2}\right) \cong 0.292$$
(26)

As it can be seen the result is smaller than one. It should be noted that  $T_d$  is proportional to H. this means that the high value of H needs more time for oscillations. In Fig. 3, the rotor speed variations for four different values of inertia constant of one typical synchronous DG have been simulated and shown.  $D/T_d$  for four cases has been determined, as follows:

For 
$$\begin{cases} H = 0.5\\ T_d = 0.22 \end{cases} \Rightarrow \frac{D}{T_d} \approx 0.2190 \tag{27}$$



Fig. 3 Behavior of rotor speed deviation for different H.

For 
$$\begin{cases} H = 1.5\\ T_d = 0.4 \end{cases} \stackrel{\frown}{\Rightarrow} \frac{D}{T_d} \cong 0.19875 \tag{28}$$

For 
$$\begin{cases} H = 3.0 \\ T_d = 0.6 \Rightarrow \frac{D}{T_d} \approx 0.17\overline{6} \end{cases}$$
(29)

For 
$$\begin{cases} H = 4.0\\ T_d = 0.7 \Rightarrow \frac{D}{T_d} \approx 0.17306 \end{cases}$$
(30)

Considering the aforementioned results, it can be said that  $D/T_d$  for the most of DGs is smaller than one and in the worst case, it is equal to 1. Consequently,  $D/T_d = 1$  can be substituted in Eq. (23), as follows:

$$\psi = 0.5729 \frac{\Delta \delta_0}{180} \tag{31}$$

In this equation,  $\Delta \delta_0$  has a vital role to determine the limits of islanding and non–islanding conditions. To illustrate the discrimination procedure of the proposed method, the following two criterions must be considered.

1. If  $\Delta \delta_0 \leq 10^{\circ}$ 

For this condition, the frequency variations certainly are in acceptable range (i.e.,  $59.3^{Hz} \le f \le 60.5^{Hz}$ ) [3]. Thus, over/under frequency protections will not operate. Consequently, NDZ could be written, as follows:

$$\psi(pu) \le 0.5729 \frac{10}{180} \ge 0.03182$$
  
 $\psi \le 3.182\%$  (32)

2. If  $\Delta \delta_0 \ge 10^\circ$ 

For this situation, frequency probably exceeds its acceptable range and over/under frequency protections for more cases will operate. If frequency variations were remained in acceptable range, NDZ of the method could be achieved, as follows:

$$\psi(pu) \ge 0.5729 \frac{10}{180} \ge 0.03182$$
  
 $\psi \ge 3.182\%$  (33)

#### 2.3 Procedure of Proposed Method

In this subsection, the calculation procedure of  $f_{mean}$  is described. To calculate the  $f_{mean}$ , both procedures, i.e. the voltage zero crossing and the rotor speed have used. After the computation of  $f_{mean}$ , the detection index is calculated, as follows:

$$D_{on/off} = k_g \left| \Delta f_{mean-on/off} \right|$$
(34)

where,  $\Delta f_{mean}$  is  $(f_b - f_{mean})$  and  $f_b$  and D are the fundamental frequency and the detection index of the proposed method, respectively. The  $k_g$  is a gain, adjusted to 100. The flowchart of the proposed method is shown in Fig. 4. In this figure,  $D_{th1}$  is the first threshold value of the detection index, which can be acquired from comparing islanding and non- islanding cases. Using Eqs. (14) and (15) for  $\Delta P = 3\%$  and  $\Delta \delta_0 = 10^{\circ}$ , different detection parameters have been represented in Table 1.

Table 1. Detection indices for both case study systems.

|                  |                     | $D_{on}^{*}$ | $D_{off}$ | $D_{th1}$ | $D_{th2}$ |
|------------------|---------------------|--------------|-----------|-----------|-----------|
| First<br>system  | SDG                 | 8.10         | 10.32     | 8         | 32        |
| Second<br>system | Gas<br>Turbine      | 9.62         | 12.86     | 9         | 36        |
|                  | Diesel<br>Generator | 10.37        | 13.42     | 10        | 40        |

\*The unit of D is Hertz.



Fig. 4 Flowchart of proposed method.

### 3 Simulation Results and Discussion

To verify the effectiveness of the proposed method, various islanding and non-islanding occurrences have been applied on the case study systems as shown in Figs. 5 and 6. For both under study systems, sixth–order model of SDG for simulations is used. More information about first and second case study systems can be found in [12] and [29], respectively. It should be noted that all simulations have been carried out in Matlab/SimPowerSystem software environment. The most important disturbances which may result in wrong performance of islanding detection methods are short circuit faults, load variations and capacitor bank switching. In this paper, 55 different islanding and non–islanding cases have been studied by the proposed



Fig. 5 Single line diagram of first case study system.



Fig. 6 Single line diagram of second case study system.

|                              |                                 |                                    | 01      |                                  | 5                     |                  |
|------------------------------|---------------------------------|------------------------------------|---------|----------------------------------|-----------------------|------------------|
| Disturbance                  | Explain                         | $f_{mean}\left(\mathbf{Hz}\right)$ | D (Hz)  | Exceeds<br>from V <sub>min</sub> | Detection by          | Classification   |
|                              | $R_f = 11$                      | 59.81194                           | 18.806  | Yes                              | UVP                   | Non- islanding   |
| Three phase to ground faults | $\dot{R_f} = 15$                | 59.83105                           | 16.895  | Yes                              | UVP                   |                  |
| (ahm)                        | $R_{f} = 20$                    | 59.86752                           | 13.248  | Yes                              | UVP                   |                  |
| (onn)                        | $\dot{R}_f = 1$                 | 59.76596                           | 23.404  | Yes                              | UVP                   |                  |
|                              | $R_f = 7$                       | 59.81310                           | 18.690  | Yes                              | UVP                   |                  |
| Double line to ground faults | $R_{f} = 15$                    | 59.91235                           | 8.765   | Yes                              | UVP                   | Non- islanding   |
| (ohm)                        | $R_{f} = 30$                    | 59.95681                           | 4.319   | Yes                              | UVP                   | i ton ibianang   |
|                              | $R_f = 5$                       | 59.88311                           | 11.689  | Yes                              | UVP                   |                  |
| Single line to ground faults | $R_{f}^{\prime} = 10$           | 59.91728                           | 8.272   | Yes                              | UVP                   | Non- islanding   |
| (ohm)                        | $R_{f}^{'}=20$                  | 59.94312                           | 5.688   | No                               | $D_{thl}$             | ittoir ibianaing |
|                              | $O_{c} = 40$                    | 59 99552                           | 0.448   | No                               | Data                  |                  |
| Capacitor switching off      | $Q_c = 30$                      | 60.00198                           | 0.198   | No                               | $D_{th1}$             | Non islanding    |
| (Mvar)                       | $Q_c = 20$                      | 60.00170                           | 0.030   | No                               | $D_{th1}$             | Non- Islanding   |
|                              | <u>2</u> ( <u>2</u> 0           | 60.00050                           | 0.050   | N                                |                       |                  |
| Capacitor switching on       | $Q_C = 40$                      | 60.008/6                           | 0.876   | No                               | $D_{thl}$             |                  |
| (Myar)                       | $Q_C = 30$                      | 60.00793                           | 0.793   | No                               | $D_{thl}$             | Non- islanding   |
| (                            | $Q_C = 20$                      | 60.00521                           | 0.521   | No                               | $D_{thl}$             |                  |
| RLC load switching off       | S = 40 + j 30                   | 59.98999                           | 1.001   | No                               | $D_{thl}$             |                  |
|                              | S = 30 + j 20                   | 60.00992                           | 0.992   | No                               | $D_{thl}$             | Non- islanding   |
| (MW + J MVar)                | $S = 20 + j \ 10$               | 60.00705                           | 0.705   | No                               | $D_{thl}$             | C C              |
| RLC load switching on        | S = 40 + i 30                   | 60.01895                           | 1.895   | No                               | $D_{thl}$             |                  |
|                              | S = 30 + i 20                   | 59.99190                           | 0.810   | No                               | $D_{thl}$             | Non- islanding   |
| (MW + J Mvar)                | $S = 20 + j \ 10$               | 59.99333                           | 0.667   | No                               | $D_{thl}$             | i ton ibianang   |
| C B2 or C B3 switching off   | $\Delta P = 2.7$                |                                    |         |                                  |                       |                  |
| (percent)                    | $\Delta Q = 4$                  | 60.18375                           | 18.375  | No                               | $D_{thl}$             | Islanding        |
|                              | - <u>z</u>                      |                                    |         |                                  |                       |                  |
| C.B2 or C.B3 switching off   | $\Delta P = -2$                 | 59.84654                           | 15.346  | No                               | $D_{thl}$             | Islanding        |
| (percent)                    | $\Delta Q = 8$                  |                                    |         |                                  |                       |                  |
| C.B2 or C.B3 switching off   | $\Delta P = 8$                  | 60.60548                           | 60.548  | No                               | Det & Det 2           | Islanding        |
| (percent)                    | $\Delta Q = -3$                 |                                    |         |                                  | -in1 = -in2           | 8                |
| C.B2 or C.B3 switching off   | $\Delta P = 40$                 | 62 92079                           | 202 070 | Vac                              | OED& D                | Islanding        |
| (percent)                    | $\Delta Q = 60$                 | 05.82078                           | 382.078 | res                              | $OFP \alpha D_{th2}$  | Islanding        |
| C B2 or C B3 switching off   | $\Lambda P = 2.2$               |                                    |         |                                  |                       |                  |
| (nercent)                    | $\Delta I = 5.5$ $\Delta O = 0$ | 60.21956                           | 21.956  | No                               | $D_{thl}$             | Islanding        |
| (percent)                    | Δ <u>φ</u> 0                    |                                    |         |                                  |                       |                  |
| C.B2 or C.B3 switching off   | $\Delta P = -6$                 | 59 58752                           | 41 248  | No                               | D                     | Islanding        |
| (percent)                    | $\Delta Q = -5.5$               | 57.50752                           | 71.270  | 140                              | ₽ th1                 | istanding        |
| C B2 or C B3 switching off   | $\Delta P = -16.5$              |                                    |         |                                  |                       |                  |
| (percent)                    | $\Delta O = 10$                 | 59.05327                           | 94.673  | No                               | $D_{th1}$ & $D_{th2}$ | Islanding        |
| (r                           | -z ···                          |                                    |         |                                  |                       |                  |

Table 2. Classification of different islanding and non-islanding conditions using proposed method on the first system.

| Disturbance                     | Explain   | $D_{DGI}(\mathrm{Hz})$ | $D_{DG2}(\text{Hz})$ | Exceeds<br>from V <sub>min</sub> 1 | Exceeds<br>from V <sub>min</sub> 2 | Detection<br>by           | Classification                      |
|---------------------------------|---|------------------------|----------------------|------------------------------------|------------------------------------|---------------------------|-------------------------------------|
| C.B1 switching off<br>(percent) | $\Delta P_1 = 3$ $\Delta Q_1 = -5$  | 16.650                 | 0.0635               | No                                 | No                                 | $D_{thI}$                 | Islanding of DG <sub>1</sub>        |
| C.B1 switching off<br>(percent) | $\Delta P_1 = 2.5$ $\Delta Q_1 = 3$                                       | 10.320                 | 0.0638               | No                                 | No                                 | $D_{thl}$                 | Islanding of DG <sub>1</sub>        |
| C.B1 switching off<br>(percent) | $\Delta P_1 = -60$ $\Delta Q_1 = 25$                                      | 303.20                 | 0.0843               | No                                 | No                                 | UFP &<br>D <sub>th1</sub> | Islanding of DG <sub>1</sub>        |
| C.B1 switching off<br>(percent) | $\Delta P_1 = 25$ $\Delta Q_1 = -25$                                      | 37.527                 | 0.1270               | Yes                                | Yes                                | D <sub>th2</sub>          | Islanding of DG <sub>1</sub>        |
| C.B1 switching off<br>(percent) | $\Delta P_1 = 40$ $\Delta Q_1 = 5$  | 177.81                 | 0.3611               | Yes                                | Yes                                | $OFP \& D_{th2}$          | Islanding of DG <sub>1</sub>        |
| C.B2 switching off<br>(percent) | $\Delta P_2 = 4.5$ $\Delta Q_2 = -4$                                      | 31.280                 | 0.0921               | No                                 | No                                 | $D_{thl}$                 | Islanding of DG <sub>2</sub>        |
| C.B2 switching off<br>(percent) | $\Delta P_2 = -3$ $\Delta Q_2 = -1$                                       | 13.120                 | 0.0484               | No                                 | No                                 | $D_{thl}$                 | Islanding of DG <sub>2</sub>        |
| C.B2 switching off<br>(percent) | $\Delta P_2 = 3.2$ $\Delta Q_2 = 3$                                       | 22.850                 | 0.0658               | No                                 | No                                 | $D_{thl}$                 | Islanding of DG <sub>2</sub>        |
| C.B2 switching off<br>(percent) | $\Delta P_2 = 2$ $\Delta Q_2 = 3$   | 13.390                 | 0.0339               | No                                 | No                                 | $D_{thl}$                 | Islanding of DG <sub>2</sub>        |
| C.B2 switching off<br>(percent) | $\Delta P_2 = -16$ $\Delta Q_2 = 5$                                       | 89.490                 | 0.2626               | No                                 | No                                 | UFP &<br>D <sub>th1</sub> | Islanding of DG <sub>2</sub>        |
| C.B2 switching off<br>(percent) | $\Delta P_2 = 55$ $\Delta Q_2 = -33$                                      | 306.50                 | 1.5450               | yes                                | yes                                | $D_{th2}$                 | Islanding of DG <sub>2</sub>        |
| C.B3 switching off<br>(percent) | $\Delta P_1 = 8$ $\Delta Q_1 = -10$ $\Delta P_2 = 10$ $\Delta Q_2 = -8$   | 53.140                 | 54.610               | No                                 | No                                 | $D_{th1}$                 | Islanding of both $DG_1$ and $DG_2$ |
| C.B3 switching off<br>(percent) | $\Delta P_1 = 5$ $\Delta Q_1 = -8$ $\Delta P_2 = 7$ $\Delta Q_2 = -6$     | 32.091                 | 33.045               | No                                 | No                                 | D <sub>th1</sub>          | Islanding of both $DG_1$ and $DG_2$ |
| C.B3 switching off<br>(percent) | $\Delta P_1 = -2.5$ $\Delta Q_1 = 2$ $\Delta P_2 = -2.5$ $\Delta Q_2 = 2$ | 11.950                 | 12.389               | No                                 | No                                 | D <sub>th1</sub>          | Islanding of both $DG_1$ and $DG_2$ |

Table 3. Classification of different Islanding conditions using proposed method on the second system.

method. The phase–locked loop block with three phase voltage of DG is used to achieve the frequency waveform. From Fig. 4, the proposed method has been introduced as supplementary protection of Over/Under Frequency Protection (OFP/UFP). To prevent sending of any undesired trip signal for sever disturbances like three phases faults, Under Voltage Protection (UVP) has also been used. The acceptable range of voltage is 0.88 pu–1.1 pu [3]. In the case of frequency and regarding the IEEE standard–1547, variations should be in the range of 59.3-60.5 Hz [3]. The simulated short circuit faults are Single Line to Ground (SLG), Double Line to Ground (DLG) and three phases with different fault

resistances. It should be noted that the short circuit duration of all faults is 6 cycles and both islanding and non–islanding disturbances start at t = 2s.

Eventually, Tables 2-4, present the detection index for all of the disturbances. Table 2, depicts the tested results of the proposed method on the first case study system and Tables 3, 4 are related to the second case study system.

In these tables, the subscript "1" and "2" indicates gas turbine and diesel generator on the second case study systems. From Table 2, although, it can be seen for more faults, the detection index exceeds from first threshold but UVP detects these disturbances as non-

| Disturbance                                      | Explain      | $D_{DGI}$ | $D_{DG2}$ | Exceeds                 | Exceeds                 | Detection by | Classification |
|--|--------------|-----------|-----------|-------------------------|-------------------------|--------------|----------------|
|  | <b>F</b>     | (Hz)      | (Hz)      | from V <sub>min</sub> 1 | from V <sub>min</sub> 2 |              |                |
| Three phase to ground                            | $R_f = 5$    | 1.7040    | 8.9760    | Yes                     | Yes                     | UVP          | Non islanding  |
| faults (ohm) line CD                             | $R_{f} = 10$ | 2.0429    | 3.5384    | Yes                     | Yes                     | UVP          | Non- Islanding |
| Three phase to ground<br>faults (ohm) line BC    | $R_f = 5$    | 1.2720    | 8.5436    | Yes                     | Yes                     | UVP          | Non islanding  |
|  | $R_{f} = 10$ | 1.2174    | 3.6059    | Yes                     | Yes                     | UVP          | Non- Islanding |
| Three phase to ground<br>faults (ohm) bus D      | $R_f = 5$    | 2.0634    | 8.8741    | Yes                     | Yes                     | UVP          | Non islanding  |
|  | $R_{f} = 10$ | 2.9223    | 3.3374    | Yes                     | Yes                     | UVP          | Non- Islanding |
| DLG faults (ohm) line CD                         | $R_f = 5$    | 1.9375    | 4.7761    | Yes                     | Yes                     | UVP          | Nen islandini  |
|  | $R_{f} = 10$ | 1.3308    | 2.2294    | Yes                     | Yes                     | UVP          | Non- Islanding |
| DLC faults (abm) line PC                         | $R_f = 5$    | 1.1524    | 4.9517    | Yes                     | Yes                     | UVP          | Non islanding  |
| DLO lautis (olilii) lille BC                     | $R_{f} = 10$ | 0.7544    | 2.3576    | Yes                     | Yes                     | UVP          | Non- Islanding |
| DLC faults (share) has D                         | $R_f = 5$    | 2.6814    | 4.4321    | Yes                     | Yes                     | UVP          | Nen islanding  |
| DLG faults (ohm) bus D                           | $R_{f} = 10$ | 2.0084    | 2.0213    | Yes                     | Yes                     | UVP          | Non- Islanding |
| SI C faulta (ahm) lina CD                        | $R_f = 5$    | 1.1445    | 1.7914    | Yes                     | Yes                     | UVP          | Non- islanding |
| SLG faults (ohm) line CD                         | $R_{f} = 10$ | 0.6507    | 1.0024    | No                      | No                      | $D_{th1}$    |                |
| SLC faults (abm) line DC                         | $R_f = 5$    | 0.6352    | 2.0487    | Yes                     | Yes                     | UVP          | Non- islanding |
| SLG faults (ohm) line BC                         | $R_{f} = 10$ | 1.1770    | 0.3412    | No                      | No                      | $D_{thl}$    |                |
| SLC faults (alma) hus D                          | $R_f = 5$    | 1.6968    | 1.5290    | Yes                     | Yes                     | UVP          | Non islanding  |
| SLO fauns (onin) bus D                           | $R_{f} = 10$ | 0.8753    | 0.9982    | No                      | No                      | $D_{thI}$    | Non- Islanding |
| Capacitor switching off                          | $Q_C = 6$    | 0.1045    | 0.3061    | No                      | No                      | $D_{thl}$    |                |
| (Myar) on bus C                                  | $Q_C = 4$    | 0.0523    | 0.1959    | No                      | No                      | $D_{thl}$    | Non- islanding |
|  | $Q_C = 2$    | 0.0070    | 0.0823    | No                      | No                      | $D_{thl}$    |                |
| Capacitor switching on                           | $Q_C = 6$    | 0.1390    | 0.2236    | No                      | No                      | $D_{thl}$    |                |
| (Myar) on bus C                                  | $Q_C = 4$    | 0.1117    | 0.1548    | No                      | No                      | $D_{thl}$    | Non- islanding |
|  | $Q_C = 2$    | 0.0869    | 0.0924    | No                      | No                      | $D_{thl}$    |                |
| RLC load switching off $(MW + i Myar)$ on hus E  | S = 6 + j 4  | 0.0569    | 0.0212    | No                      | No                      | $D_{thl}$    |                |
|  | S = 4 + j 2  | 0.0478    | 0.0184    | No                      | No                      | $D_{thl}$    | Non- islanding |
|  | S = 2 + j 1  | 0.0358    | 0.0152    | No                      | No                      | $D_{thl}$    |                |
| RLC load switching on<br>(MW + j Mvar) on bus E  | S = 6 + j 4  | 0.0575    | 0.0233    | No                      | No                      | $D_{thl}$    |                |
|  | S = 4 + j 2  | 0.0483    | 0.0196    | No                      | No                      | $D_{thl}$    | Non- islanding |
|  | S = 2 + j 1  | 0.0371    | 0.0168    | No                      | No                      | $D_{thl}$    |                |
| RLC load switching off<br>(MW + j Mvar) on bus D | S = 6 + j 4  | 0.1031    | 0.1224    | No                      | No                      | $D_{thl}$    |                |
|  | S = 4 + j 2  | 0.1285    | 0.0549    | No                      | No                      | $D_{thl}$    | Non- islanding |
|  | S = 2 + j 1  | 0.0502    | 0.0474    | No                      | No                      | $D_{thl}$    |                |
| DLC load arritahing ar                           | S = 6 + j 4  | 0.0476    | 0.1514    | No                      | No                      | $D_{thl}$    |                |
| $(MW \pm i Myor)$ on by D                        | S = 4 + j 2  | 0.0360    | 0.1469    | No                      | No                      | $D_{thl}$    | Non- islanding |
| (W W + J W V ar) on bus D                        | S = 2 + j 1  | 0.0248    | 0.1273    | No                      | No                      | $D_{thl}$    |                |

Table 4. Classification of different Non-islanding conditions using proposed method on the second system.

islanding conditions. In this paper, averaging time in all of the simulations has been adjusted to  $t = T_d$  s. According to the IEEE standard–1547, the maximum allowable time to detect the islanding situation is 2s. Typically, the time of the islanding detection depends upon the magnitude of active and reactive power imbalances. For small power mismatches, the islanding situation should be detected within two seconds whereas for large power mismatches, this time is reduced to 0.160s. The amount of  $T_d$  is different for various types

of synchronous machine–based DGs. For example, in first case study system, DG has a  $T_d$  of 0.338s and for second case study,  $T_{d1}$ =0.280s and  $T_{d2}$ =0.275s. For these cases (i.e.,  $T_d > 160$ ms), it is better to use the OFP/UFP with the proposed method, because in large power mismatches, OFP/UFP has good performance and can detect the islanding condition quickly (i.e.,  $t < 160^{\text{ms}}$ ) [21]. These conditions have been shown in Table 2 and 3 for large values of  $\Delta P$  and  $\Delta Q$ . The coordination of the OFP/UFP and proposed method result in a better

performance and lesser NDZ. In the case of second system and at the first attempt, both SDGs have been islanded, separately. For this situation, the proposed method operated, excellently. For second attempt, both gas turbine and diesel generator have been islanded, simultaneously. In this condition the proposed method could detect the islanding events with active power imbalances up to 2.5%.

# 4 Comparison of Proposed Method with Two Passive Methods

### 4.1 ROCOF Method

The ROCOF relay is a simple method to detect the islanding conditions, which is considered by many utilities. Although, the implementation of this method is very simple and cheaper than the other methods but in small power mismatches has a poor performance and cannot correctly detect the islanding condition. Thus, in this paper, the proposed method is compared with



**Fig. 7** Frequency of DG (a), output of ROCOF (b), trip signal of proposed method (c) and trip signal of ROCOF relay (d) in islanding conditions with  $\Delta P$ =3.3% and  $\Delta Q$ =0% at first system.



**Fig. 8** Frequency of DG (a), output of ROCOF (b), trip signal of proposed method (c) and trip signal of ROCOF relay (d) in islanding conditions with  $\Delta P$ =-2 % and  $\Delta Q$ =8% at first system.

ROCOF relay. According to this method, the rate of change of frequency after crossing of a 1<sup>st</sup> order filter is computed and it is compared with a preset threshold value. The 1st order filter is used to reduce high frequency transients. It should be noted that before sending a trip signal, the terminal voltage of DG must be compared with a  $V_{Min}$  to prevent an undesired trip, which is caused by generator startup and short circuit faults. The threshold value of the ROCOF relay is changed between 0.3 Hz/s to 2.5 Hz/s. Therefore, in this study by considering many scenarios such as short circuit faults, capacitor bank switching and load changing; threshold value is selected to 2 Hz/s. Figs. 7-10, depict the trip signals of proposed method and ROCOF relay for special islanding and non-islanding conditions. In this figures, it can be seen that for -2%and +3.3% of active power mismatches, the ROCOF relay has a poor performance and cannot detect the islanding conditions.



**Fig. 9** Frequency of DG (a), output of ROCOF (b), trip signal of proposed method (c) and trip signal of ROCOF relay (d) for 30 MW and 20 Mvar of load shedding at first system.



**Fig 10.** Frequency of DG (a), output of ROCOF (b), trip signal of proposed method (c) and trip signal of ROCOF relay (d) for three phases fault with  $R_f = 1$  ohm at first system.

The NDZ of ROCOF relay in same conditions for both proposed method and ROCOF relay is more than 10%. Fig. 9 shows the wrong decision of ROCOF relay for a sample of load shedding. Finally, Fig. 10 depicts the correct decision of proposed method, when encountered with sever disturbance. As a result, although the ROCOF relay in large power mismatches (larger than 10% of active power mismatches) has a good performance and can quickly detect the islanding conditions but has a large NDZ.

### 4.2 Rate of Change of Frequency over Power

This method was introduced for the first time in [16]. Unlike of the ROCOF method, this procedure is more sensitive and has lower NDZ than the ROCOF. Also, this technique has two different threshold preset values. Thus, adjusting of these two parameters is rather difficult problem. Overall procedure of rate of change of frequency over power (ROCOFOP) method is based on comparing of output signal with first threshold; in this case, if output value of signal is larger than the first threshold, an embedded counter is incremented by one. Finally, by encroachment of counter value from second threshold, ROCOFOP proceeds to send a trip command. In the paper, this method is implemented in



Fig. 11 Output results of ROCOFOP for non-islanding situations at first system.



**Fig 12.** Output results of ROCOFOP for a few of islanding situations at first system.

Matlab environment on the case study system. The sample results of this method are depicted in Figs. 11 and 12. To reduce the false trip commands for nonislanding situations, the first and second thresholds are adjusted to 3 and 4, respectively. These threshold values are selected based on simulation results of different nonislanding situations. For the larger values than the adjusted values, in the case of thresholds, both parameters of detection time and NDZ criteria are increased. On the other hand, the lower values create false trips. Thus, in the paper, with these adjusted values for thresholds, the ROCOFOP method has an undesired trip for a special three phase fault. This status has been shown in Fig. 11-b. According to this figure, when the ROCOFOP method encounters with three phases fault, sends a trip command. This disturbance describes voltage sag, which causes a SDG terminal voltage drop of 20%. The time for all faults is six cycles. Fig. 12 depicts the results of the ROCOFOP method in islanding conditions. It is obvious that the ROCOFOP method has relatively large NDZ. For islanding condition with  $\Delta P = 15\%$ , this method can detect the islanding condition within 0.283s. For lower values, the performance of the ROCOFOP is reduced but in comparison with ROCOF, it is the better choice. For example, the ROCOFOP method can detect the islanding condition with  $\Delta P = 7\%$  within 0.717s, whereas the proposed method with  $\Delta P = 2.7\%$  and the detection time of 0.338s (first system) for islanding condition has robust performance. Also, for larger than 5% of active power mismatches, the ROCOFOP method can detect the islanding in more than 1s, whereas the proposed method for the same condition has the detection time of 0.338s (first system). It is necessary to note that for implementation of the ROCOFOP method, its output signal must be discrete. The discretisation process has been carried out through one Zero-Order-Hold (ZOH) filter. In this paper, this process with frequency of  $f_b$ , which is adjusted to 60 Hz, has been accomplished. Eventually, the proposed method in comparison with two typical passive methods is effective and has a robust performance and good capability to detect the islanding conditions with small active power mismatches up to 3%.

### 5 Conclusion

This paper has proposed a new islanding detection method based on average value of frequency. By monitoring the frequency of the DG and calculating its average value, the proposed method can detect the islanding situation. Although this method is an integralbased method and has a rather long detection time but in comparison with derivative-based methods (e.g., ROCOF and ROCOFOP) has small NDZ. In fact, the proposed method is an effective supplement for OFP/UFP, which can reduce NDZ of OFP/UFP to less than 3%. To evaluate the performance and capability of the proposed method, two approaches have been presented through analytical and simulation based approaches. Different islanding and non-islanding cases such as short circuit faults, capacitor bank switching and load changes in various values and locations of the test systems have been studied. In addition, the proposed method has been compared with both ROCOF and ROCOFOP methods and it has been shown that the proposed method for active power mismatches smaller than 10% has better performance and for larger than 10%, because of existing OFP/UFP in structure of proposed method as back up protection, the same capability of both ROCOF and ROCOFOP methods has been established.

### Appendix

### A. Simplified Swing Equation

The following equation presents the swing equation [30, 31]:

$$\frac{2H}{\omega_b}\frac{d^2\delta}{dt^2} + D\frac{d\delta}{dt} = P_m - P_{\max}\sin(\delta)$$
 (A-1)

If a part of the system encountered with a disturbance and the rotor angle ( $\delta$ ) has a small variation, the following equation can be written:

$$\frac{2H}{\omega_b} \frac{d^2}{dt^2} (\delta_0 + \Delta\delta) + D \frac{d}{dt} (\delta_0 + \Delta\delta)$$

$$= P_m - P_{\max} \sin(\delta_0 + \Delta\delta)$$
(A-2)

This equation can be rewritten, as follows:

$$\frac{2H}{\omega_b} \frac{d^2 \delta_0}{dt^2} + \frac{2H}{\omega_b} \frac{d^2 \Delta \delta}{dt^2} + D \frac{d \delta_0}{dt} + D \frac{d \Delta \delta}{dt}$$
$$= P_m - P_{\max} [\sin \delta_0 \cos \Delta \delta + \sin \Delta \delta \cos \delta_0] \qquad (A-3)$$

If the rotor angle deviation has a small variation ( $\Delta \delta \leq 10^{\circ}$ ), by substituting sin ( $\Delta \delta$ ) with  $\Delta \delta$  and cos ( $\Delta \delta$ ) with 1, the above mentioned equation is converted to the following two simple equations. The first equation (i.e.,

(A-4)) expresses the behavior of the power system in steady state condition and the second one (i.e., (A-5)) expresses the transition state of the synchronous generator.

$$\frac{2H}{\omega_{b}}\frac{d^{2}\delta_{0}}{dt^{2}} + D\frac{d\delta_{0}}{dt} = P_{m} - P_{\max}\sin(\delta_{0})$$
(A-4)

$$\frac{2H}{\omega_b} \frac{d^2 \Delta \delta}{dt^2} + D \frac{d\Delta \delta}{dt} = -P_{\text{max}} \cos(\Delta \delta)$$
(A-5)

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